frequency; (c) use light of longer wavelength; (d) use a metal surface with a larger work function. In each case justify your answer. **Q38.13** A photon of frequency f undergoes Compton scattering from an electron at rest and scatters through an angle  $\phi$ . The frequency of the scattered photon is f'. How is f' related to f? Does your answer depend on  $\phi$ ? Explain.

Q38.14 Can Compton scattering occur with protons as well as electrons? For example, suppose a beam of x rays is directed at a target of liquid hydrogen. (Recall that the nucleus of hydrogen consists of a single proton.) Compared to Compton scattering with electrons, what similarities and differences would you expect? Explain.

**Q38.15** Why must engineers and scientists shield against x-ray production in high-voltage equipment?

**Q38.16** In attempting to reconcile the wave and particle models of light, some people have suggested that the photon rides up and down on the crests and troughs of the electromagnetic wave. What things are *wrong* with this description?

Q38.17 Some lasers emit light in pulses that are only  $10^{-12}$  s in duration. The length of such a pulse is  $(3 \times 10^8 \text{ m/s})(10^{-12} \text{ s}) = 3 \times 10^{-4} \text{ m} = 0.3 \text{ mm}$ . Can pulsed laser light be as monochromatic as light from a laser that emits a steady, continuous beam? Explain.

### **EXERCISES**

### Section 38.1 Light Absorbed as Photons: The Photoelectric Effect

**38.1** •• (a) A proton is moving at a speed much slower than the speed of light. It has kinetic energy  $K_1$  and momentum  $p_1$ . If the momentum of the proton is doubled, so  $p_2 = 2p_1$ , how is its new kinetic energy  $K_2$  related to  $K_1$ ? (b) A photon with energy  $E_1$  has momentum  $p_1$ . If another photon has momentum  $p_2$  that is twice  $p_1$ , how is the energy  $E_2$  of the second photon related to  $E_1$ ?

38.2 • Bin Response of the Eye. The human eye is most sensitive to green light of wavelength 505 nm. Experiments have found that when people are kept in a dark room until their eyes adapt to the darkness, a *single* photon of green light will trigger receptor cells in the rods of the retina. (a) What is the frequency of this photon? (b) How much energy (in joules and electron volts) does it deliver to the receptor cells? (c) To appreciate what a small amount of energy this is, calculate how fast a typical bacterium of mass  $9.5 \times 10^{-12}$  g would move if it had that much energy.

**38.3** • A photon of green light has a wavelength of 520 nm. Find the photon's frequency, magnitude of momentum, and energy. Express the energy in both joules and electron volts.

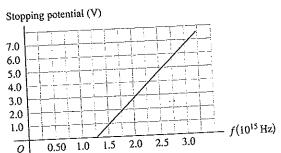
38.4 • 810 A laser used to weld detached retinas emits light with a wavelength of 652 nm in pulses that are 20.0 ms in duration. The average power during each pulse is 0.600 W. (a) How much energy is in each pulse in joules? In electron volts? (b) What is the energy of one photon in joules? In electron volts? (c) How many photons are in each pulse?

**38.5** • A 75-W light source consumes 75 W of electrical power. Assume all this energy goes into emitted light of wavelength 600 nm. (a) Calculate the frequency of the emitted light. (b) How many photons per second does the source emit? (c) Are the answers to parts (a) and (b) the same? Is the frequency of the light the same thing as the number of photons emitted per second? Explain.

**38.6** • A photon has momentum of magnitude  $8.24 \times 10^{-28}$  kg·m/s. (a) What is the energy of this photon? Give your answer in joules and in electron volts. (b) What is the wavelength of this photon? In what region of the electromagnetic spectrum does it lie?

**38.7** • The graph in Fig. E38.7 shows the stopping potential as a function of the frequency of the incident light falling on a metal surface. (a) Find the photoelectric work function for this metal. (b) What value of Planck's constant does the graph yield? (c) Why does the graph *not* extend below the x-axis? (d) If a different metal were used, which characteristics of the graph would you expect to be the same and which ones would be different?

Figure E38.7



**38.8** • The photoelectric threshold wavelength of a tungsten surface is 272 nm. Calculate the maximum kinetic energy of the electrons ejected from this tungsten surface by ultraviolet radiation of frequency  $1.45 \times 10^{15}$  Hz. Express the answer in electron volts. **38.9** • • A clean nickel surface is exposed to light of wavelength

235 nm. What is the maximum speed of the photoelectrons emitted from this surface? Use Table 38.1.

38.18 •• What would the minimum work function for a metal have to be for visible light (380-750 nm) to eject photoelectrons?

**38.11** •• When ultraviolet light with a wavelength of 400.0 nm falls on a certain metal surface, the maximum kinetic energy of the emitted photoelectrons is measured to be 1.10 eV. What is the maximum kinetic energy of the photoelectrons when light of wavelength 300.0 nm falls on the same surface?

38.12 •• The photoelectric work function of potassium is 2.3 eV. If light having a wavelength of 250 nm falls on potassium, find (a) the stopping potential in volts; (b) the kinetic energy in electron volts of the most energetic electrons ejected; (c) the speed of these electrons.

**38.13** • When ultraviolet light with a wavelength of 254 nm falls on a clean copper surface, the stopping potential necessary to stop emission of photoelectrons is 0.181 V. (a) What is the photoelectric threshold wavelength for this copper surface? (b) What is the work function for this surface, and how does your calculated value compare with that given in Table 38.1?

# Section 38.2 Light Emitted as Photons: X-Ray Production

38.14 • The cathode-ray tubes that generated the picture in early color televisions were sources of x rays. If the acceleration voltage in a television tube is 15.0 kV, what are the shortest-wavelength x rays produced by the television? (Modern televisions contain shielding to stop these x rays.)

**38.15** • Protons are accelerated from rest by a potential difference of 4.00 kV and strike a metal target. If a proton produces one photon on impact, what is the minimum wavelength of the resulting x rays? How does your answer compare to the minimum wavelength if 4.00-keV electrons are used instead? Why do x-ray tubes use electrons rather than protons to produce x rays?

38.16 •• (a) What is the minimum potential difference between the filament and the target of an x-ray tube if the tube is to produce

x rays with a wavelength of 0.150 nm? (b) What is the shortest wavelength produced in an x-ray tube operated at 30.0 kV?

### Section 38.3 Light Scattered as Photons: Compton Scattering and Pair Production

**38.17** • An x ray with a wavelength of 0.100 nm collides with an electron that is initially at rest. The x ray's final wavelength is 0.110 nm. What is the final kinetic energy of the electron?

**38.18** • X rays are produced in a tube operating at 18.0 kV. After emerging from the tube, x rays with the minimum wavelength produced strike a target and are Compton-scattered through an angle of 45.0°. (a) What is the original x-ray wavelength? (b) What is the wavelength of the scattered x rays? (c) What is the energy of the scattered x rays (in electron volts)?

**38.19** •• X rays with initial wavelength 0.0665 nm undergo Compton scattering. What is the longest wavelength found in the scattered x rays? At which scattering angle is this wavelength observed?

**38.20** • A beam of x rays with wavelength 0.0500 nm is Compton-scattered by the electrons in a sample. At what angle from the incident beam should you look to find x rays with a wavelength of (a) 0.0542 nm; (b) 0.0521 nm; (c) 0.0500 nm?

**38.21** •• If a photon of wavelength 0.04250 nm strikes a free electron and is scattered at an angle of 35.0° from its original direction, find (a) the change in the wavelength of this photon; (b) the wavelength of the scattered light; (c) the change in energy of the photon (is it a loss or a gain?); (d) the energy gained by the electron

**38.22** •• A photon scatters in the backward direction ( $\phi = 180^{\circ}$ ) from a free proton that is initially at rest. What must the wavelength of the incident photon be if it is to undergo a 10.0% change in wavelength as a result of the scattering?

**38.23** •• X rays with an initial wavelength of  $0.900 \times 10^{-10}$  m undergo Compton scattering. For what scattering angle is the wavelength of the scattered x rays greater by 1.0% than that of the incident x rays?

**38.24** •• A photon with wavelength  $\lambda = 0.1385$  nm scatters from an electron that is initially at rest. What must be the angle between the direction of propagation of the incident and scattered photons if the speed of the electron immediately after the collision is  $8.90 \times 10^6$  m/s?

**38.25** • An electron and a positron are moving toward each other and each has speed 0.500c in the lab frame. (a) What is the kinetic energy of each particle? (b) The e<sup>+</sup> and e<sup>-</sup> meet head-on and annihilate. What is the energy of each photon that is produced? (c) What is the wavelength of each photon? How does the wavelength compare to the photon wavelength when the initial kinetic energy of the e<sup>+</sup> and e<sup>-</sup> is negligibly small (see Example 38.6)?

# Section 38.4 Wave—Particle Duality, Probability, and Uncertainty

**38.26** • A laser produces light of wavelength 625 nm in an ultrashort pulse. What is the minimum duration of the pulse if the minimum uncertainty in the energy of the photons is 1.0%?

**38.27** • An ultrashort pulse has a duration of 9.00 fs and produces light at a wavelength of 556 nm. What are the momentum and momentum uncertainty of a single photon in the pulse?

**38.28** • A horizontal beam of laser light of wavelength 585 nm passes through a narrow slit that has width 0.0620 mm. The intensity of the light is measured on a vertical screen that is 2.00 m from the slit. (a) What is the minimum uncertainty in the vertical component of the momentum of each photon in the beam after the

photon has passed through the slit? (b) Use the result of part (a) to estimate the width of the central diffraction maximum that is observed on the screen.

#### **PROBLEMS**

38.29 • Exposing Photographic Film. The light-sensitive compound on most photographic films is silver bromide, AgBr. A film is "exposed" when the light energy absorbed dissociates this molecule into its atoms. (The actual process is more complex, but the quantitative result does not differ greatly.) The energy of dissociation of AgBr is  $1.00 \times 10^5$  J/mol. For a photon that is just able to dissociate a molecule of silver bromide, find (a) the photon energy in electron volts; (b) the wavelength of the photon; (c) the frequency of the photon. (d) What is the energy in electron volts of a photon having a frequency of 100 MHz? (e) Light from a firefly can expose photographic film, but the radiation from an FM station broadcasting 50,000 W at 100 MHz cannot. Explain why this is so. 38.30 ·· (a) If the average frequency emitted by a 200-W light bulb is  $5.00 \times 10^{14}$  Hz, and 10.0% of the input power is emitted as visible light, approximately how many visible-light photons are emitted per second? (b) At what distance would this correspond to  $1.00 \times 10^{11}$  visible-light photons per square centimeter per second if the light is emitted uniformly in all directions?

**38.31** • When a certain photoelectric surface is illuminated with light of different wavelengths, the following stopping potentials are observed:

Stopping potential (V)
1.48
1.15
0.93
0.62
0.36
0.24

Plot the stopping potential on the vertical axis against the frequency of the light on the horizontal axis. Determine (a) the threshold frequency; (b) the threshold wavelength; (c) the photoelectric work function of the material (in electron volts); (d) the value of Planck's constant h (assuming that the value of e is known).

**38.32** • A 2.50-W beam of light of wavelength 124 nm falls on a metal surface. You observe that the maximum kinetic energy of the ejected electrons is 4.16 eV. Assume that each photon in the beam ejects a photoelectron. (a) What is the work function (in electron volts) of this metal? (b) How many photoelectrons are ejected each second from this metal? (c) If the power of the light beam, but not its wavelength, were reduced by half, what would be the answer to part (b)? (d) If the wavelength of the beam, but not its power, were reduced by half, what would be the answer to part (b)?

**38.33** ••• CP BiB Removing Vascular Lestons. A pulsed dye laser emits light of wavelength 585 nm in 450- $\mu$ s pulses. Because this wavelength is strongly absorbed by the hemoglobin in the blood, the method is especially effective for removing various types of blemishes due to blood, such as port-wine-colored birthmarks. To get a reasonable estimate of the power required for such laser surgery, we can model the blood as having the same specific heat and heat of vaporization as water (4190 J/kg·K, 2.256 ×10<sup>6</sup> J/kg). Suppose that each pulse must remove 2.0  $\mu$ g of blood by evaporating it, starting at 33°C. (a) How much energy must each pulse deliver to the blemish? (b) What must be the power output of this laser? (c) How many photons does each pulse deliver to the blemish?

**38.34** • The photoelectric work functions for particular samples of certain metals are as follows: cesium, 2.1 eV; copper, 4.7 eV;

potassium, 2.3 eV; and zinc, 4.3 eV. (a) What is the threshold wavelength for each metal surface? (b) Which of these metals could *not* emit photoelectrons when irradiated with visible light (380-750 nm)?

**38.35** •• An incident x-ray photon of wavelength 0.0900 nm is scattered in the backward direction from a free electron that is initially at rest. (a) What is the magnitude of the momentum of the scattered photon? (b) What is the kinetic energy of the electron after the photon is scattered?

**38.36** •• CP A photon with wavelength  $\lambda = 0.0900$  nm is incident on an electron that is initially at rest. If the photon scatters in the backward direction, what is the magnitude of the linear momentum of the electron just after the collision with the photon? **38.37** •• CP A photon with wavelength  $\lambda = 0.1050$  nm is incident on an electron that is initially at rest. If the photon scatters at an angle of  $60.0^{\circ}$  from its original direction, what are the magnitude and direction of the linear momentum of the electron just after the collision with the photon?

**38.38** •• CP An x-ray tube is operating at voltage V and current I. (a) If only a fraction p of the electric power supplied is converted into x rays, at what rate is energy being delivered to the target? (b) If the target has mass m and specific heat c (in  $J/kg \cdot K$ ), at what average rate would its temperature rise if there were no thermal losses? (c) Evaluate your results from parts (a) and (b) for an x-ray tube operating at 18.0 kV and 60.0 mA that converts 1.0% of the electric power into x rays. Assume that the 0.250-kg target is made of lead ( $c = 130 \text{ J/kg} \cdot K$ ). (d) What must the physical properties of a practical target material be? What would be some suitable target elements?

38.39 · Nuclear fusion reactions at the center of the sun produce gamma-ray photons with energies of about 1 MeV (106 eV). By contrast, what we see emanating from the sun's surface are visiblelight photons with wavelengths of about 500 nm. A simple model that explains this difference in wavelength is that a photon undergoes Compton scattering many times—in fact, about 10<sup>26</sup> times, as suggested by models of the solar interior—as it travels from the center of the sun to its surface. (a) Estimate the increase in wavelength of a photon in an average Compton-scattering event. (b) Find the angle in degrees through which the photon is scattered in the scattering event described in part (a). (Hint: A useful approximation is  $\cos \phi \approx 1 - \phi^2/2$ , which is valid for  $\phi \ll 1$ . Note that  $\phi$  is in radians in this expression.) (c) It is estimated that a photon takes about 106 years to travel from the core to the surface of the sun. Find the average distance that light can travel within the interior of the sun without being scattered. (This distance is roughly equivalent to how far you could see if you were inside the sun and could survive the extreme temperatures there. As your answer shows, the interior of the sun is very opaque.)

**38.40** •• (a) Derive an expression for the total shift in photon wavelength after two successive Compton scatterings from electrons at rest. The photon is scattered by an angle  $\theta_1$  in the first scat-

tering and by  $\theta_2$  in the second. (b) In general, is the total shift in wavelength produced by two successive scatterings of an angle  $\theta/2$  the same as by a single scattering of  $\theta$ ? If not, are there any specific values of  $\theta$ , other than  $\theta=0^\circ$ , for which the total shifts are the same? (c) Use the result of part (a) to calculate the total wavelength shift produced by two successive Compton scatterings of  $30.0^\circ$  each. Express your answer in terms of h/mc. (d) What is the wavelength shift produced by a single Compton scattering of  $60.0^\circ$ ? Compare to the answer in part (c).

**38.41** •• A photon with wavelength 0.1100 nm collides with a free electron that is initially at rest. After the collision the wavelength is 0.1132 nm. (a) What is the kinetic energy of the electron after the collision? What is its speed? (b) If the electron is suddenly stopped (for example, in a solid target), all of its kinetic energy is used to create a photon. What is the wavelength of this photon?

**38.42** •• An x-ray photon is scattered from a free electron (mass m) at rest. The wavelength of the scattered photon is  $\lambda'$ , and the final speed of the struck electron is v. (a) What was the initial wavelength  $\lambda$  of the photon? Express your answer in terms of  $\lambda'$ , v, and m. (Hint: Use the relativistic expression for the electron kinetic energy.) (b) Through what angle  $\phi$  is the photon scattered? Express your answer in terms of  $\lambda$ ,  $\lambda'$ , and m. (c) Evaluate your results in parts (a) and (b) for a wavelength of  $5.10 \times 10^{-3}$  nm for the scattered photon and a final electron speed of  $1.80 \times 10^{8}$  m/s. Give  $\phi$  in degrees.

**38.43** •• (a) Calculate the maximum increase in photon wavelength that can occur during Compton scattering. (b) What is the energy (in electron volts) of the lowest-energy x-ray photon for which Compton scattering could result in doubling the original wavelength?

### CHALLENGE PROBLEM

**38.44** ••• Consider Compton scattering of a photon by a moving electron. Before the collision the photon has wavelength  $\lambda$  and is moving in the +x-direction, and the electron is moving in the -x-direction with total energy E (including its rest energy  $mc^2$ ). The photon and electron collide head-on. After the collision, both are moving in the -x-direction (that is, the photon has been scattered by 180°). (a) Derive an expression for the wavelength  $\lambda'$  of the scattered photon. Show that if  $E \gg mc^2$ , where m is the rest mass of the electron, your result reduces to

$$\lambda' = \frac{hc}{E} \left( 1 + \frac{m^2 c^4 \lambda}{4hcE} \right)$$

(b) A beam of infrared radiation from a CO<sub>2</sub> laser ( $\lambda = 10.6~\mu m$ ) collides head-on with a beam of electrons, each of total energy  $E = 10.0~{\rm GeV}$  (1 GeV =  $10^9~{\rm eV}$ ). Calculate the wavelength  $\lambda'$  of the scattered photons, assuming a 180° scattering angle. (c) What kind of scattered photons are these (infrared, microwave, ultraviolet, etc.)? Can you think of an application of this effect?

## Answers

# Chapter Opening Question



The energy of a photon E is inversely proportional to its wavelength  $\lambda$ : The shorter the wavelength, the more energetic is the photon. Since visible light has shorter wavelengths than infrared light,

the headlamp emits photons of greater energy. However, the light from the infrared laser is far more *intense* (delivers much more energy per second per unit area to the patient's skin) because it emits many more photons per second than does the headlamp and concentrates them onto a very small spot.