

Closed book. No calculators are to be used for this quiz.

Quiz duration: 10 minutes

First Name:

Last name:

Student ID:

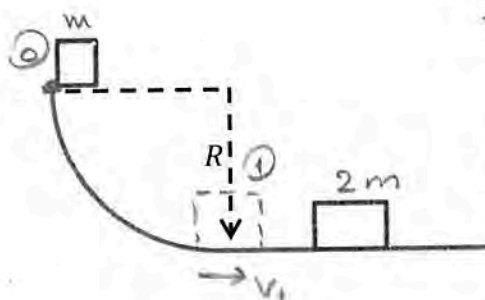
Signature:

A block of mass  $m$  slides from a quarter circular track of radius  $R$  as shown in the figure. After reaching the ground surface, the block makes a completely elastic collision with another block of mass  $2m$ . There is no friction. Find the height the first block can reach after the collision in terms of  $R$ .

SOL.

Cons. of En.

$$mgR = \frac{mv_1^2}{2} \Rightarrow v_1 = \sqrt{2gR}$$



Since there is an elastic coll  
cons. of Mom. and En  
in  $x$  dir.

$$① \quad mv_1 = mv_1' + 2m \cdot v_2'$$

$$② \quad \frac{mv_1^2}{2} = \frac{mv_1'^2}{2} + \frac{2m \cdot v_2'^2}{2}$$

$$\Rightarrow v_1^2 = v_1'^2 + 2 \cdot \frac{(v_1^2 + v_1'^2 - 2v_1 \cdot v_1')}{2}$$

$$\Rightarrow 2v_1^2 = 2v_1'^2 + v_1^2 + v_1'^2 - 2v_1 v_1'$$

$$\Rightarrow 3v_1'^2 - 2v_1 v_1' - v_1^2 = 0 \Rightarrow (3v_1' + v_1)(v_1' - v_1) = 0$$

$$3v_1' + v_1$$

$$v_1' - v_1$$

$v_1'$  should be negative in  $-x$  dir.

$$\Rightarrow \boxed{v_1' = -\frac{v_1}{3}} \Rightarrow \boxed{v_1' = -\frac{\sqrt{2gR}}{3}}$$

Then Cons. of En.

$$\frac{mv_1'^2}{2} = mgh \Rightarrow h = \frac{v_1'^2}{2g} = \frac{2gR}{2 \cdot 9g} = \boxed{\frac{R}{9}} \checkmark$$

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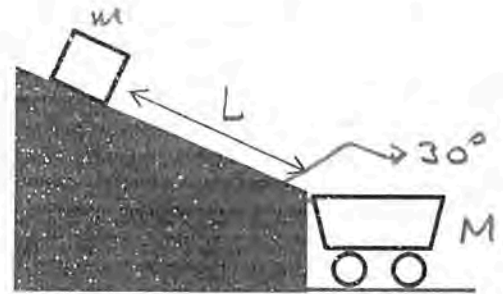
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A box of mass  $m$  slides down on a frictionless inclined surface of length  $L$  and drops into a cart of mass  $M$  as shown in the figure. The inclination angle is  $30^\circ$  with the horizontal ground. Find the speed of the cart in terms of given parameters. (ignore the friction between the cart and the ground.

Gravitational acceleration is  $g$ )



SOL.

$$\textcircled{1} \text{ Cons. of En. } \Rightarrow m g L \cdot \sin 30^\circ = \frac{m v^2}{2} \Rightarrow v = \sqrt{2 g L \cdot \frac{1}{2}} = \sqrt{g L}$$

$\textcircled{2}$  Cons of Mom in "x" direction:

$$v_x = v \cdot \cos 30^\circ = \frac{\sqrt{3}}{2} v \Rightarrow m \frac{\sqrt{3}}{2} v = (m+M) V \Rightarrow$$

$$V = \frac{\sqrt{3} m}{2(m+M)}$$

$V$ : velocity of the cart + box

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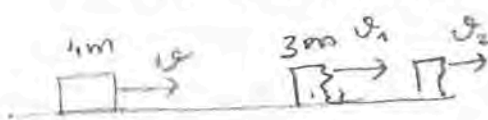
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A particle of mass  $4m$  moving with speed  $v$  on a horizontal frictionless surface explodes into two pieces of mass  $3m$  and  $m$ . The explosion releases an energy equal to the kinetic energy of the particle before the collision. Determine the speed of the piece with mass  $m$  in terms of  $v$ .



SOL.

① Cons. of Momentum

$$4mv = 3mv_1 + mv_2 \Rightarrow 4v = 3v_1 + v_2$$

$$\Rightarrow v_1 = \frac{4v - v_2}{3}$$

② Conservation of Energy

$$K_i + W_{others} = K_f$$

where  $W_{others}$  is the energy released during the explosion.

$$\text{and } W_{others} = K_i$$

$$\Rightarrow \frac{1}{2} 4mv^2 + \frac{1}{2} 4mv^2 = \frac{3mv_1^2}{2} + \frac{mv_2^2}{2} \Rightarrow 8v^2 = 3v_1^2 + v_2^2$$

where  $v_1 = \frac{4v - v_2}{3}$

$$\Rightarrow 8v^2 = \left(\frac{4v - v_2}{3}\right)^2 \cdot 3 + v_2^2 \Rightarrow 8v^2 = \frac{16v^2 + v_2^2 - 8v v_2}{3} + v_2^2$$

$$\Rightarrow \cancel{24v^2} = \cancel{16v^2} + v_2^2 - 8v v_2 + 3v_2^2 \Rightarrow \cancel{8v^2} = \cancel{4v_2^2} - \cancel{8v v_2}$$

$$\Rightarrow v_2^2 - 2v v_2 - 2v^2 = 0$$

$$v_2 = v \pm \sqrt{v^2 + 4v^2} = v \pm \sqrt{5}v$$

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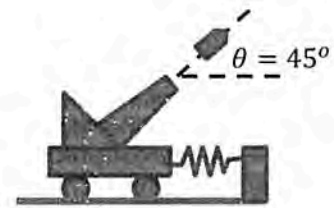
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A cannon aimed at  $45^\circ$  above the horizontal is attached to a spring at rest (spring constant  $k$ ) as shown in the figure. The other end of the spring is fixed. The mass of the cannon is  $M$  and it contains a projectile of mass  $m$ . If the projectile is fired with a speed  $v$  from the cannon, determine the maximum extension of the spring during the recoil of the cannon (ignore all friction).



SOL.

Cons. of Mom. in "x" direction:

$$P_{ix} = P_{fx} = \text{const.} \Rightarrow M \cdot 0 = mv \cdot \cos 45^\circ + (M-m)V$$

$$\Rightarrow 0 = mv \cdot \frac{\sqrt{2}}{2} + (M-m)V \Rightarrow \boxed{V = \frac{mv \cdot \frac{\sqrt{2}}{2}}{M-m}}$$

$M-m$ : mass of canon

Cons. of Energy

$$\frac{(M-m) \cdot V^2}{2} = \frac{kx^2}{2} \Rightarrow x = \sqrt{\frac{(M-m)V^2}{k}} = V \sqrt{\frac{(M-m)}{k}} \quad V: \text{velocity of the canon}$$

$$\Rightarrow x = \frac{mv \sqrt{2}/2}{M-m} \cdot \sqrt{\frac{(M-m)}{k}} = \frac{mv \sqrt{2}}{2} \sqrt{\frac{1}{(M-m)k}} = \boxed{\frac{mv \sqrt{2}}{2} \sqrt{\frac{2}{(M-m)k}}}$$

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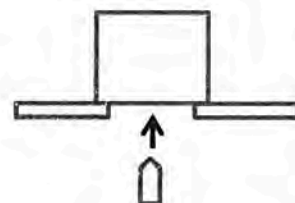
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A wooden block with mass  $m_1$  rests on a table over a large hole as shown in figure. A bullet with mass  $m_2$  enters into the block from the bottom with speed  $v_i$  and remains in the block. If the block and the bullet rise to a height of  $h$  above the table, determine  $v_i$  in terms of given quantities (gravitational acceleration:  $g$ ).



SOL.



Conservation of Energy after the collision

$$\frac{(m_1 + m_2) V_1^2}{2} = (m_1 + m_2) g h$$

$$V_1 = \sqrt{2gh}$$

where  $V_1$  is the initial velocity of the total mass

② Conservation of Momentum

(the mass of the bullet  $m_2$  is so small that the effect of the grav. can be neglected)

$$\vec{P}_i = \vec{P}_f = \text{const} \Rightarrow m_2 v_i = (m_1 + m_2) V_1 \Rightarrow$$

$$v_i = \frac{m_1 + m_2}{m_2} \sqrt{2gh}$$