

Closed book. No calculators are to be used for this quiz.

Quiz duration: 10 minutes

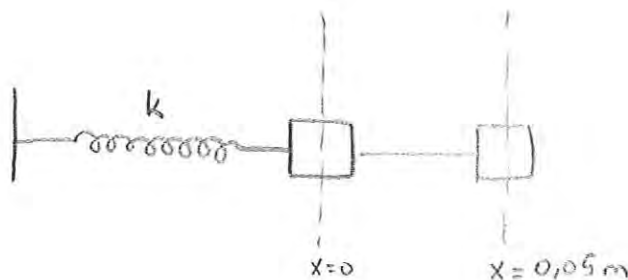
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Consider a spring that does not obey Hooke's Law very faithfully. One end of the spring is fixed. To keep the spring stretched or compressed an amount  $x$ , a force along the  $x$ -axis with  $x$ -component  $F_x = kx - bx^2$  must be applied to the free end. Here  $k = 100 \text{ N/m}$  and  $b = 700 \text{ N/m}^2$ . Note that  $x > 0$  when the spring is stretched and  $x < 0$  when it is compressed. How much work must be done to stretch this spring by  $0.05 \text{ m}$ ?



The force is not constant. So,  $W = \int_{x_0}^{x_1} F(x) dx$

$$W = \int_0^{0,05} (kx - bx^2) dx = \left( \frac{kx^2}{2} - \frac{bx^3}{3} \right) \Big|_{x=0}^{x=0,05} = 50.25 \cdot 10^{-4} - \frac{700 \cdot 1,25 \cdot 10^{-4}}{3}$$

$$= 1250 \cdot 10^{-4} - \frac{875}{3} \cdot 10^{-4} = \underline{\underline{958,3 \cdot 10^{-4} \text{ J}}}$$

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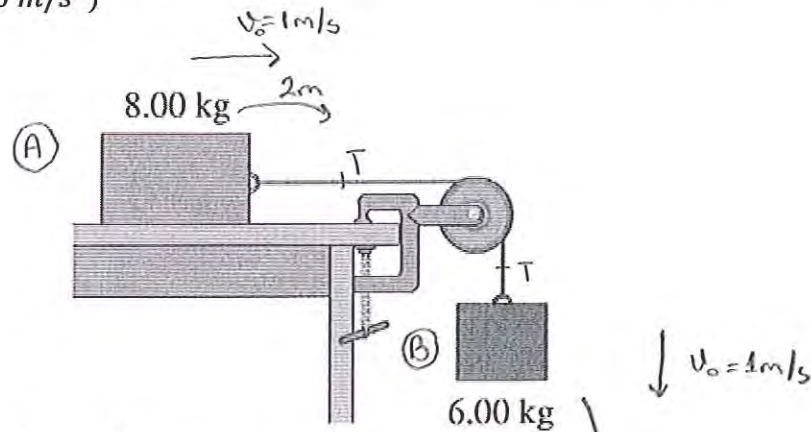
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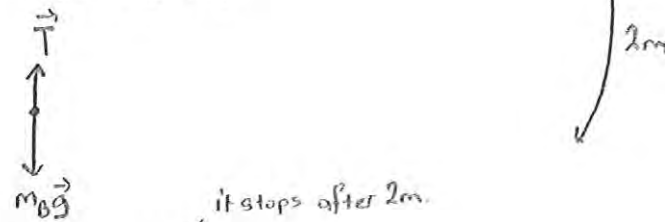
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Consider the system shown in Figure below. The rope and pulley have negligible mass, and the pulley is frictionless. Initially the 6 kg block is moving downward and the 8 kg block is moving to the right, both with a speed of 1 m/s. The blocks come to rest after moving 2 m. Use the work-energy theorem to calculate the coefficient of kinetic friction between the 8 kg block and the tabletop. (Take  $g = 10 \text{ m/s}^2$ )



Work-Energy thm:  $W_{tot} = K_2 - K_1$

for block B:



$$W_B = (m_B g - T)(2m) = \cancel{K_{B2}} - K_{B1}$$

0

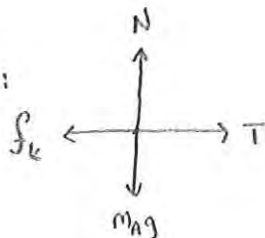
it stops after 2m.

$$(60 - T)2 = -\frac{1}{2}6 \cdot 1^2$$

$$120 - 2T = -3$$

$$T = 61.5 \text{ N}$$

for block A:



$$W_A = (T - f_k)(2m) = \cancel{K_{A2}} - K_{A1}$$

$$(61.5 - \mu_k m_A g)2 = -\frac{1}{2}m_A 1^2$$

$$123 - 2\mu_k 160 = -4$$

$$\boxed{\mu_k = \frac{127}{320} \approx 0.4}$$

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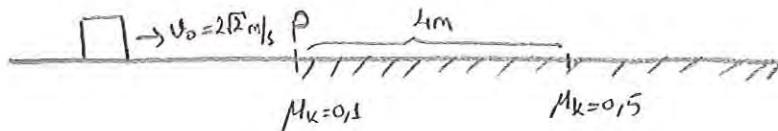
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A box is sliding with a speed of  $2\sqrt{2} \text{ m/s}$  on a horizontal surface when, at point P, it encounters a rough section. On the rough section, the coefficient of friction is not constant, but starts at 0.1 at P and increases linearly with distance past P, reaching a value of 0.5 at 4 m past point P. Use the work-energy theorem to find how far this box slides before stopping. (Take  $g = 10 \text{ m/s}^2$ )



$\mu_k$  is increasing linearly  
at 4m  $\mu_k$  has increased 0,4.  
So, we can say that

$$\mu_k(x) = 0,1x + 0,1$$

Check the values:

$x=0 \Rightarrow \mu_k = 0,1 \checkmark$   
 $x=4 \Rightarrow \mu_k = 0,5 \checkmark$

Work-Energy Thm:  $W_{tot} = K_2 - K_1$

$W_{tot} = \int_0^{x'} f_k(x) dx = - \int_0^{x'} \mu_k(x) \cdot mg dx$

$\mu_k$  is a function of  $x$

$$W_{tot} = -mg \int_0^{x'} (0,1x + 0,1) dx = -mg \left( \frac{0,1x^2}{2} + 0,1x \right) \Big|_{x=0}^{x=x'}$$

$$= -10m (0,05x'^2 + 0,1x') = \frac{K_2}{0} - K_1$$

$$-10m \cdot 0,05x'^2 - 10m \cdot 0,1x' = -\frac{1}{2}m(2\sqrt{2})^2$$

$$0,5x'^2 + x' = 4 \quad (\text{multiply by 2})$$

$$x'^2 + 2x' - 8 = 0$$

+4   -2

$x' = -4$   
 $x' = 2$  } we choose the positive one:  $x' = 2m$

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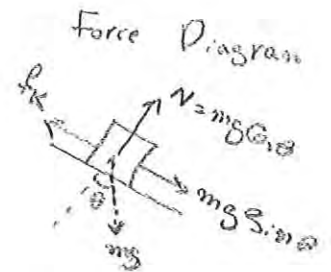
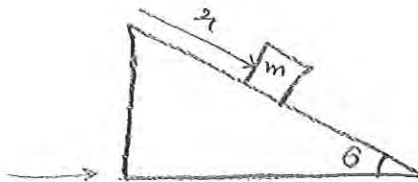
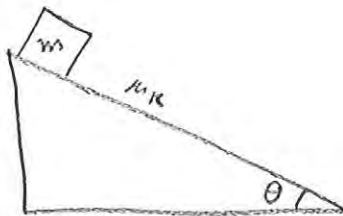
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A block with mass  $2 \text{ kg}$  slides  $2 \text{ m}$  down an inclined plane that slopes downward at an angle of  $37^\circ$ . The coefficient of kinetic friction between the inclined plane and the block is  $0.2$ . If the block starts from rest, find its final kinetic energy using the work-energy theorem? (Take  $g = 10 \text{ m/s}^2$ ,  $\sin 37^\circ = 0.6$  and  $\cos 37^\circ = 0.8$ )



Net forces  $\left\{ \begin{array}{l} f_k: \text{friction} = \mu_k mg \cos \theta \\ F_g = mg \sin \theta \end{array} \right.$

$$\rightarrow F_{\text{Total}} = F_g - f_k$$

$$\rightarrow W_{\text{net}}: \text{Net Work} = (F_g - f_k) x$$

$$m = 2 \text{ kg}$$

$$\mu_k = 0.2$$

$$\theta = 37^\circ$$

constant

$$K_1: \text{initial Kinetic Energy} = 0$$

$$x = 2 \text{ m}$$

$$g = 10$$

work-energy theorem.  $W_{\text{total}} = K_2 - K_1 \Rightarrow W_{\text{total}} = K_2$

$$\Rightarrow (F_g - f_k) x = K_2 \rightarrow mg(\sin \theta - \mu_k \cos \theta) x = K_2$$

$$\Rightarrow 2 \times 10 (\sin 37^\circ - (0.2) \cos 37^\circ) = K_2$$

$$\Rightarrow K_2 = 2 \times 10 (0.6 - 0.16) = 8.8 \text{ J}$$

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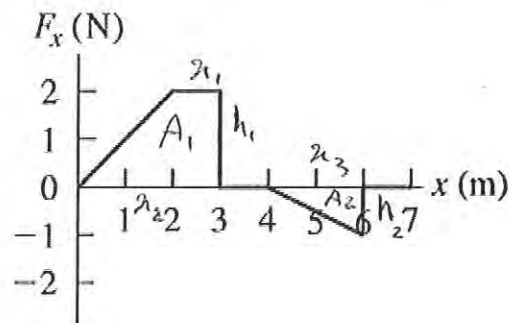
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A force  $\vec{F}$  is applied to a 2 kg block parallel to the x-axis as it moves along a straight track. The x-component of the force varies with the x-coordinate of the car as shown in figure below. Calculate the work done by the force  $\vec{F}$  when the car moves from (a)  $x = 0$  to  $x = 7$  m.



$$W = \int_{x_1}^{x_2} F dx$$

→ From this relation the integration is the sum of the area  $A_1$  and  $A_2$ . But, we should mention that because the force  $F_x$  is negative from  $x=4$  m to  $x=6$  m so we should subtract  $A_1$  and  $A_2$ .

$$W = A_1 - A_2$$

$$A_1 = \text{trapezoid} \Rightarrow A_1 = \frac{(x_1 + x_2) \times h}{2} = \frac{(1 + 3) \times 2}{2} = 4$$

$$A_2 = \text{triangle} \Rightarrow A_2 = \frac{h_2 \times x_2}{2} = \frac{2 \times 1}{2} = 1$$

$$W = A_1 - A_2 = 3 \text{ N}\cdot\text{m}$$