

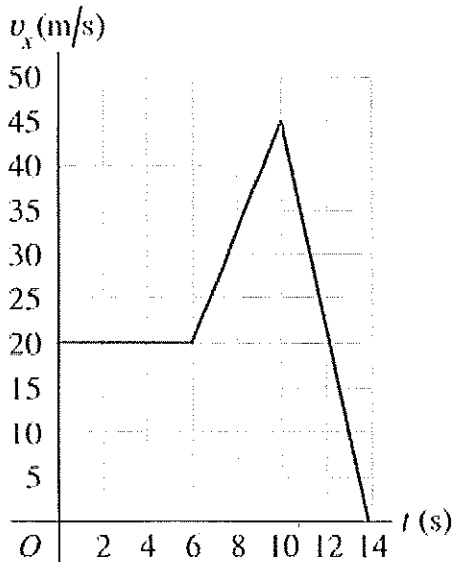
Closed book. No calculators are to be used for this quiz.  
Quiz duration: 10 minutes

Name:

Student ID:

Signature:

The graph below shows the velocity of a motorcycle police officer plotted as a function of time. (a) Find the instantaneous acceleration at  $t=3$  s, at  $t=7$  s, and at  $t=11$  s. (b) How far does the officer go in the first 6 s? The first 10 s? The first 14 s?



a) At  $t=3$  s,  $v_x-t$  curve is a straight line, which has zero slope, so

• At  $t=3$   $a_x = 0$

• At  $t=7$  s,  $a_{x,t} = \frac{\Delta v_x}{\Delta t} = \frac{45 \text{ m/s} - 20 \text{ m/s}}{10 \text{ s} - 6 \text{ s}} = 6.25 \text{ m/s}^2$

• At  $t=11$  s,  $a_{x,t} = \frac{10 - 45 \text{ m/s}}{14 \text{ s} - 10 \text{ s}} = -11.25 \text{ m/s}^2$

b) For  $t=0$  to  $t=6$  s;  $x-x_0 = v_{0x} \cdot t + \frac{1}{2} a t^2$ , but  $a_x = 0$  in this interval.

$$x - x_0 = v_{0x} \cdot t = (20 \text{ m/s}) \cdot (6 \text{ s}) = 120 \text{ m}.$$

• For  $t=6$  s to  $t=10$  s;  $x - x_0 = v_{0x} \cdot t + \frac{1}{2} a t^2$ ,  $a = 6.25 \text{ m/s}^2$ ,  $v_{0x} = 20 \text{ m/s}$ ,  $x_0 = 120 \text{ m}$

$$x - 120 \text{ m} = (20 \text{ m/s}) \cdot 4 \text{ s} + \frac{1}{2} (6.25 \text{ m/s}^2) (4 \text{ s})^2$$

$$x = 250 \text{ m}.$$

• For  $t=10$  s to  $t=14$  s;  $a = -11.25 \text{ m/s}^2$ ,  $v_{0x} = 45 \text{ m/s}$ ,  $x_0 = 250 \text{ m}$ .

$$x - 250 \text{ m} = (45 \text{ m/s}) \cdot 4 \text{ s} + \frac{1}{2} (-11.25 \text{ m/s}^2) (4 \text{ s})^2$$

$$x - 250 \text{ m} = 180 \text{ m} - 90 \text{ m}$$

$$x = 340 \text{ m}.$$

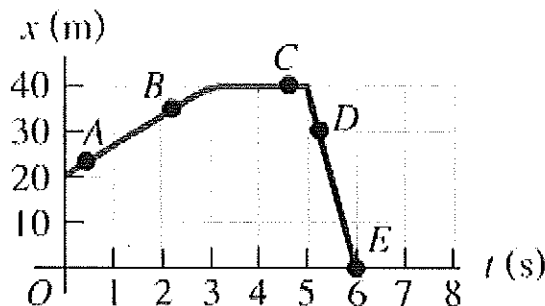
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A test car travels in a straight line along the x-axis. The graph below shows the car's position as a function of time. (a) Find the car's instantaneous velocity at points A, B, C, D, and E. (b) Find the car's instantaneous acceleration at points A, B, C, D, and E.



a) Instantaneous velocity is given by the slope of the x versus t graph.

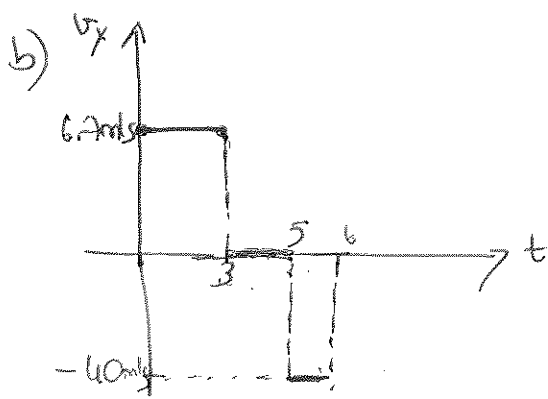
$$A: v_x = \frac{\Delta x}{\Delta t} = \frac{(40\text{m} - 20\text{m})}{3\text{s}} = 6.7\text{m/s}$$

$$B: \text{same as point A, } v_x = 6.7\text{m/s.}$$

$$C: v_x = 0 \text{ (straight line)}$$

$$D: v_x = \frac{(0 - 40\text{m})}{1\text{s}} = -40\text{m/s}$$

$$E: \text{same as point D, } v_x = -40\text{m/s}$$



Since the  $v_x$ - $t$  graph is straight line, slope is zero, so acceleration is zero through all points.

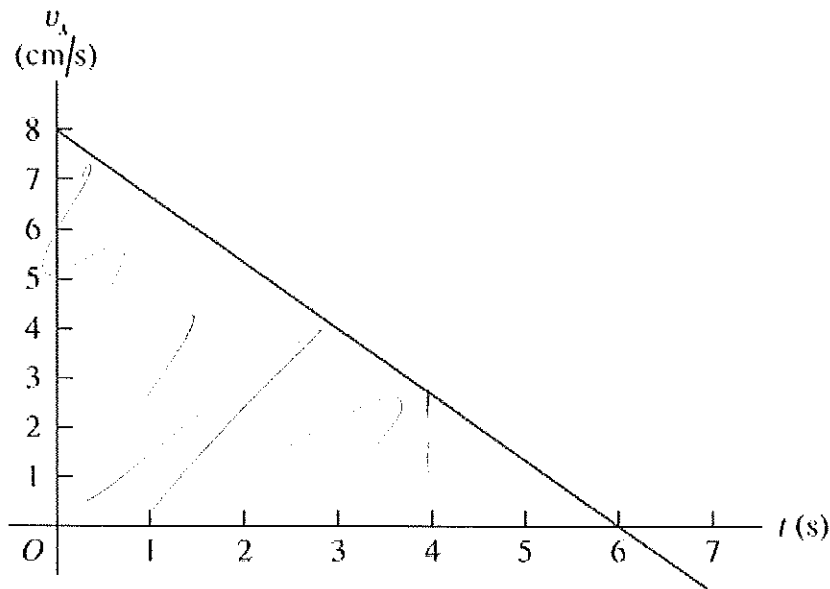
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A cat walks in a straight line. The graph of its velocity as a function of time is given below. (a) Find the cat's velocity at  $t=4$  s and  $t=7$  s. (b) What distance does the cat move during the first 4 s (between  $t=0$  s and  $t=4$  s)?



a) Use the formula  $v_x = v_{0x} + a_x \cdot t$ , to find the velocity.

Let us first find the acceleration:  $a_x = \frac{-8 \text{ m/s}}{6 \text{ s}} = -1.4 \text{ m/s}^2$

$$\text{at } t=4 \text{ s } \quad v_x = 8 \text{ m/s} + (-1.4 \text{ m/s}^2) \cdot 4$$

$$v_x = 2.4 \text{ m/s}$$

$$\text{at } t=7 \text{ s } \quad v_x = 8 \text{ m/s} + (-1.4 \text{ m/s}^2) \cdot 7 = -1.8 \text{ m/s}$$

$$\text{b) } \quad x - x_0 = v_{0x} \cdot t + \frac{1}{2} a t^2$$

$$x = (8 \text{ m/s}) \cdot 4 \text{ s} + \frac{1}{2} \cdot (-1.4 \text{ m/s}^2) \cdot (4 \text{ s})^2$$

$$x = 32 \text{ m} - 11.2 \text{ m} = 20.8 \text{ m}$$

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A ball is thrown vertically upward with an initial velocity  $v_0$ . Find an expression for the height of the ball at  $t = t_{max}/2$  where  $t_{max}$  is the time it takes for the ball to reach the maximum height. You should consider the gravitational acceleration to be  $g$ . Your answer should be a function of  $v_0$  and  $g$  only.



At maximum height  $v_y = 0$ .

$$v_y = v_{ay} + a_y \cdot t, \quad v_{ay} = v_0, \quad a_y = -g$$

$$0 = v_0 - g t_{max}$$

$$v_0 = g t_{max} \rightarrow t_{max} = \frac{v_0}{g}$$

$$y - y_0 = v_{ay} \cdot t + \frac{1}{2} a t^2$$

$$\text{At } \frac{t_{max}}{2} = \frac{v_0}{2g} \rightarrow y - y_0 = v_0 \cdot \left(\frac{v_0}{2g}\right) - \frac{1}{2} g \cdot \frac{v_0^2}{4g^2}$$

$$y - y_0 = \frac{v_0^2}{2g} - \frac{v_0^2}{8g}$$

$$y - y_0 = \frac{3v_0^2}{8g}$$

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The acceleration of a bus is given by  $a_x(t) = \alpha t$  where  $\alpha = 1.2 \text{ m/s}^3$ .

(a) If the bus's velocity at  $t=1 \text{ s}$  is  $5 \text{ m/s}$  what is its velocity at  $t=2 \text{ s}$ ?

(b) If the bus's position is  $6 \text{ m}$  at  $t=1 \text{ s}$  what is its position at  $t=2 \text{ s}$ ?

a) Given  $a = \alpha t$  at  $t=1$ ,  $v_x = 5 \text{ m/s}$

$$v(t) = \int a(t) dt$$

$$= \int \alpha t dt$$

$$v(t) = 1.2 \frac{t^2}{2} + c$$

At  $t=1$   $v(1) = 1.2 \text{ m/s}^3 \cdot \frac{1^2}{2} + c = 5 \text{ m/s}$

$$0.6 \text{ m/s} + c = 5 \text{ m/s}$$

$$c = 4.4 \text{ m/s}$$

At  $t=2$   $v(2) = 1.2 \text{ m/s}^3 \cdot \frac{2^2}{2} + 4.4 \text{ m/s}$

$$v(2) = 6.8 \text{ m/s}$$

b)  $x = \int v dt$

$$= \int \left( \frac{\alpha t^2}{2} + 4.4 \text{ m/s} \right) dt$$

$$x(t) = \alpha \frac{t^3}{6} + (4.4 \text{ m/s}) \cdot t + c$$

at  $t=1 \Rightarrow x(1) = 1.2 \text{ m/s}^3 \cdot \frac{1^3}{6} + (4.4 \text{ m/s}) \cdot 1 + c = 6 \text{ m}$

$$4.6 \text{ m} + c = 6 \text{ m}$$

$$c = 1.4 \text{ m}$$

at  $t=2$   
 $x(2) = 1.2 \text{ m/s}^3 \cdot \frac{2^3}{6} + (4.4 \text{ m/s}) \cdot 2 + 1.4 \text{ m}$

$$x(2) = 11.8 \text{ m}$$