Math 103 Homework Set $\# 2^{1}$

Due on March 7, 2006, at 12:30

1) Let $\forall x \in (0,1), \ \forall n \in \mathbb{Z}, \ N_{x,n} := (n - \frac{1}{x}, n + x)$. Determine

$$1.a) \qquad \bigcup_{n \in \mathbb{Z}} N_{\frac{1}{2},n}$$

$$1.b) \qquad \bigcap_{n \in \mathbb{Z}} N_{\frac{1}{2},n}$$

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$$\bigcap_{n \in \mathbb{Z}} N_{\frac{1}{2},n}$$
1.c)
$$\bigcup_{x \in (0,1)} N_{x,0}$$

$$1.d) \qquad \bigcap_{x \in (0,1)} N_{x,0}$$

2) Let A, B and C be sets. Prove

2.a)
$$(A - B) - C \subseteq A - (B - C)$$
;

2.b)
$$A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$$
.

3) Let A be a set, $\{B_{\alpha}\}_{{\alpha}\in\tau}$ be a family of sets, and S is the universal set for A and B_{α} for all $\alpha \in \tau$. Prove

3.a)
$$A \cup \left(\bigcap_{\alpha \in \tau} B_{\alpha}\right) = \bigcap_{\alpha \in \tau} (A \cup B_{\alpha})$$

$$3.b) \qquad \left(\bigcup_{\alpha \in \tau} B_{\alpha}\right)^{c} = \bigcap_{\alpha \in \tau} B_{\alpha}^{c}$$

4) Let A and B be subsets of a set U, and recall that for every set S the power set of S is denoted by 2^S . Prove

$$4.a) 2^A \subseteq 2^U;$$

$$4.b) 2^{A-B} \neq 2^A - 2^B$$

¹Each problem will be graded out of 20 points.