



# **A Mode-Based Hybrid Controller Design for Agile Maneuvering Unmanned F-16 Aircraft**

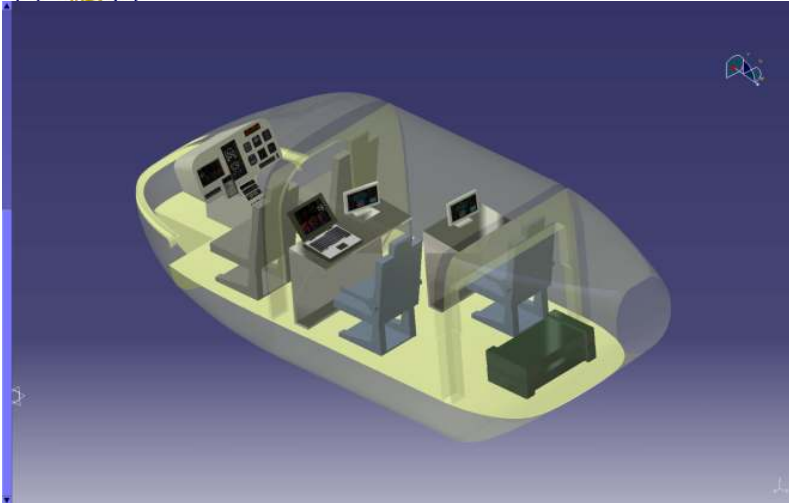
N. Kemal Ure, Prof. Gokhan Inalhan

*Istanbul Technical University*

*Controls and Avionics Laboratory*



# CAL INDUSTRIAL PROJECTS



*İTÜ LCH AVIONICS  
SYSTEMS*

- Primary Funding Sources
  - DPT
  - ASELSAN

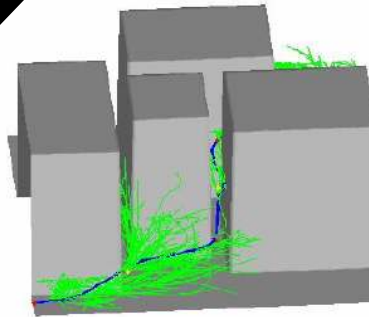
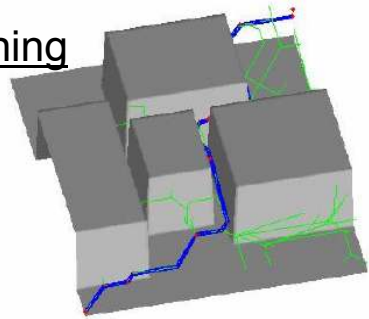
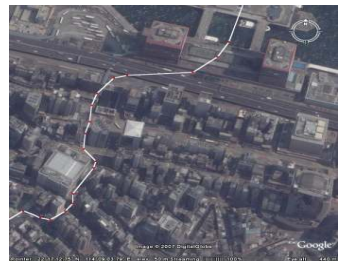


*İTÜ ASELSAN Research  
Flight Simulator*

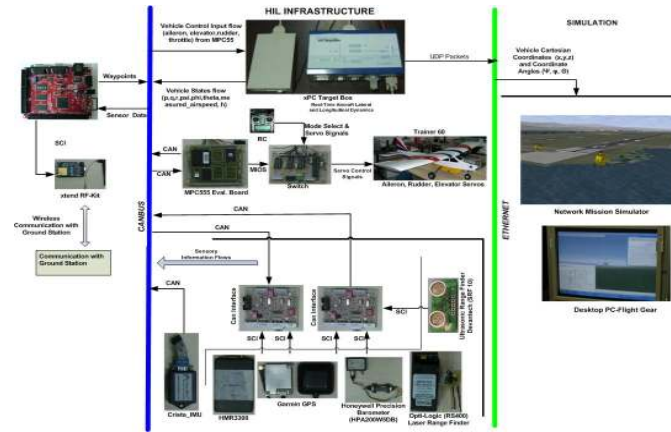


# CAL RESEARCH PROJECTS

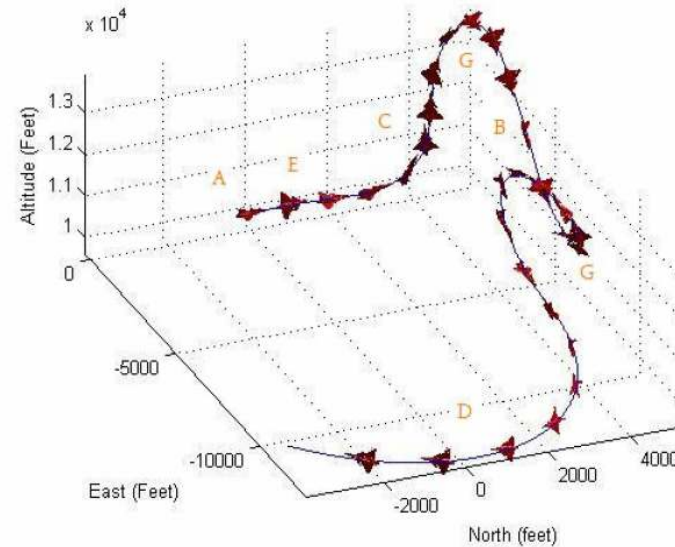
## 3D Real-time Motion Planning



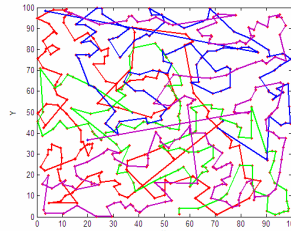
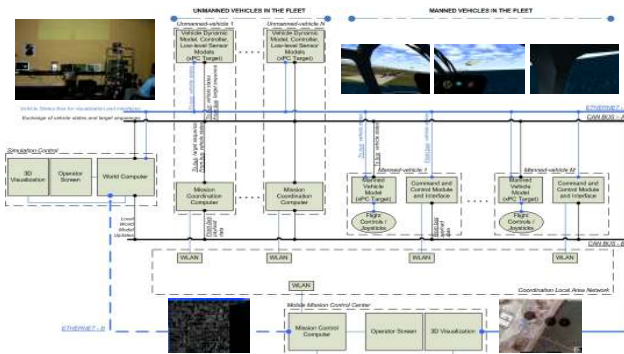
## Bus backboned Microavionics



## Agile Nonlinear Flight Controls



## Mission Planning for Manned and Unmanned Fleets





# CAL STUDENT PROJECTS

- Micro-avionics test platforms : Flight controls and image processing

## MicroBee



Autonomous control

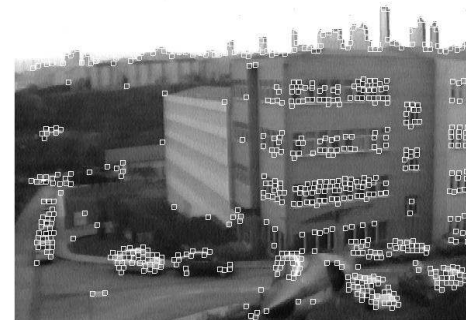
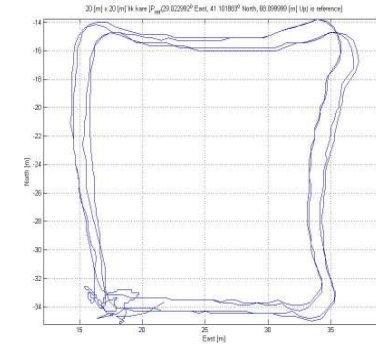
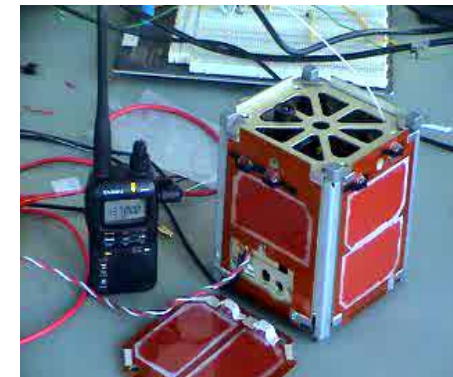
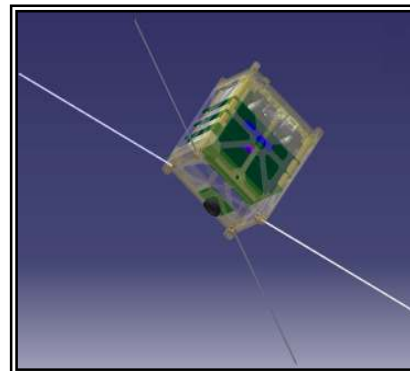


Image Processing

## ITU-pSAT I

- Scheduled for launch  
In late 2008- early 2009



ITU pSAT I Engineering Model



# Outline

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- Problem Statement and Previous Work
- F-16 Aircraft Model
- Motion Language for Agile Maneuvering
- Hybrid System Representation of Agile Maneuvers
- Properties and advantages of Hybrid System  
Description
- Nonlinear Sliding Control of full flight envelope  
Dynamics
- Simulations



# Problem Statement

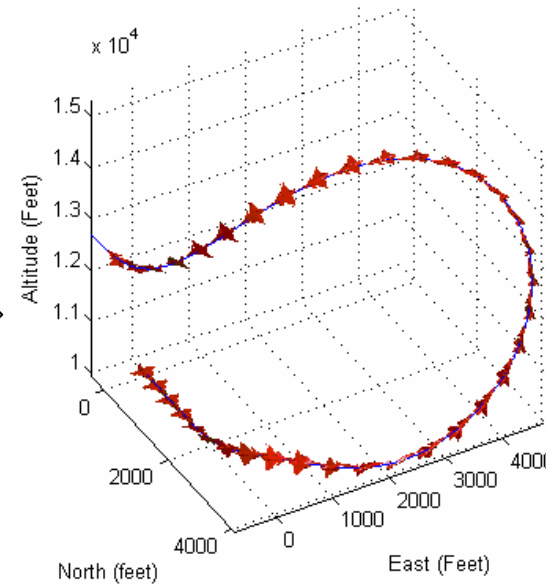
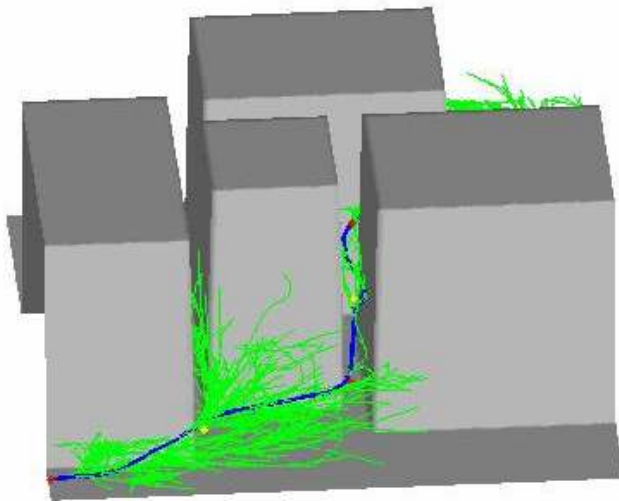
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- **Autonomous Control of Agile Maneuvers over full flight envelope**
  - Perform agile maneuvers in case of evasive and tactical advantage gain positions
  - Output tracking over full flight envelope, especially in extreme cases (high AOA , high g)
- Design flight trajectory generation algorithms over full flight envelope
  - Agile and competitive maneuvering in dynamically changing and complex environments

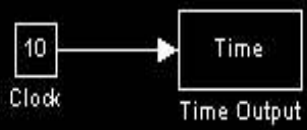


# Two Facets of the Problem

- Autonomous design and execution of agile maneuvers



- A low level enabling technology for cooperative control of UAV fleets that driven by performance goals



NONLINEAR F 16 SIMULATION

I.T.U - Faculty of Aeronautics And Astronautics

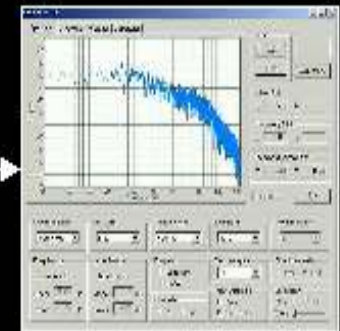
Control And Avionics Laboratory



Cockpit



F 16



Outputs

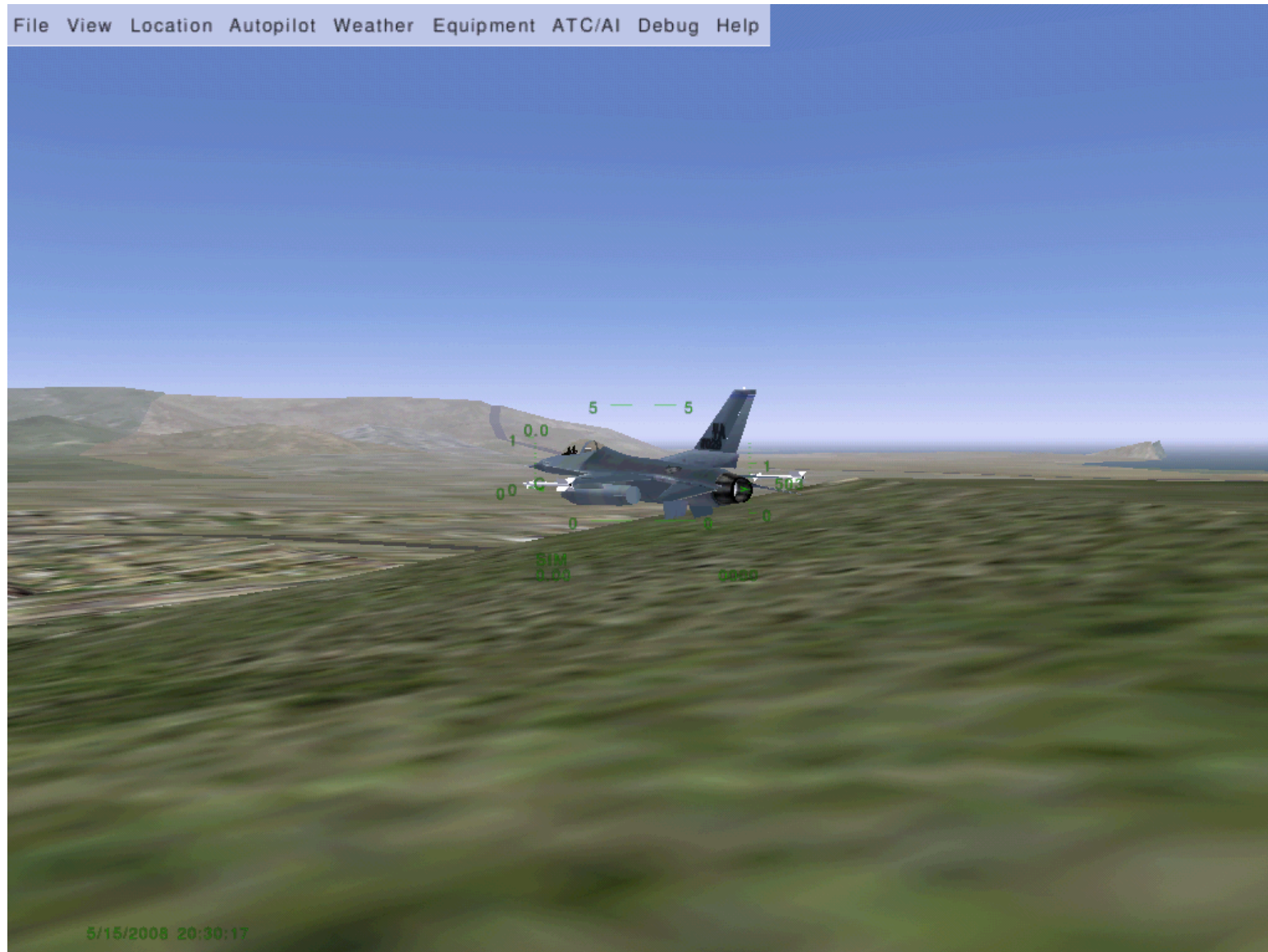


To Workspace





# Agile Maneuver Example





# Challenges

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- Generation of agile maneuvers
  - Lack of general expressions for six degrees of freedom flight dynamics
  - Complexity of decomposing the maneuvers in state space
  - Feasibility constraints on maneuvers
- Execution of agile maneuvers
  - Highly coupled, nonlinear dynamics
  - Demand for high precision tracking on high magnitude angular rates
  - Robustness properties



# Previous Works

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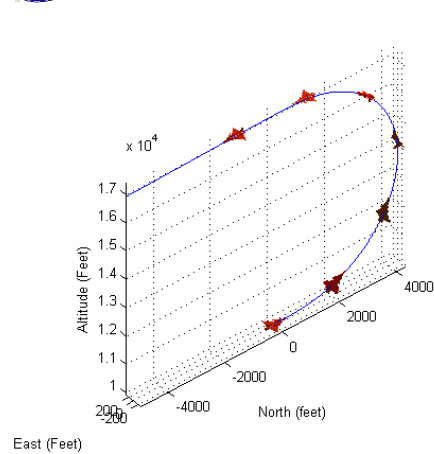
- Hybrid Systems Description for Flight Maneuvering
  - Hybrid and modal representation of single and multiple aircraft dynamics (Tomlin, 1998),(Frazzoli,2002)
- Experimental Work on Agile Maneuvering
  - Gavrilets, Feron (MIT) : outdoors
  - How (MIT) : indoors

Major issues that is still open...

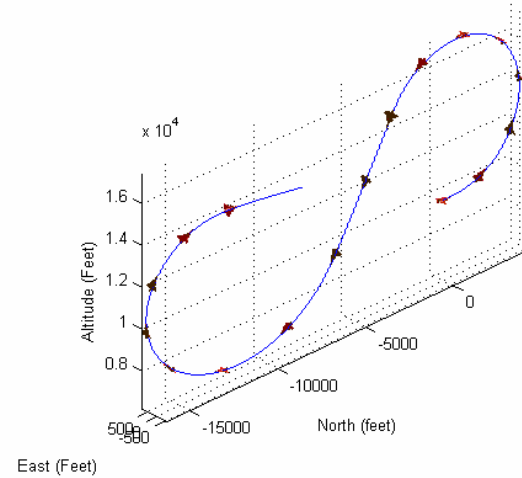
- Full flight envelope dynamics?
- Trajectory-free controller design?



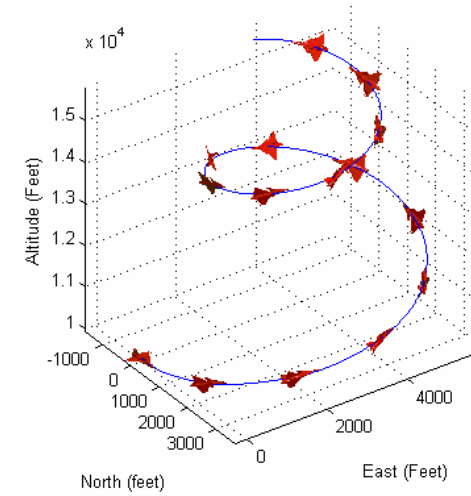
# Motion Description for Agile Flight



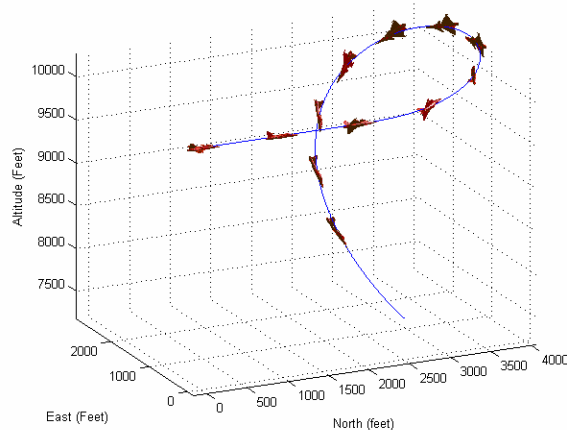
**Immelmann**



**Cuban Eight**



**Turning Climb**

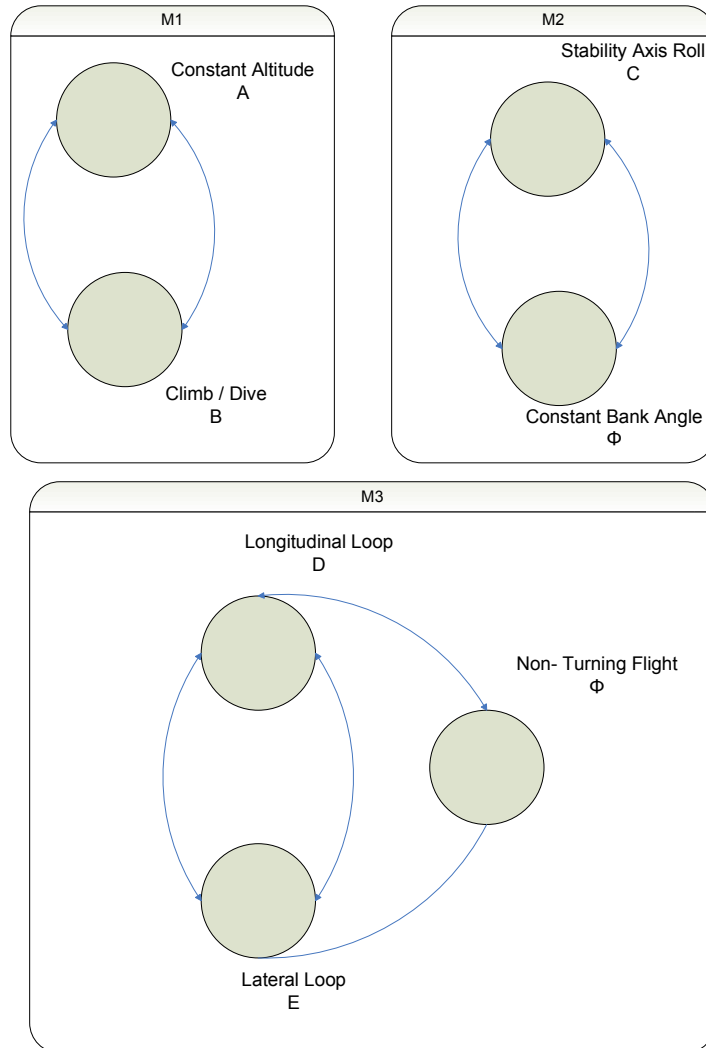


**High Yo-Yo**

**Acrobatic and combat maneuvers is a good starting point....**



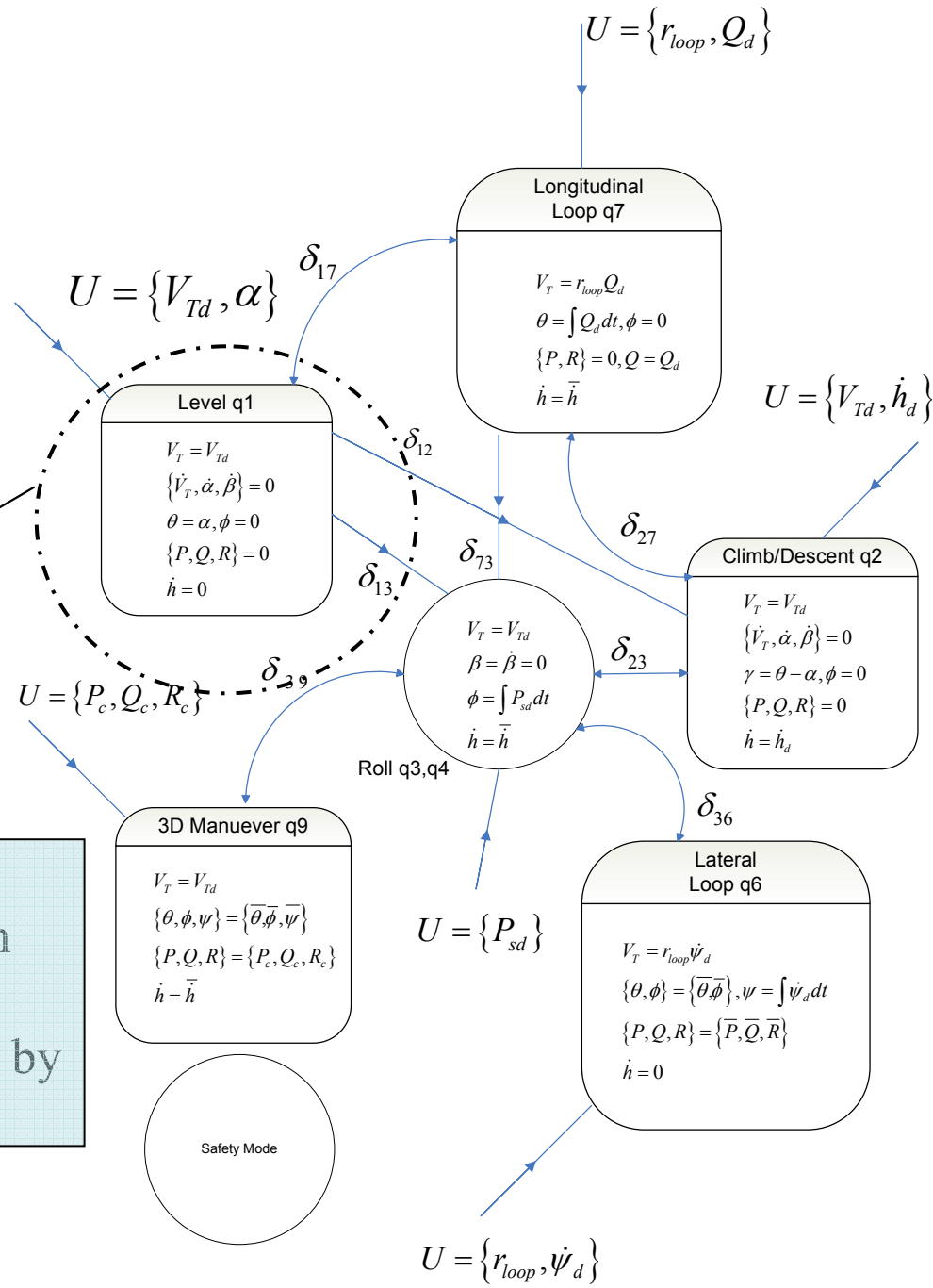
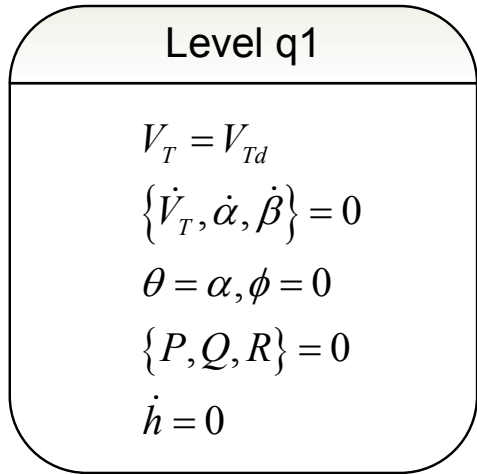
# Coordinated Automata Description



	M1	M2	M3	Description of Maneuver Segment
$q_1$	A	$\emptyset$	$\emptyset$	Level Flight
$q_2$	B	$\emptyset$	$\emptyset$	Climb/Descent
$q_3$	A	C	$\emptyset$	Straight Rolling Flight
$q_4$	B	C	$\emptyset$	C/D Rolling Flight
$q_5$	A	$\emptyset$	D	AOA Regulation in Level Flight
$q_6$	A	$\emptyset$	E	Coordinated Turn
$q_7$	B	$\emptyset$	D	Pitch Up/Down
$q_8$	B	$\emptyset$	E	Turning C/D
$q_9$	B	C	D(E)	Barrel Roll, Helix, 3D Maneuvers
$q_{10}$	A	C	E	Rolling Circle



# Maneuver Modes

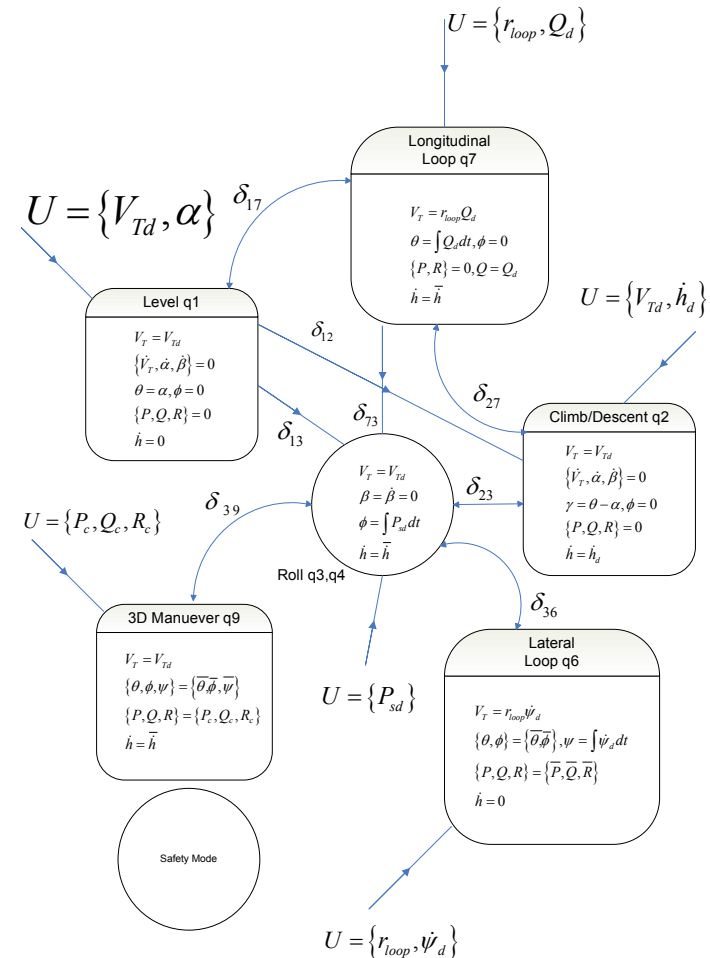
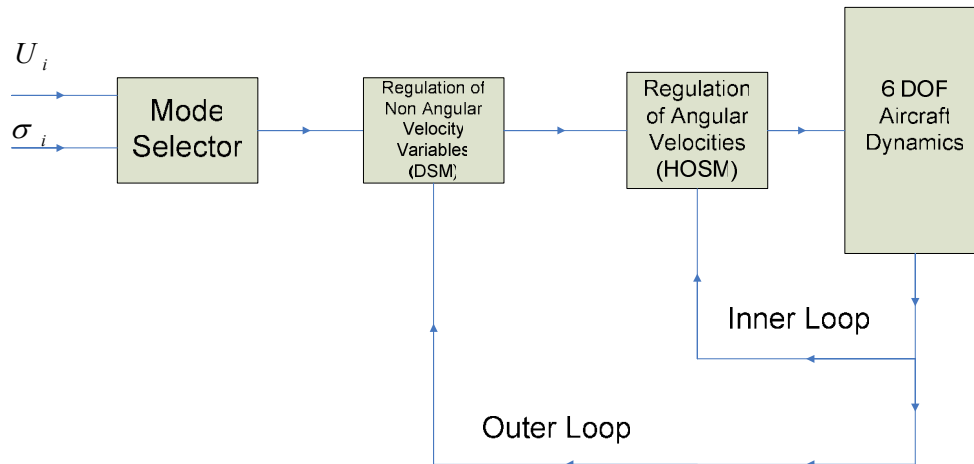


- Each maneuver mode represents a discrete state in finite automata
- Each mode is characterized by different state constraints



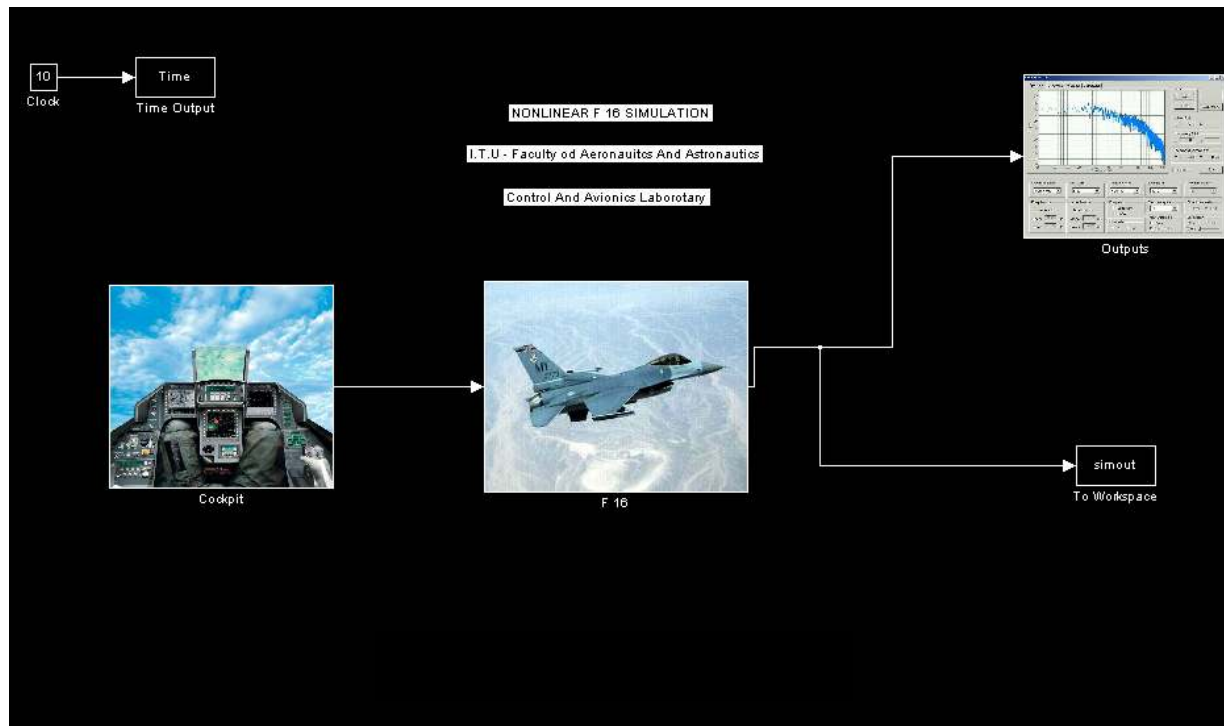
# Solution

- A structured finite automaton, spanning full flight envelope
- Nonlinear sliding manifold control system that tracks the outputs of the automaton





# Aircraft Model



- A Full Scale 6 DOF High Fidelity Dynamic Model
- Highly Coupled Nonlinear State Equations
- 52 Look-up Tables To Build-up Aerodynamic Forces and Moments through control surface deflections (Including Stall Effect)
- Actuator Models with rate limits and saturation
- Afterburning Turbofan Engine Model controlled via throttle

State Vector

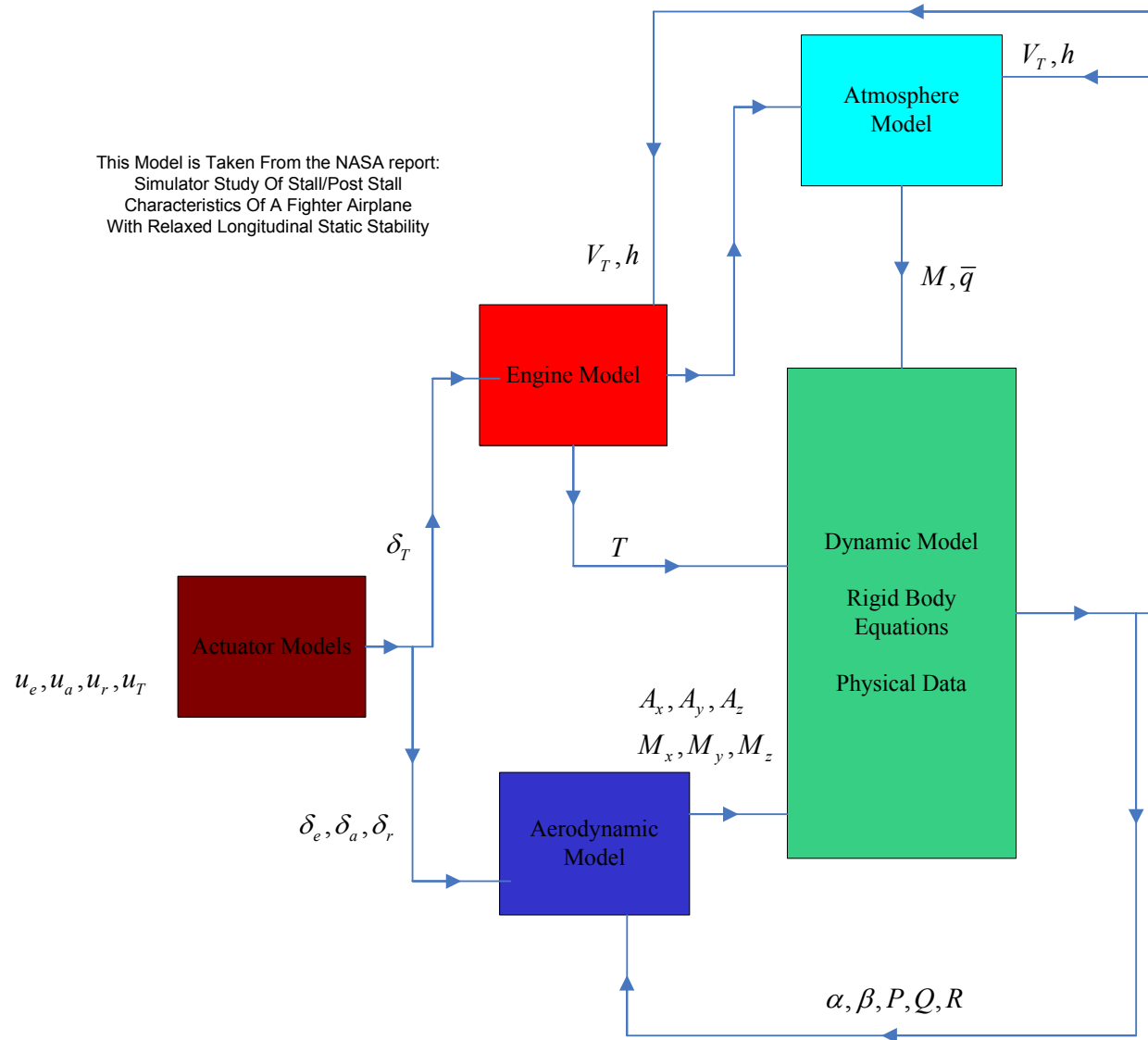
$$X = \left[ V_T \quad \alpha \quad \beta \quad \phi \quad \theta \quad \psi \quad P \quad Q \quad R \quad n_p \quad e_p \quad h \right]^T$$





# Aircraft Model Cont

This Model is Taken From the NASA report:  
Simulator Study Of Stall/Post Stall  
Characteristics Of A Fighter Airplane  
With Relaxed Longitudinal Static Stability





# Aircraft Model Cont

Aerodynamic Model

$$c_x(\alpha, \beta, \delta_h = 10^\circ)$$

BETA	-30.0	-25.0	-20.0	-15.0	-10.0	- 8.0	- 6.0	- 4.0	- 2.0	+30.0
ALPHA	0.0	+ 2.0	+ 4.0	+ 6.0	+ 8.0	+10.0	+15.0	+20.0	+25.0	
-20.0	-.10230	-.10120	-.10000	-.10470	-.10350	-.09910	-.09990	-.09100	-.08840	
-15.0	-.08840	-.09070	-.09000	-.09130	-.09180	-.09430	-.09450	-.09880	-.09200	-.09310
-10.0	-.10100	-.10070	-.10090	-.10040	-.10000	-.10060	-.10300	-.10650	-.10750	-.10460
- 5.0	-.06640	-.07150	-.07550	-.07800	-.08450	-.08730	-.08850	-.09660	-.08960	-.08980
0.0	-.04720	-.04980	-.05210	-.05330	-.05670	-.05780	-.05900	-.06950	-.06020	-.06400
+ 5.0	-.02000	-.02060	-.01950	-.01840	-.01690	-.01610	-.01510	-.01150	-.01340	-.01550
+10.0	.01820	.02420	.02810	.03130	.03260	.03310	.03220	.03270	.03200	.03200
+15.0	.03130	.03130	.03230	.03290	.03280	.03260	.03130	.02810	.02420	.01820
+20.0	.04710	.05240	.05070	.04900	.04810	.04750	.04740	.04690	.04600	.05370
+25.0	.06640	.07140	.07000	.06960	.06960	.06960	.06960	.06960	.06960	.06960
+30.0	.08840	.09330	.09200	.09100	.09000	.08900	.08840	.08810	.08770	.08770
+35.0	.10230	.10700	.10550	.10400	.10250	.10100	.09950	.09800	.09650	.09500
+40.0	.11770	.12240	.12100	.11950	.11800	.11650	.11500	.11350	.11200	.11050
+45.0	.13460	.13930	.13800	.13650	.13500	.13350	.13200	.13050	.12900	.12750
+50.0	.15300	.15770	.15650	.15500	.15350	.15200	.15050	.14900	.14750	.14600
+55.0	.17300	.17770	.17650	.17500	.17350	.17200	.17050	.16900	.16750	.16600
+60.0	.19460	.19930	.19800	.19650	.19500	.19350	.19200	.19050	.18900	.18750
+70.0	.25040	.25510	.25350	.25200	.25050	.24900	.24750	.24600	.24450	.24300
+80.0	.31190	.31660	.31500	.31350	.31200	.31050	.30900	.30750	.30600	.30450
+90.0	.38040	.38510	.38350	.38200	.38050	.37900	.37750	.37600	.37450	.37300

Actuator Models

	Deflection Limit (deg)	Rate Limit (deg/s)
Elevator	25	60
Ailerons	21.5	80
Rudder	30	120



# Aircraft Model Cont

Dynamic Model

Rigid Body  
Equations

Physical Data

$$\begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{z} \end{bmatrix} = \begin{bmatrix} c\theta^* c\psi & (-c\phi^* s\psi + s\phi^* s\theta^* c\psi) & (s\phi^* s\psi + c\phi^* s\theta^* c\psi) \\ c\theta^* s\psi & (c\phi^* c\psi + s\phi^* s\theta^* s\psi) & (-s\theta^* c\psi + c\phi^* s\theta^* s\psi) \\ -s\theta & s\phi^* s\theta & c\phi^* c\theta \end{bmatrix} \begin{bmatrix} U \\ V \\ W \end{bmatrix}$$

$$m \begin{Bmatrix} \dot{U} \\ \dot{V} \\ \dot{W} \end{Bmatrix} + \begin{bmatrix} 0 & -R & Q \\ R & 0 & -P \\ -Q & P & 0 \end{bmatrix} \begin{Bmatrix} U \\ V \\ W \end{Bmatrix} = mg \begin{bmatrix} -\sin\theta \\ \cos\theta \sin\phi \\ \cos\theta \cos\phi \end{bmatrix} + \begin{bmatrix} A_x \\ A_y \\ A_z \end{bmatrix}$$

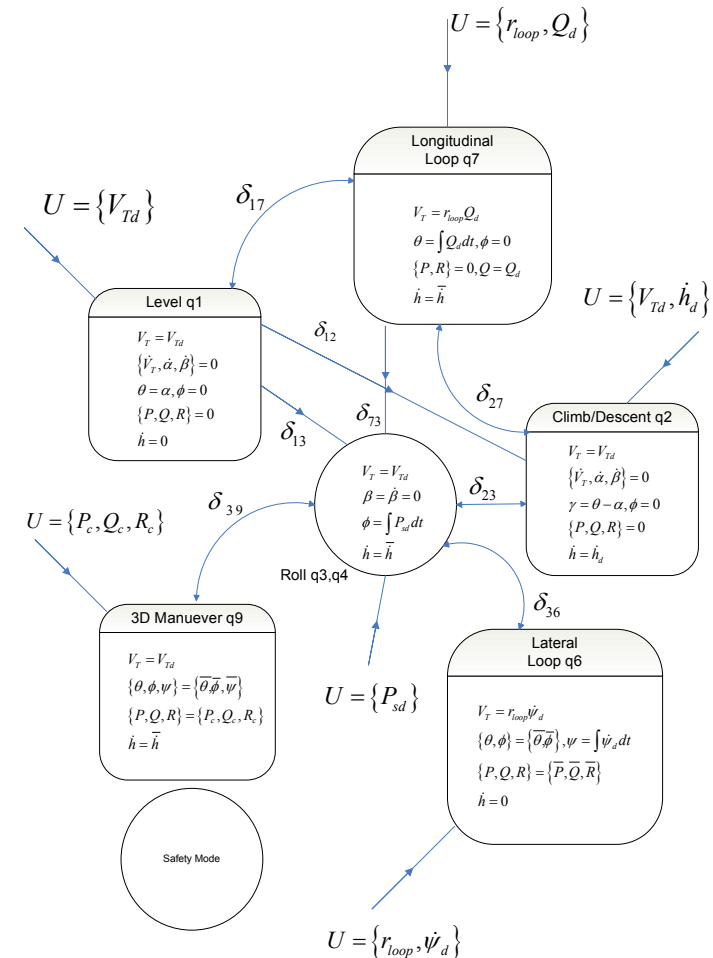
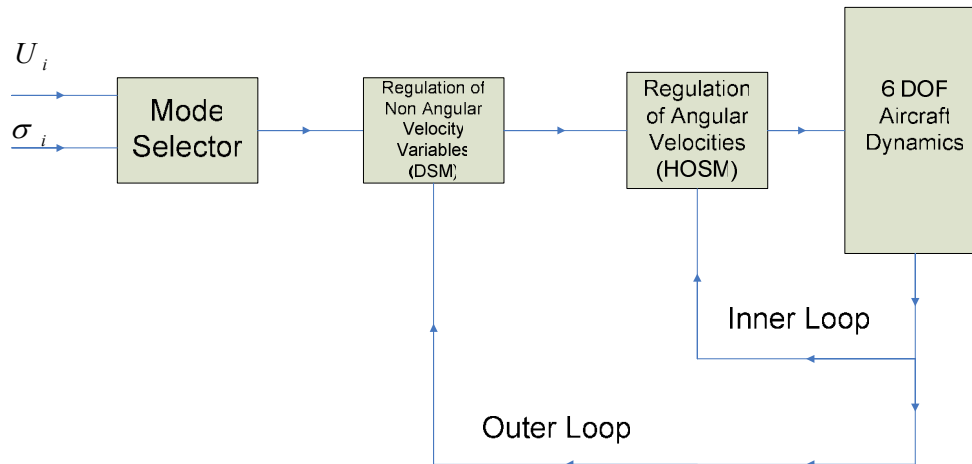
$$\begin{bmatrix} \dot{\psi} \\ \dot{\theta} \\ \dot{\phi} \end{bmatrix} = \begin{bmatrix} 0 & s\psi / c\theta & c\phi / c\theta \\ 0 & c\phi & -s\phi \\ 1 & s\phi^* t\theta & c\phi^* t\theta \end{bmatrix} \begin{bmatrix} P \\ Q \\ R \end{bmatrix}$$

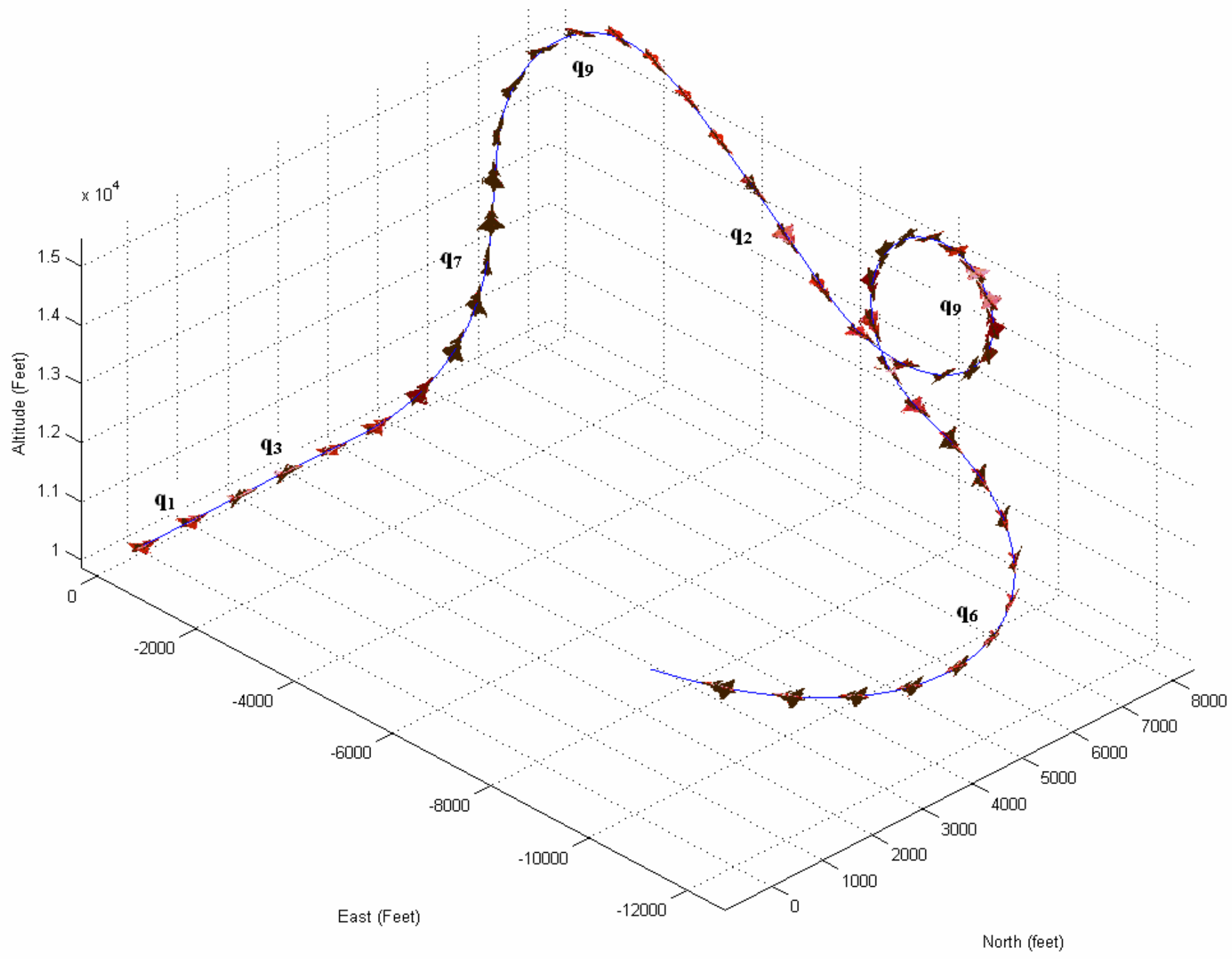
$$[I] \begin{bmatrix} \dot{P} \\ \dot{Q} \\ \dot{R} \end{bmatrix} + \begin{bmatrix} 0 & -R & Q \\ R & 0 & -P \\ -Q & P & 0 \end{bmatrix} \times [I] \begin{bmatrix} P \\ Q \\ R \end{bmatrix} = \begin{bmatrix} M_x \\ M_y \\ M_z \end{bmatrix}$$



# Solution

- A structured finite automaton, spanning full flight envelope
- Nonlinear sliding manifold control system that tracks the outputs of the automaton







# Hybrid System Description for Control Purposes

$$MBMA = \{Q, X, U, D, \Sigma, f, \delta, Dom, Init, \Omega\}$$

Set of Discrete States = Modes:

$$Q = \{q_0, q_1, q_2, q_3, q_4, q_5, q_6\} = \{\text{Level, Climb, Roll, Long. Loop, Lat. Loop, 3D, Safety}\}$$

Set of Continuous States = Flight dynamics

$$X = [V_T \quad \alpha \quad \beta \quad \phi \quad \theta \quad \psi \quad P \quad Q \quad R \quad n_p \quad e_p \quad h]^T$$

Set of Continuous Inputs = Parameters that generate modal Inputs (state values that create modes)

$$U = \left\{ V_T, \dot{h}, \int P_w dt, r_{loop}, \dot{\theta}, \dot{\psi}, P, Q, R, \phi_w, \theta_w, \psi_w \right\}$$

Continuous Map = The state propagation in hybrid system form

$$\dot{X} = f(X, U, Q)$$

Set of Discrete Inputs = Switching decisions between modes

$$\Sigma = \bigcup_{i=1, j=1}^{i=1, j=7} \sigma_{ij}$$

Discrete Transition Functions = Transition conditions between flight modes

$$\delta = \bigcup_{i=1, j=1}^{i=1, j=7} \delta_{ij} \quad q_j = \delta_{ij} (q_i, \sigma_{ij})$$

Disturbances = Inputs From Environment (Wind Gusts, Sensor Noises ...etc)

$D$



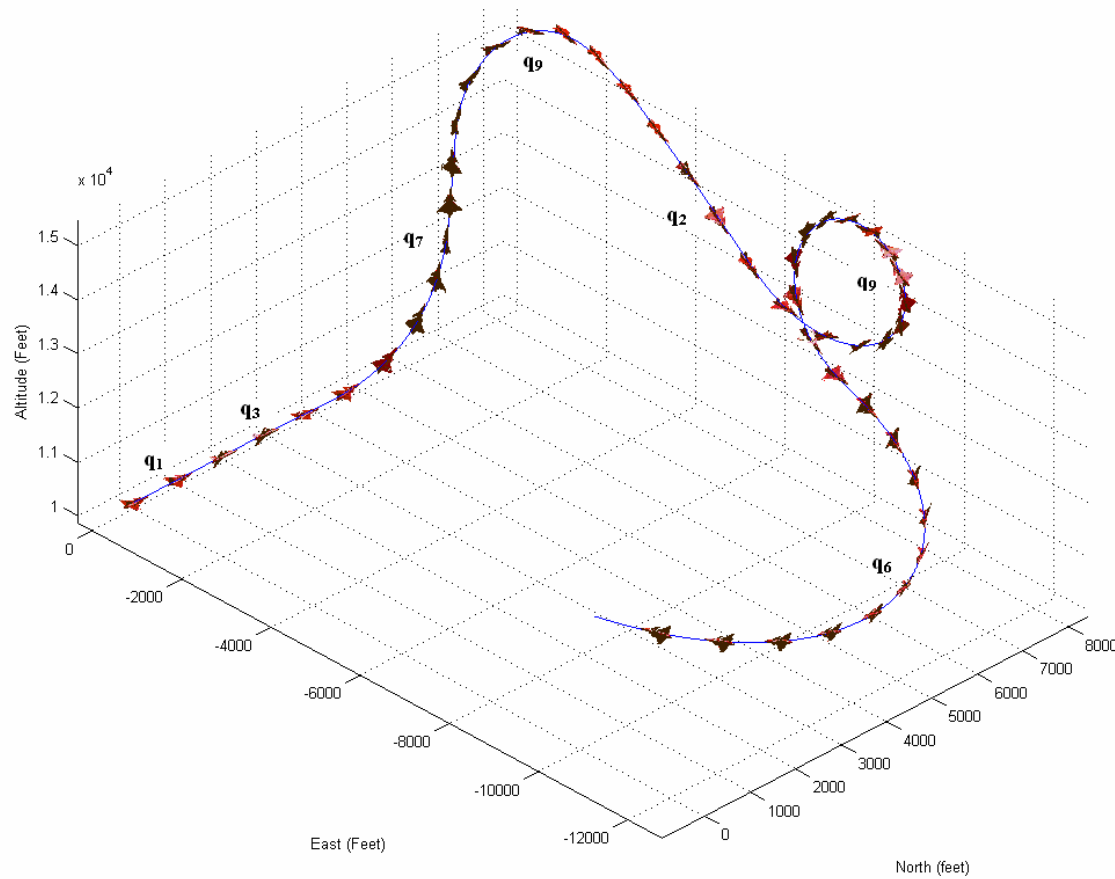
# Maneuver Identification

Mode Sequence = Maneuver Sequence

$$s = \sigma(1)\sigma(2)\sigma(3)\dots\sigma(n) \in \Sigma$$

Modal Inputs = Maneuver Parameters

$$r = u(1)u(2)u(3)\dots u(n) \in U$$





# Language

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- Discrete Input Strings  
(Mode switching sequence)

$$s = \sigma(1)\sigma(2)\sigma(3)\dots\sigma(n) \in \Sigma$$

- Continuous Input Strings (Maneuver Parameters)

$$r = u(1)u(2)u(3)\dots u(n) \in U$$

- Trajectory Acceptance Condition

$$\Omega = (q_1 \in \text{Init}) \wedge (q_{i+1} = \delta_{i,i+1}(q_i, \sigma_{i,i+1})) \wedge (q_i, x_i \in \text{Dom})$$

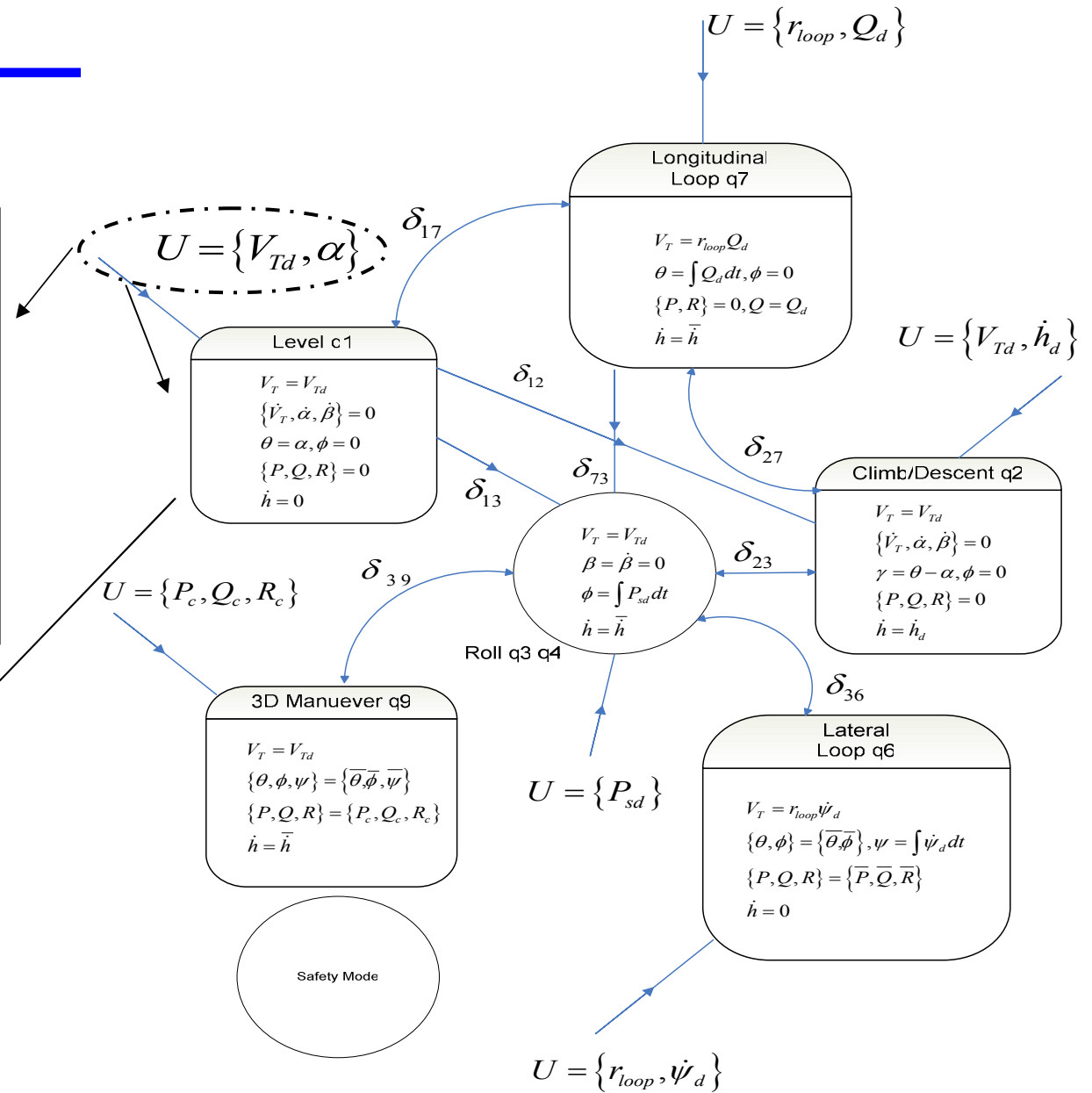
*This is the starting point for trajectory/maneuver planning algorithms...*





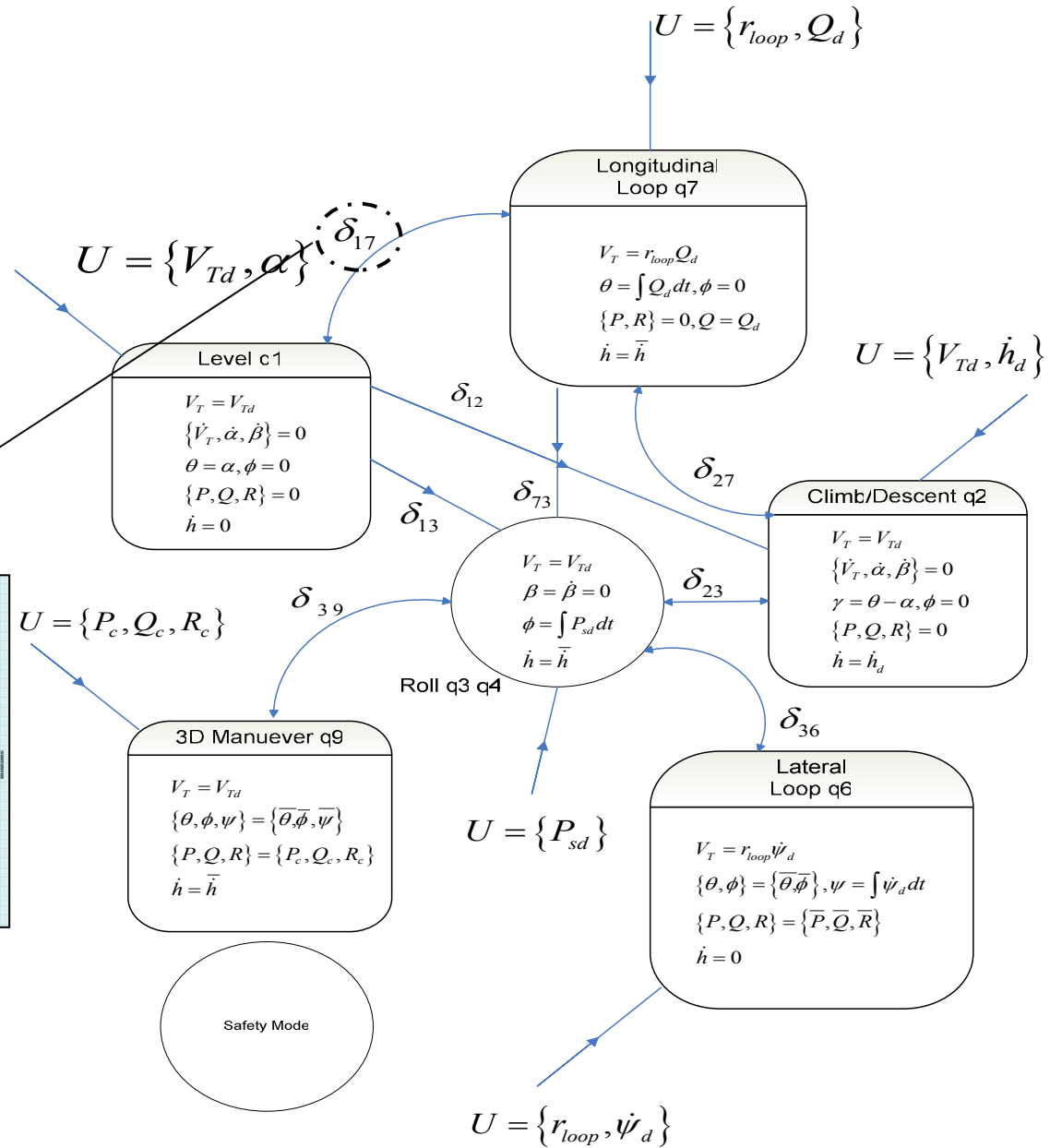
Modal input = Maneuver parameters sets the values of the constrained parameters to define the maneuver (such as velocity in level flight, radius of the loop in turning flight)

Simplified dynamics





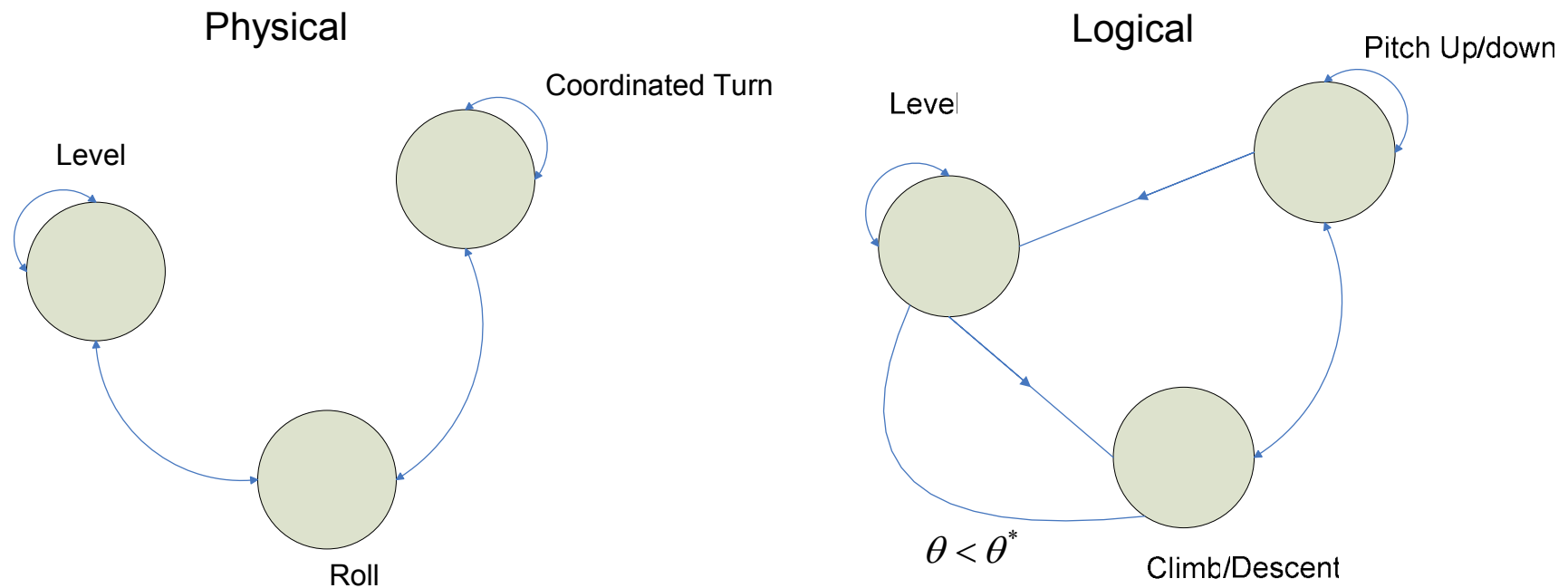
Mode transition functions, set switching conditions between modes. They limit the transitions between two specific modes from both physical and logical constraints (More on this topic in next slide)





# Examples of Sequential Constraints

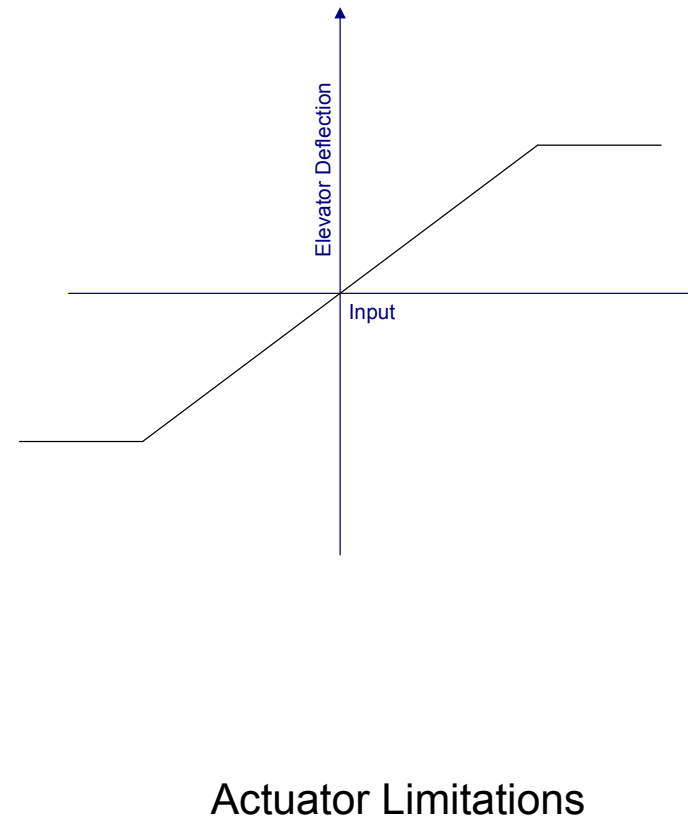
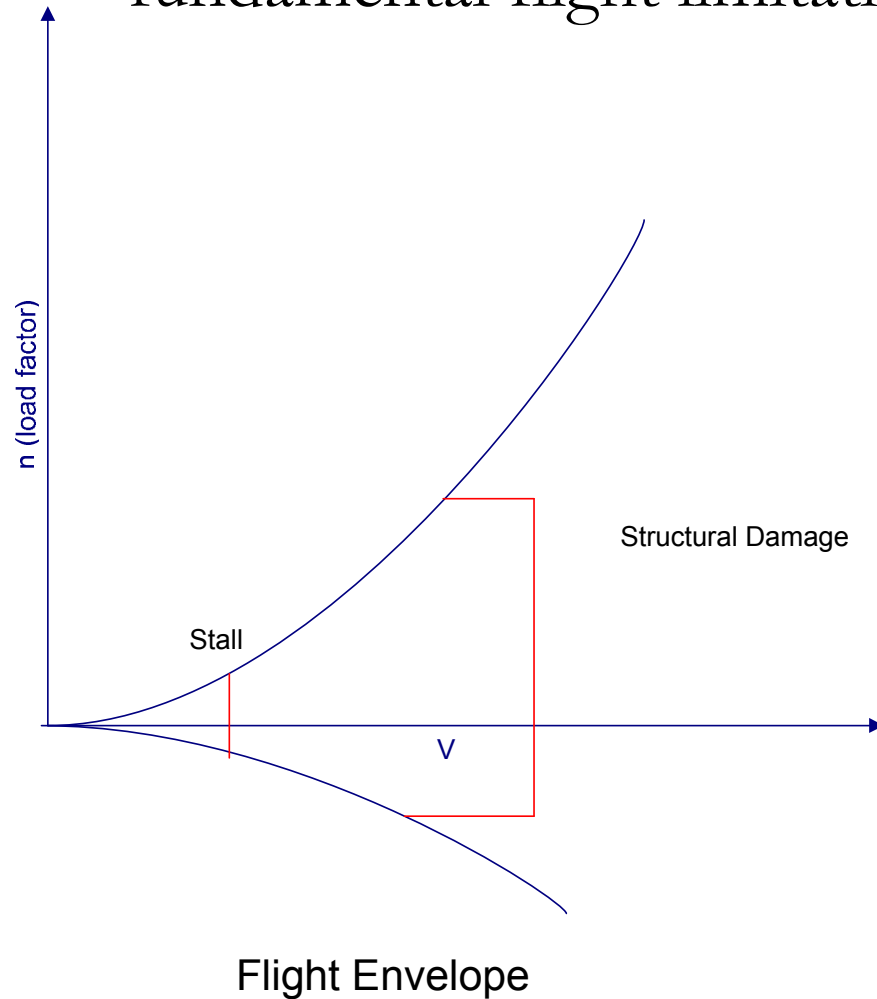
- Sequences of maneuver modes are not necessarily arbitrary and there can be limitations on when the switch is feasible.





## Flight Limitations Also Drive the Mode Transition Table

- Modal Inputs and their transitions must be in line with fundamental flight limitations





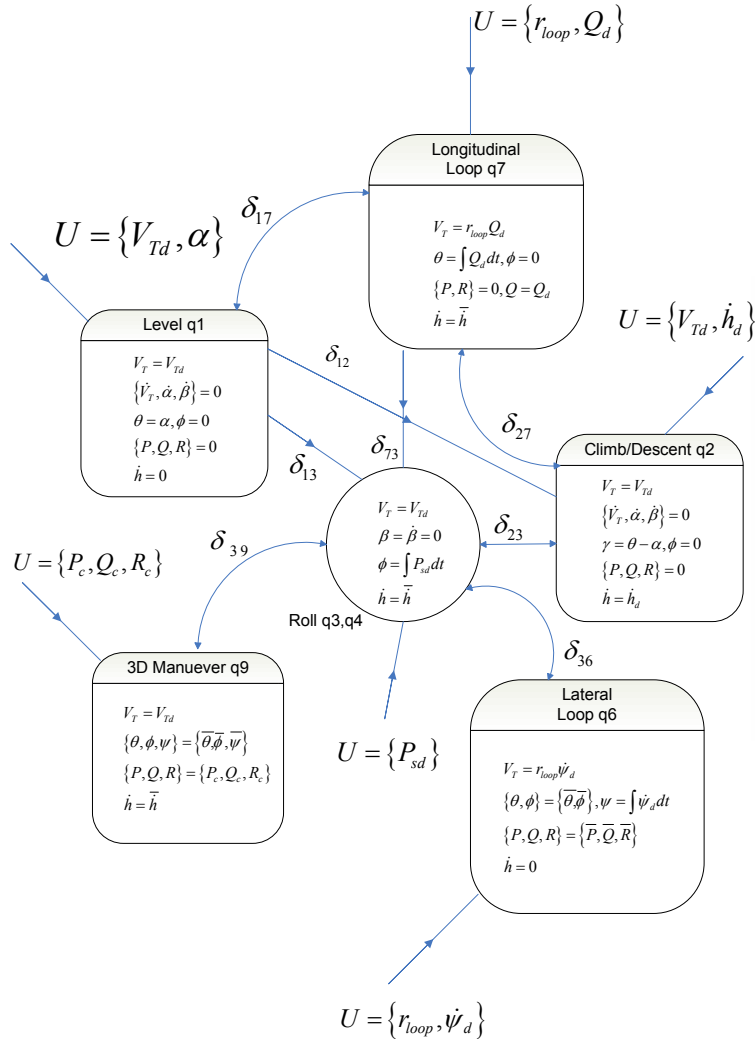
# Mode Transition Table!!!

- Either pitch angle or roll angle (sometimes both) must be regulated to a specific value, to translate between certain modes

$\delta_{ij}$	$q_1$	$q_2$	$q_3$	$q_4$	$q_5$	$q_6$	$q_7$	$q_8$	$q_9$	$q_{10}$
$q_1$	1	1	1	1	$\theta^*$	$\phi^*$	1	$\phi^*$	$\phi^*$	$\phi^*$
$q_2$	$\theta^*$	1	$\theta^*$	1	$\theta^*$	$\theta^*, \phi^*$	1	$\phi^*$	$\phi^*$	$\theta^*, \phi^*$
$q_3$	1	1	1	$\theta^*$	1	1	1	1	1	1
$q_4$	$\theta^*, \phi^*$	$\phi^*$	$\theta^*, \phi^*$	1	$\theta^*, \phi^*$	$\theta^*$	$\phi^*$	1	1	$\theta^*$
$q_5$	1	1	1	1	1	$\phi^*$	1	$\phi^*$	$\phi^*$	$\phi^*$
$q_6$	$\phi^*$	$\theta^*, \phi^*$	$\phi^*$	$\theta^*, \phi^*$	$\phi^*$	1	$\phi^*$	1	1	1
$q_7$	$\theta^*, \phi^*$	1	$\theta^*, \phi^*$	$\phi^*$	$\theta^*$	$\theta^*, \phi^*$	1	$\phi^*$	$\phi^*$	$\phi^*$
$q_8$	$\theta^*, \phi^*$	$\phi^*$	$\theta^*, \phi^*$	$\phi^*$	$\theta^*, \phi^*$	$\theta^*$	1	1	1	$\theta^*$
$q_9$	$\theta^*, \phi^*$	$\phi^*$	$\theta^*, \phi^*$	$\phi^*$	$\theta^*, \phi^*$	$\theta^*$	1	1	1	$\theta^*$
$q_{10}$	$\theta^*, \phi^*$	$\phi^*$	$\phi^*$	$\phi^*$	$\theta^*, \phi^*$	1	$\phi^*$	1	1	1



# Hybrid System

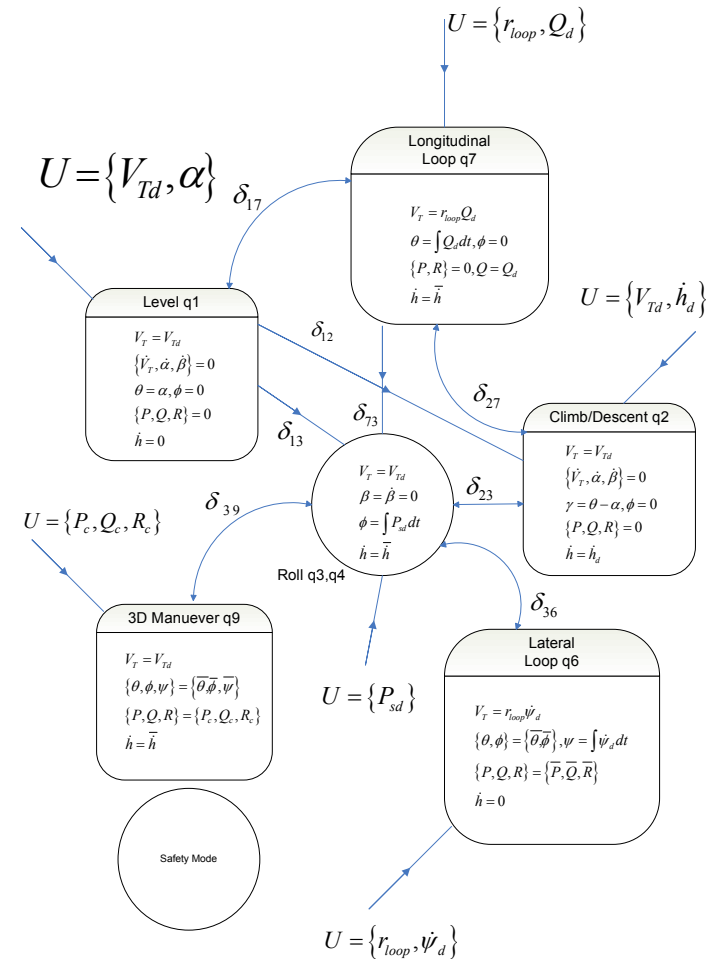
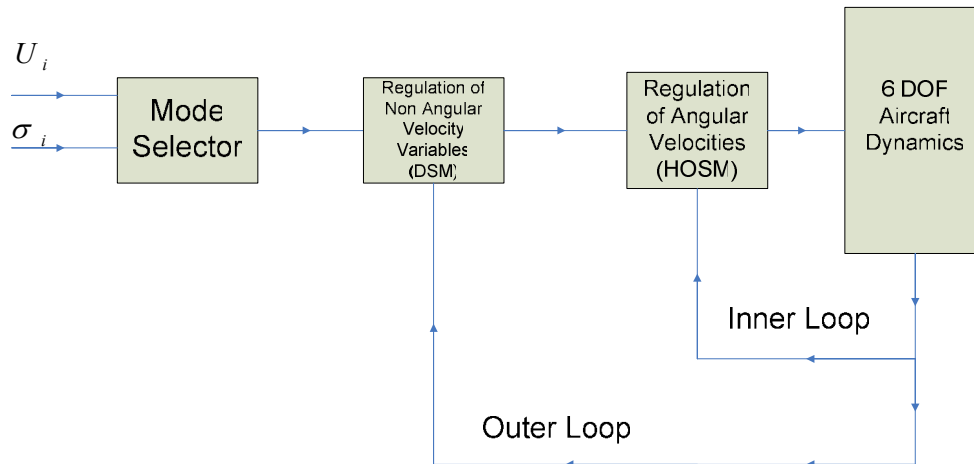


$\delta_{ij}$	$q_1$	$q_2$	$q_3$	$q_4$	$q_5$	$q_6$	$q_7$	$q_8$	$q_9$	$q_{10}$
$q_1$	1	1	1	1	$\theta^*$	$\phi^*$	1	$\phi^*$	$\phi^*$	$\phi^*$
$q_2$	$\theta^*$	1	$\theta^*$	1	$\theta^*$	$\theta^*, \phi^*$	1	$\phi^*$	$\phi^*$	$\theta^*, \phi^*$
$q_3$	1	1	1	$\theta^*$	1	1	1	1	1	1
$q_4$	$\theta^*, \phi^*$	$\phi^*$	$\theta^*, \phi^*$	1	$\theta^*, \phi^*$	$\theta^*$	$\phi^*$	1	1	$\theta^*$
$q_5$	1	1	1	1	1	$\phi^*$	1	$\phi^*$	$\phi^*$	$\phi^*$
$q_6$	$\phi^*$	$\theta^*, \phi^*$	$\phi^*$	$\theta^*, \phi^*$	$\phi^*$	1	$\phi^*$	1	1	1
$q_7$	$\theta^*, \phi^*$	1	$\theta^*, \phi^*$	$\phi^*$	$\theta^*$	$\theta^*, \phi^*$	1	$\phi^*$	$\phi^*$	$\phi^*$
$q_8$	$\theta^*, \phi^*$	$\phi^*$	$\theta^*, \phi^*$	$\phi^*$	$\theta^*, \phi^*$	$\theta^*$	1	1	1	$\theta^*$
$q_9$	$\theta^*, \phi^*$	$\phi^*$	$\theta^*, \phi^*$	$\phi^*$	$\theta^*, \phi^*$	$\theta^*$	1	1	1	$\theta^*$
$q_{10}$	$\theta^*, \phi^*$	$\phi^*$	$\phi^*$	$\phi^*$	$\theta^*, \phi^*$	1	$\phi^*$	1	1	1



# Solution

- A structured finite automaton, spanning full flight envelope
- Nonlinear sliding manifold control system that tracks the outputs of the automaton





# Hybrid Control Plan

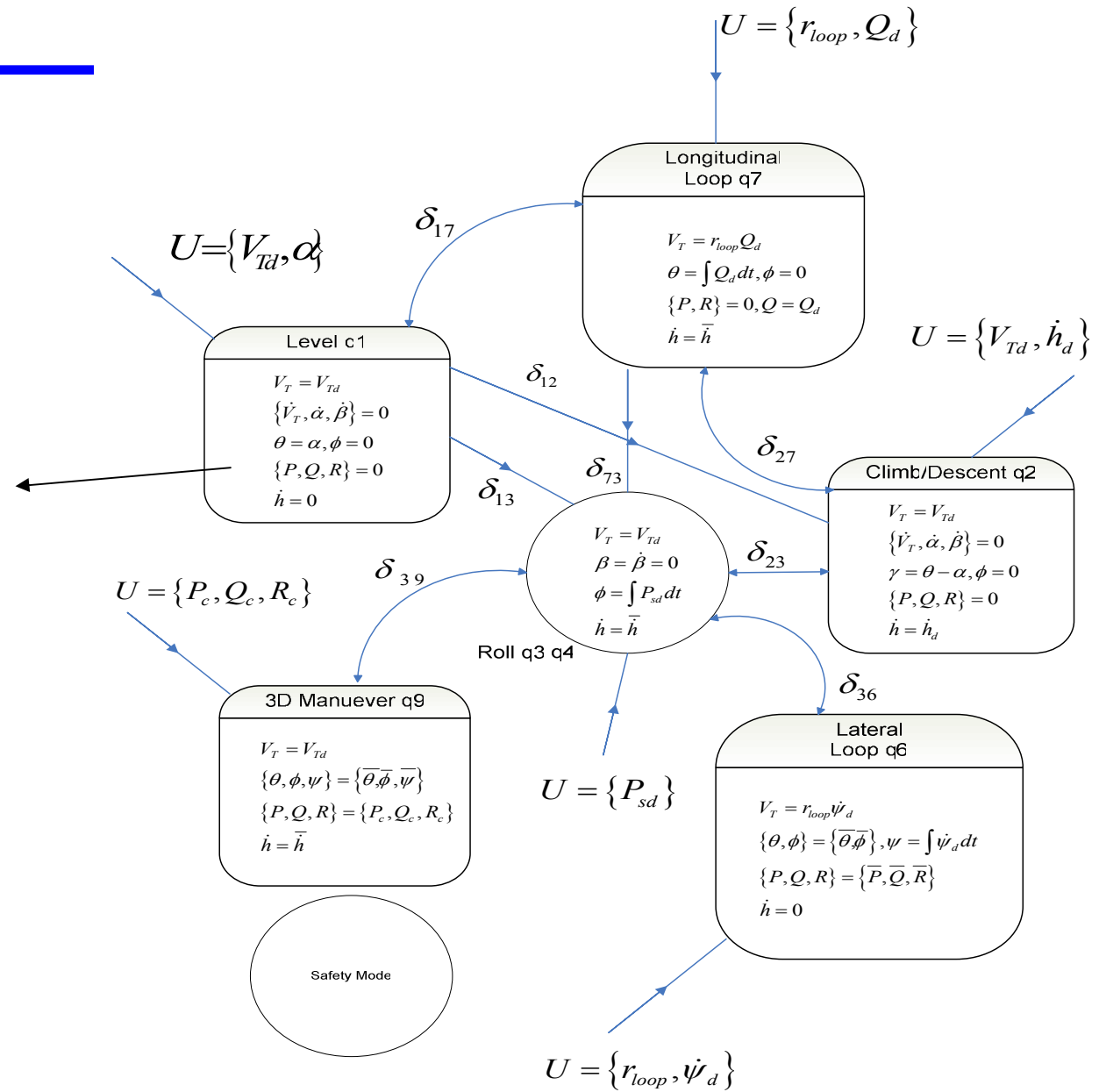
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- Switching sequence for the modes are already given by motion plan
  - Aim is to track each mode's modal input
- We can define different output variables for each maneuver mode
  - Dynamics are different (simplified ?) for each mode, so even different control strategies can be developed for each mode
- Linear tracking techniques are not adequate! We will rely on nonlinear control techniques of feedback linearization and sliding mode control (robustness?)





Simplified dynamics specific to each mode simplifies the control design procedure (However this is not the Case in 3D maneuver mode)





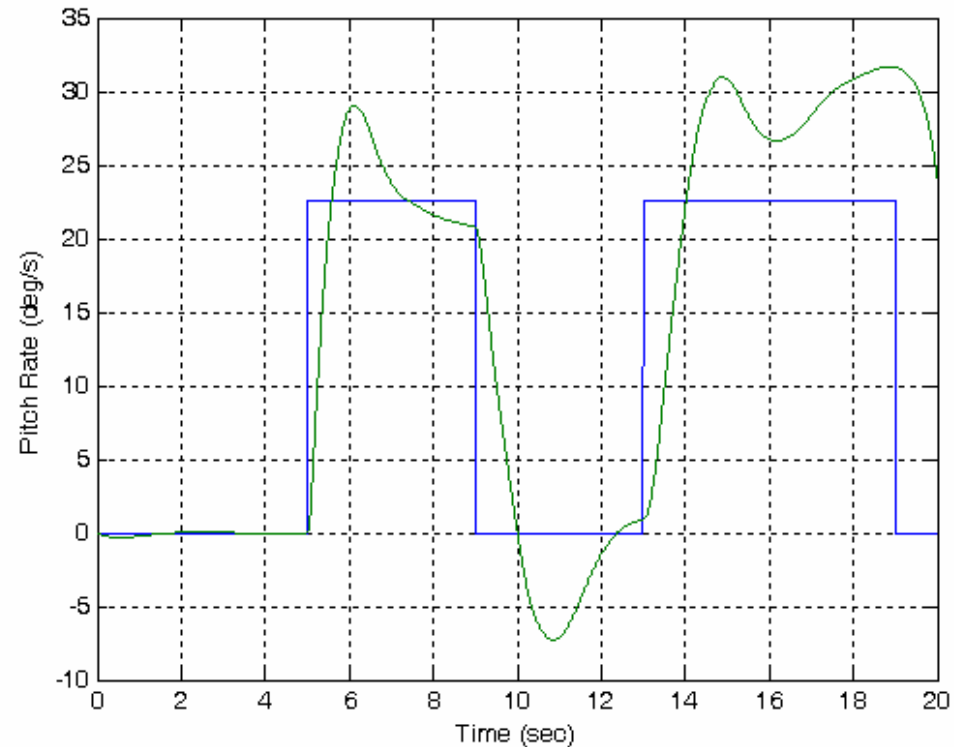
# Linear Control ?

- Performance of a robust linear controller designed with parameter space methods

Aggressiveness is defined by:

- a. Amplitude of modal inputs
- b. Frequency of switching

Performance of the Linear controllers is limited by both “a” and “b” as seen in the example (Actuator Saturation was not taken into account in this example)



*Linear control is not suitable for tracking of “non-trimmed” aggressive maneuvers*



# Aircraft Model for Control Purposes

Dynamic Model

Rigid Body  
Equations

Physical Data

$$\begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{z} \end{bmatrix} = \begin{bmatrix} c\theta^* c\psi & (-c\phi^* s\psi + s\phi^* s\theta^* c\psi) & (s\phi^* s\psi + c\phi^* s\theta^* c\psi) \\ c\theta^* s\psi & (c\phi^* c\psi + s\phi^* s\theta^* s\psi) & (-s\theta^* c\psi + c\phi^* s\theta^* s\psi) \\ -s\theta & s\phi^* s\theta & c\phi^* c\theta \end{bmatrix} \begin{bmatrix} U \\ V \\ W \end{bmatrix}$$

$$m \left\{ \begin{bmatrix} \dot{U} \\ \dot{V} \\ \dot{W} \end{bmatrix} + \begin{bmatrix} 0 & -R & Q \\ R & 0 & -P \\ -Q & P & 0 \end{bmatrix} \right\} = mg \begin{bmatrix} -\sin\theta \\ \cos\theta \sin\phi \\ \cos\theta \cos\phi \end{bmatrix} + \begin{bmatrix} A_x \\ A_y \\ A_z \end{bmatrix}$$

$$\begin{bmatrix} \dot{\psi} \\ \dot{\theta} \\ \dot{\phi} \end{bmatrix} = \begin{bmatrix} 0 & s\psi / c\theta & c\phi / c\theta \\ 0 & c\phi & -s\phi \\ 1 & s\phi^* t\theta & c\phi^* t\theta \end{bmatrix} \begin{bmatrix} P \\ Q \\ R \end{bmatrix}$$

Aerodynamic data is usually provided  
in the tabular form so:

$$\dot{X} = f(X, U)$$

$$[I] \begin{bmatrix} \dot{P} \\ \dot{Q} \\ \dot{R} \end{bmatrix} + \begin{bmatrix} 0 & -R & Q \\ R & 0 & -P \\ -Q & P & 0 \end{bmatrix} \times [I] \begin{bmatrix} P \\ Q \\ R \end{bmatrix} = \begin{bmatrix} M_x \\ M_y \\ M_z \end{bmatrix}$$

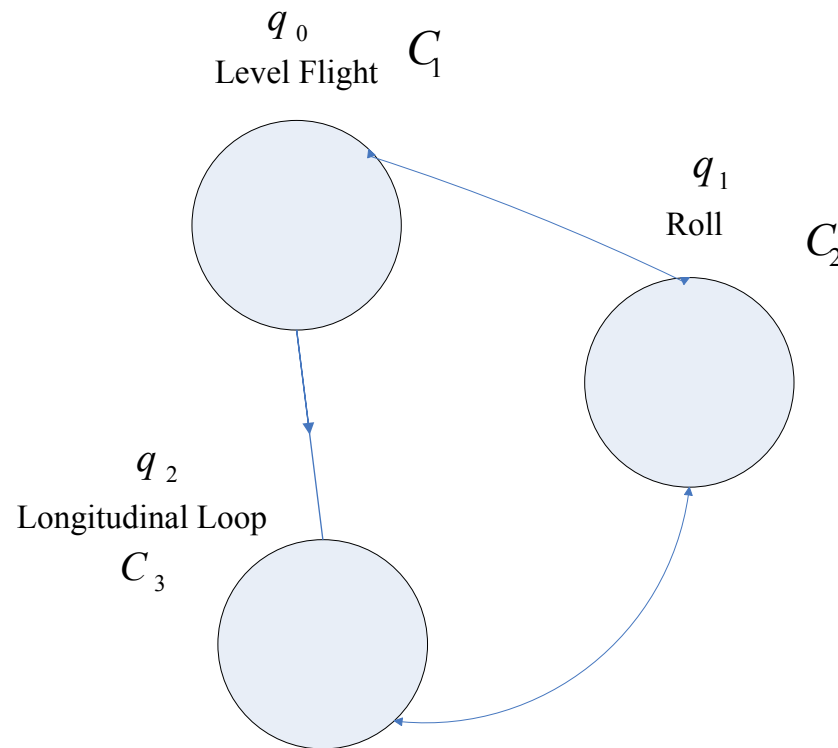
**Approximating tables by polynomial functions of (AOA, sideslip and angular rates) and linear multipliers for true inputs (elevator, aileron rudder and thrust)**

$$\dot{X} = f(X) + g(X)u$$



# Example Hybrid Control Plan

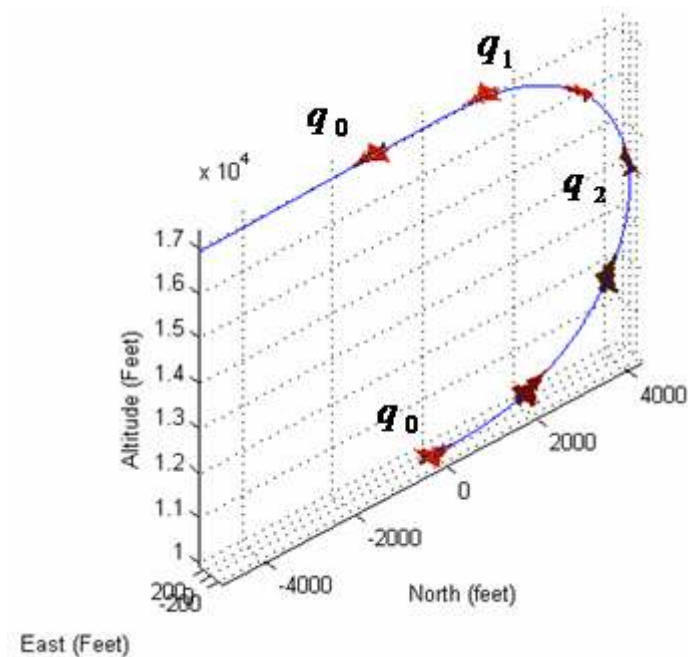
C: Controller



$$C_1 : \{V_T, x, y, z\} \text{ NMP}$$

$$C_2 : \{V_T, P, Q, R\} \text{ MP}$$

$$C_3 : \{V_T, \phi, \theta, \phi\} \text{ MP}$$





# Complete Low Level Controller Set

	Mode	State Constraints	Modal Inputs	Controller
$q_0$	Level Flight	$\dot{h} = 0, (\dot{\phi}, \dot{\theta}, \dot{\psi}) = 0$	$V_T, \alpha$	$C_2$
$q_1$	Climb/Descent	$(\dot{\phi}, \dot{\theta}, \dot{\psi}) = 0$	$V_T, (\dot{h}, \theta_w)$	$C_2$
$q_2$	Roll	$(\dot{\theta}, \dot{\psi}) = 0$	$\int P_w dt$	$C_1$
$q_3$	Longitudinal Loop	$(\dot{\phi}, \dot{\psi}) = 0$	$r_{loop}, \dot{\theta}$	$C_1, C_3$
$q_4$	Lateral Loop	$\dot{h} = 0, (\dot{\phi}, \dot{\theta}) = 0$	$r_{loop}, \dot{\psi}$	$C_2$
$q_5$	3D Mode	{ }	$V_T, P, Q, R$ $V_T, \phi_w, \theta_w, \psi_w$	$C_1, C_3, C_4$
$q_6$	Safety	{ }	{0, 1}	$C_5$

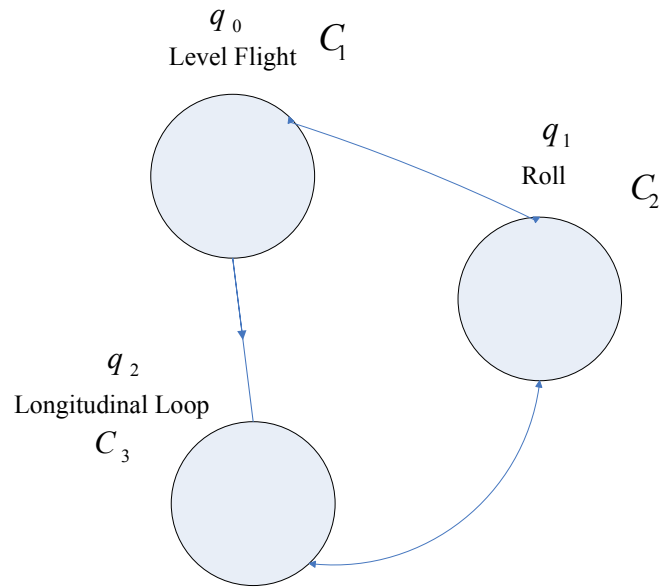
	Controlled Variables	Type
$C_1$	$V_T, P, Q, R$	MP
$C_2$	$V_T, \phi_w, \theta_w, \psi_w$	NMP
$C_3$	$V_T, \phi, \theta, \psi$	MP
$C_4$	$V_T, x, y, z$	NMP
$C_5$	$V_T, \{Quaternions\}$	MP

Subscript  $w$   
Refers to “wind axes”,  
this controller regulates the  
3D orientation of the  
velocity vector



# Two Problems with SMC

C: Controller



$$C_1 : \{V_T, x, y, z\} \text{ NMP}$$

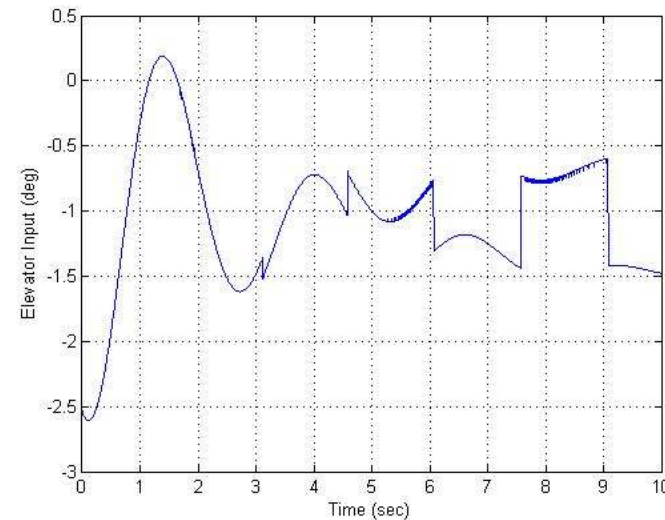
$$C_2 : \{V_T, P, Q, R\} \text{ MP}$$

$$C_3 : \{V_T, \phi, \theta, \psi\} \text{ MP}$$

1. Avoid NMP outputs !! In these sets position variables are controlled, which results in unstable attitude dynamics.

But altitude rate is a modal input, Therefore we must seek a way to stabilize internal dynamics for NMP outputs

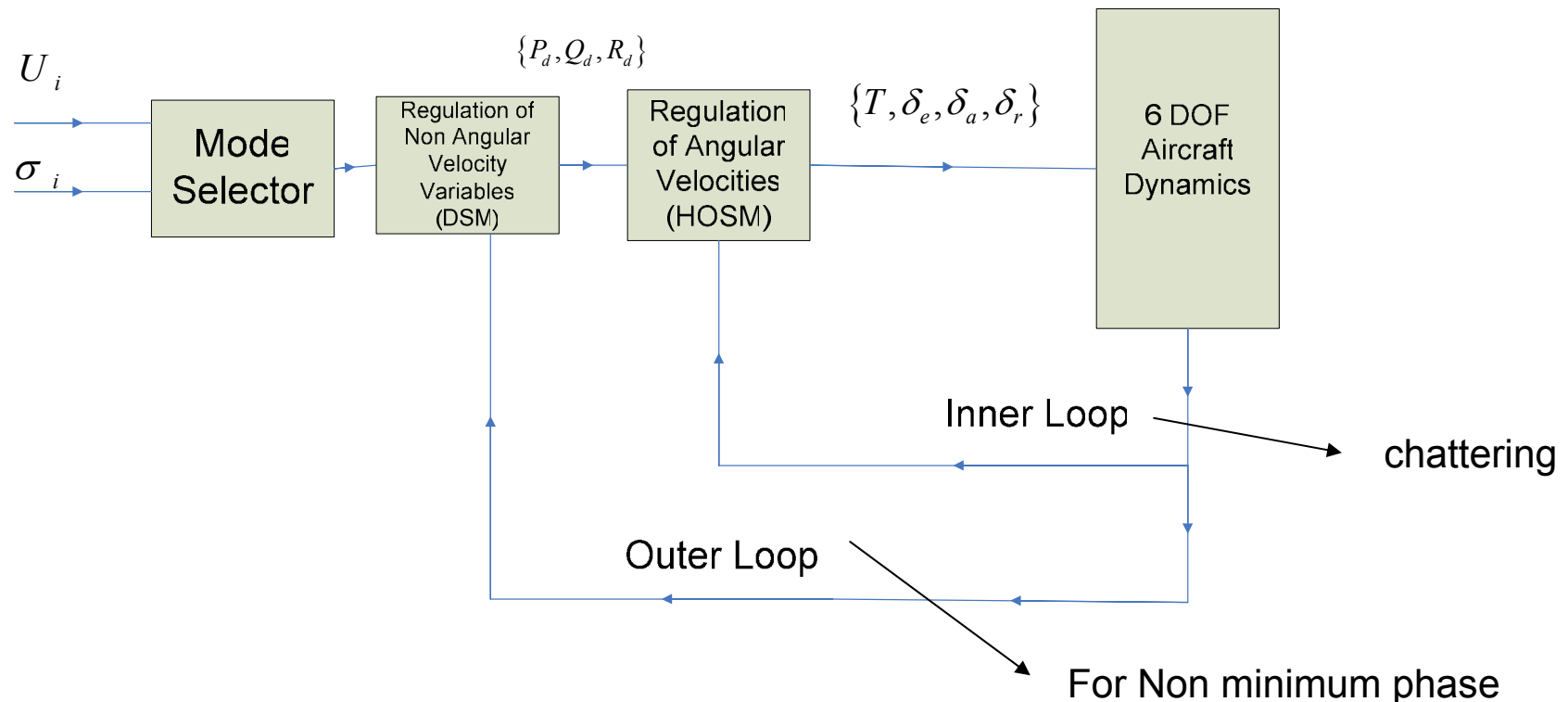
2. Discontinuous terms in control law results in chattering, which can be deadly for actuators





# Control Architecture

- To separate NMP tracking from the input chattering problem faced at sliding mode control we develop a two loop architecture





# Dynamic Sliding Manifolds

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- To stabilize rotational dynamics when tracking translational variables we can add integral terms to sliding manifold

$$s(x) = e + v + C\theta$$

- Integral term provides robustness to matched uncertainties, and internal dynamics are stabilized by rotational feedback term





# Higher Order Sliding Modes

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- Chattering is an important problem in sliding mode control
- Dangerous for actuators
- HOSM keeps the constraint
- With the following algorithm:

$$u(t) = -\lambda\sqrt{|s|}\text{sign}(s) + u_1$$
$$\dot{u}_1 = \begin{cases} -ku & |u| > u_0 \\ -W\text{sign}(s) & |u| \leq u_0 \end{cases}$$

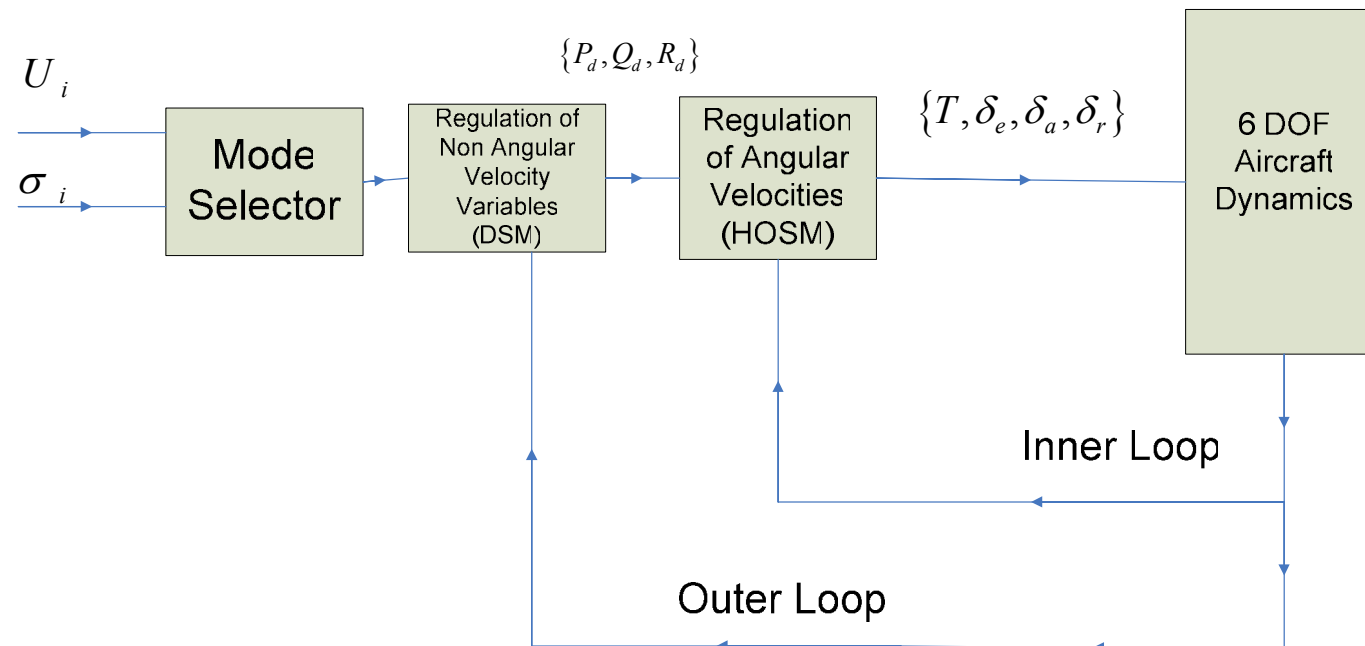
$$s + \dot{s} = 0$$

- Fast switching part is moved into derivative of input, therefore actuators are safe



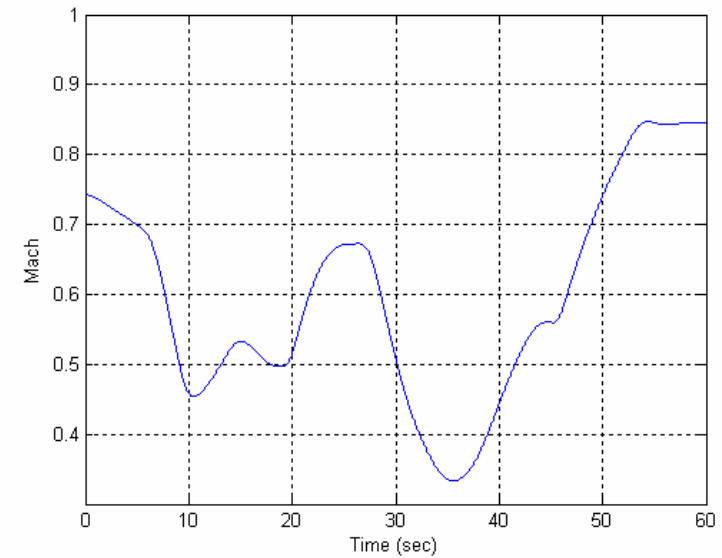
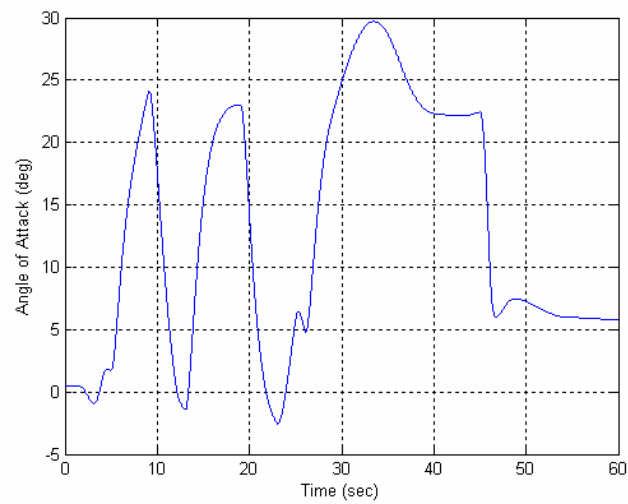
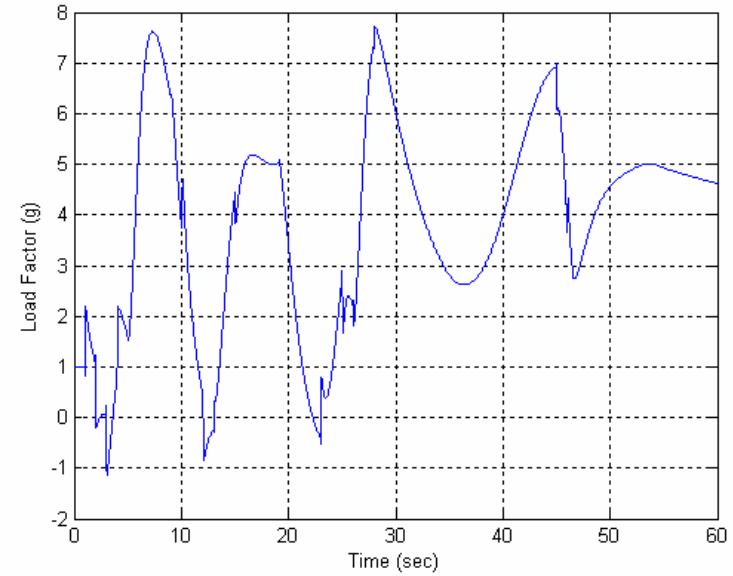
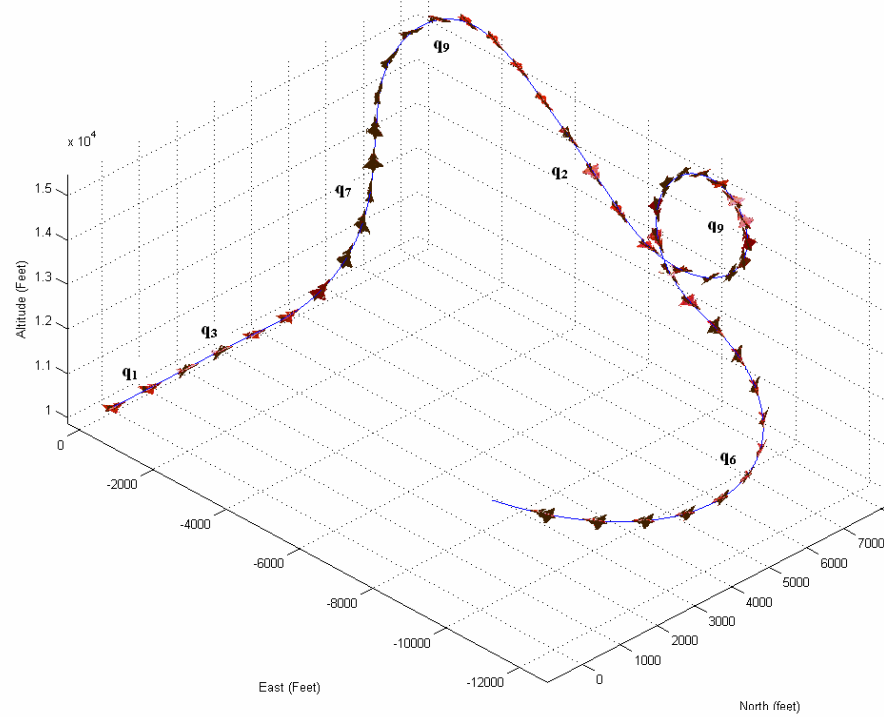
# Control Architecture

- To separate NMP tracking from HOSM part we develop a two loop architecture



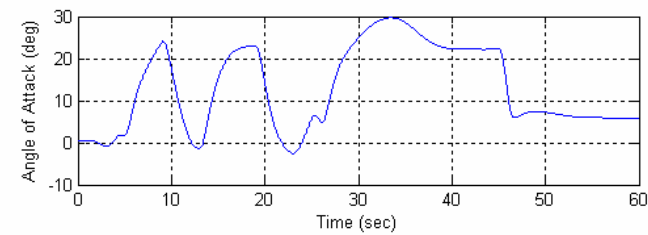
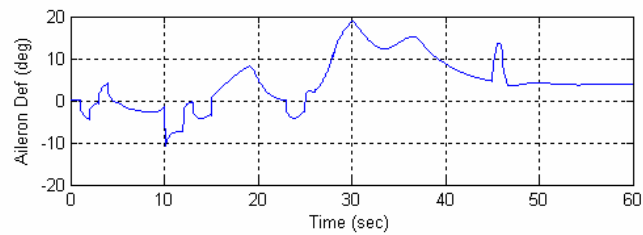
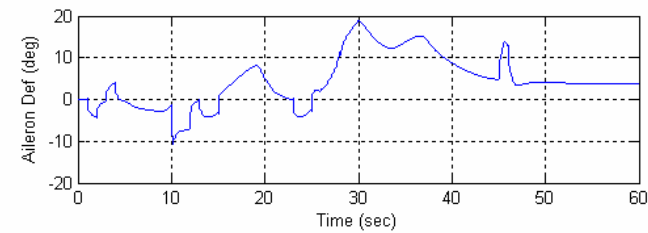
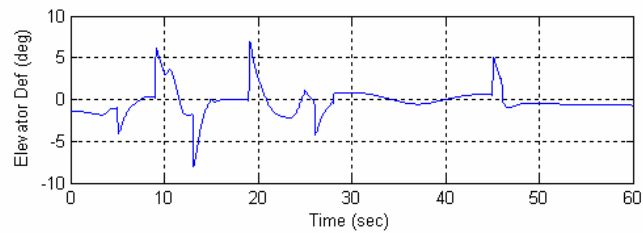
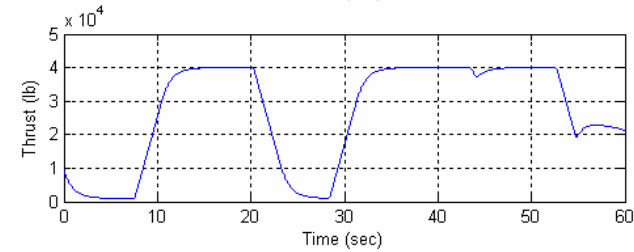
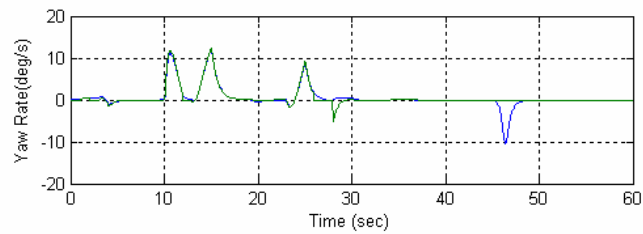
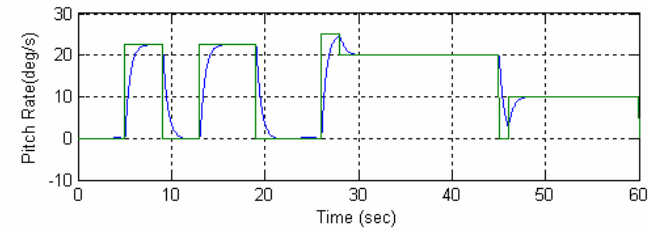
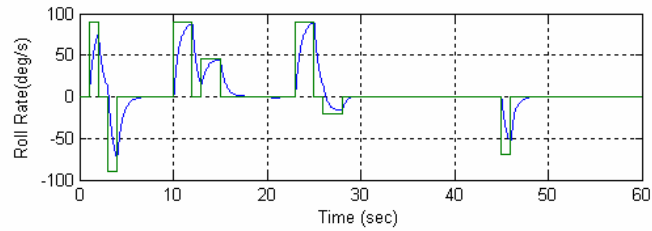


# Simulations





# Simulations cont





# Conclusion

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- We have developed a nonlinear hybrid automata, which describe the dynamics of agile flight with dynamical constraints
- We have developed a mode based control algorithm which tracks the outputs of automaton by sliding control methods
- We now want to define agility metrics to measure the complexity and aggressiveness of maneuvers, we also seek ways to expand coordinated automata by adding coordinated and un-coordinated flight
- Now that we can identify and control maneuver sequences, current research focus on structure of these sequences and planning/synthesis maneuver sequences issues related with the described finite automata.
- Issues such as
  - Reachability : underlying control structure guarantees – Lyapunov approach
  - Safe mode transitions : underlying control structure guarantees – Lyapunov approach