## Math 303, Fall 2006 Assignment for Dec. 02 - 05

- Read pages 775-781 of the textbook (Riley-Hobson-Bence, 3rd Edition).
- Solve Problems 22.1, 22.2 of the textbook.
- Solve the following problems.
  - 1. Find the stationary points of the following functionals.

$$\mathcal{F}[y(x)] = \int_a^b \sqrt{1 + \frac{y'^2}{y^2}} dx,$$

$$\mathcal{G}[y(x)] = \int_a^b \frac{\sqrt{1 + y'^2}}{1 + y} dx,$$

2. Let S be the surface of revolution of the curve  $z=x^2$  about z-axis. Find the differential equation determining the geodesics on S and obtain its solution.