

Closed book. No calculators are to be used for this quiz.

Quiz duration: 10 minutes

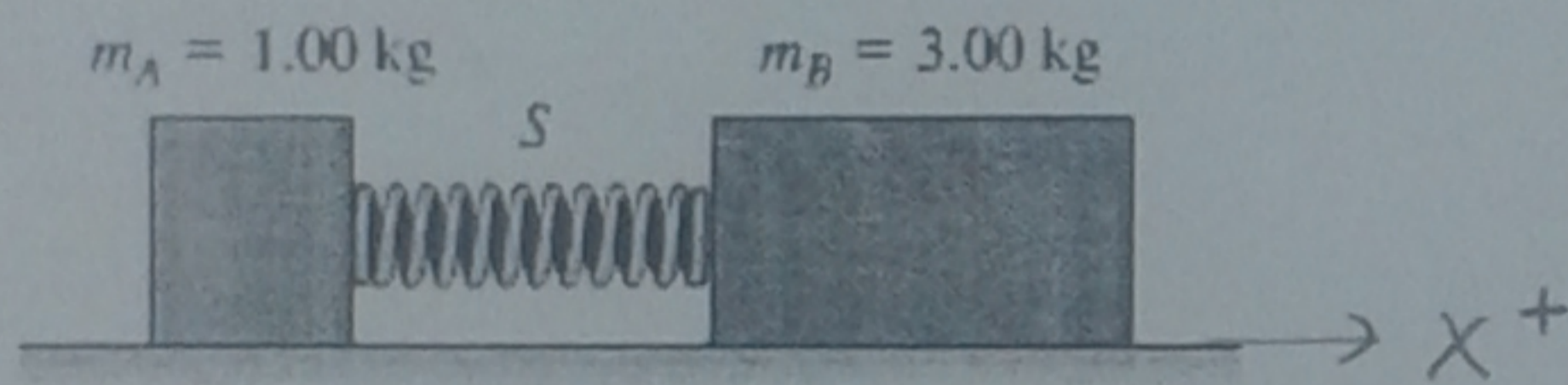
Name:

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Block A in the figure below has mass 1 kg, and block B has mass 3 kg. The blocks are forced together, compressing a spring S between them; then the system is released from rest on a level, frictionless surface. The spring, which has negligible mass, is not fastened to either block and drops to the surface after it has expanded. Block B acquires a speed of 1.2 m/s.

- a) What is the final speed of block A?
 b) How much potential energy was stored in the compressed spring?



a) $v_B = 1.2 \text{ m/s} \Rightarrow$ From the conservation of momentum:

$P_i = P_f$ (no external force applied on the system)

$$P_i = 0 \text{ and } P_f = m_B v_B - m_A v_A \Rightarrow 0 = 3 \cdot 1.2 - 1 \cdot v_A$$

$$\Rightarrow v_A = 3.6 \text{ m/s} //$$

b) From the conservation of energy:

$$\cancel{K_i} + U_i + \cancel{W_{\text{other}}} = \cancel{K_f} + U_f \Rightarrow U_i = K_f$$

where $U_i = U_{\text{spring}} = \frac{1}{2} kx^2$ and $K_f = \frac{m_A v_A^2}{2} + \frac{m_B v_B^2}{2}$

$$\Rightarrow U_{\text{spring}} = \frac{m_A v_A^2}{2} + \frac{m_B v_B^2}{2} = \frac{1 \cdot 3.6^2}{2} + \frac{3 \cdot 1.2^2}{2} = 7.2 \text{ J} //$$

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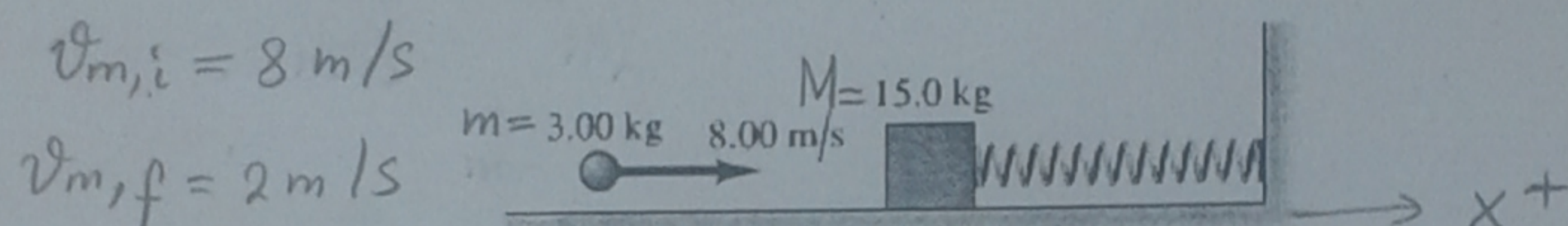
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A 15 kg block is attached to a very light horizontal spring of force constant 500 N/m and is resting on a frictionless horizontal table as shown in the figure. Suddenly it is struck by a 3 kg stone traveling horizontally at 8 m/s to the right, whereupon the stone rebounds at 2 m/s horizontally to the left. Find the maximum distance that the block will compress the spring after the collision.



From the C.O.M. \circ $P_i = P_f \Rightarrow m \cdot v_{m,i} = M \cdot v_M - m \cdot v_{m,f}$

$$\Leftrightarrow 3 \cdot 8 = 15 \cdot v_M - 3 \cdot 2 \Rightarrow v_M = \frac{3 \cdot 10}{15} = 2 \text{ m/s}$$

From the C.O.E \circ $K_i + U_i + W_{\text{others}} = K_f + U_f$
(no dissipation)

$$\Leftrightarrow K_i = U_f \Rightarrow \frac{M \cdot v_M^2}{2} = \frac{k x_{\max}^2}{2}$$

$$\Leftrightarrow x_{\max} = v_M \cdot \sqrt{\frac{M}{k}} = 2 \cdot \sqrt{\frac{15 \cdot 3}{500}} = \frac{2\sqrt{3}}{5} = \frac{\sqrt{3}}{5} \text{ m}$$

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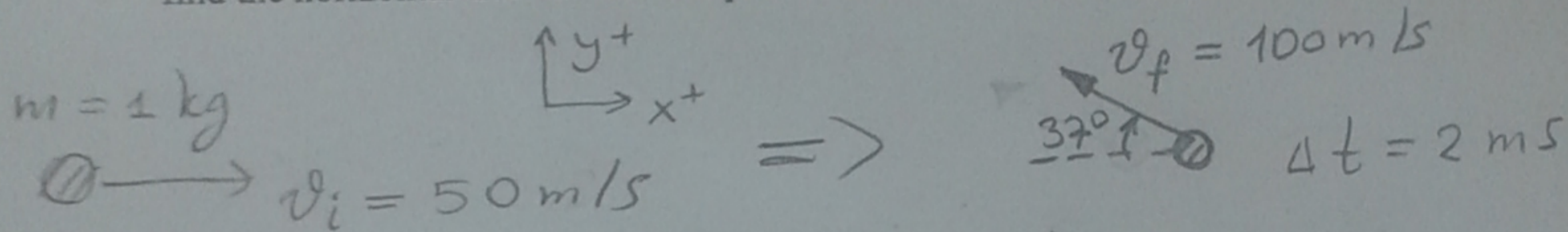
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A bat strikes a 1 kg baseball. Just before impact, the ball is traveling horizontally to the right at 50 m/s, and it leaves the bat traveling to the left at an angle 37 degrees above horizontal with a speed of 100 m/s. If the ball and bat are in contact for 2 ms (1 millisecond = 1/1000 s), find the horizontal and vertical components of the average force on the ball.



Change of momentum: $\vec{p} = \vec{F}_{\text{avg}} \cdot \Delta t$

$$x: \Delta p_x = F_{\text{avg},x} \cdot \Delta t \Rightarrow (-m v_f) - m v_i = F_{\text{avg},x} \cdot \Delta t$$

$$\Rightarrow -1 \cdot 100 - 1 \cdot 50 = F_{\text{avg},x} \cdot 2 \cdot 10^{-3}$$

$$\Rightarrow F_{\text{avg},x} = -\frac{150}{2 \cdot 10^{-3}} = -75 \cdot 10^3 \text{ N} = -75 \text{ kN} //$$

$$y: \Delta p_y = F_{\text{avg},y} \cdot \Delta t \Rightarrow m v_f \cdot \sin 37^\circ - 0 = F_{\text{avg},y} \cdot \Delta t$$

$$\Rightarrow 1 \cdot 100 \cdot \sin 37^\circ = F_{\text{avg},y} \cdot 2 \cdot 10^{-3}$$

$$\Rightarrow F_{\text{avg},y} = \frac{100 \cdot \sin 37^\circ}{2 \cdot 10^{-3}} \approx 30.1 \text{ kN} //$$

$$\Rightarrow \vec{F} = F_x \hat{i} + F_y \hat{j} = -75 \hat{i} + 30.1 \hat{j} \text{ (kN)} //$$