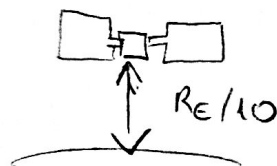


Name:

Student ID:

Signature:

A satellite with mass  $m_s$  is in a circular orbit at a height  $R_E/10$  above the Earth's surface. How much additional work should be done to make the satellite escape from the Earth? Express your answer in terms of  $G$  (gravitational constant),  $R_E$  (radius of the Earth),  $m_s$  (mass of the satellite), and  $M_E$  (mass of the Earth).



Circular orbit

$$m_s \frac{v^2}{\frac{11R_E}{10}} = \frac{m_s M_E G}{\left(\frac{11R_E}{10}\right)^2}$$

$$v^2 = \frac{10 M_E G}{11 R_E}$$

$$E_{\text{mechanical}, i} = \frac{1}{2} m_s v^2 - \frac{M_E G m_s}{\left(\frac{11R_E}{10}\right)} = -\frac{1}{2} \frac{M_E m_s G}{\left(\frac{11R_E}{10}\right)}$$

$$E_{\text{mechanical}, f} + W = 0$$

→ since potential is defined wrt. infinity and the speed is zero when the satellite reaches infinity

$$W = + \frac{1}{2} \frac{M_E m_s G}{\left(\frac{11R_E}{10}\right)}$$

Name:

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Signature:

A rocket is launched from the surface of the Earth with an initial speed  $v_{in}$ . Find an expression for the minimum value of  $v_{in}$  such that the rocket will completely escape from the Earth. Express your answer in terms of  $G$  (gravitational constant),  $R_E$  (radius of the Earth), and  $M_E$  (mass of the Earth).

$$E_{\text{mechanical}} = 0 = K + U$$

$$U = - \frac{G m_{\text{rocket}} M_E}{R_E} \quad (\text{potential at the surface})$$

$$K = \frac{1}{2} m_{\text{rocket}} v_{in}^2$$

$$\frac{1}{2} m_{\text{rocket}} v_{in}^2 - \frac{G m_{\text{rocket}} M_E}{R_E} = 0$$

$$v_{in} = \sqrt{\frac{2 G M_E}{R_E}}$$

Closed book. Duration: 10 minutes

Name:

Student ID:

Signature:

A satellite with mass  $m_s$  is initially stationary at the surface of the Earth. How much work should be done to place this satellite to a circular orbit at a height  $R_E/10$  above the Earth's surface? Express your answer in terms of  $G$  (gravitational constant),  $R_E$  (radius of the Earth),  $m_s$  (mass of the satellite), and  $M_E$  (mass of the Earth).

Circular motion

$$\frac{m_s v_0^2}{\frac{11R_E}{10}} = \frac{m_s M_E G}{\left(\frac{11R_E}{10}\right)^2}$$

$$v_0^2 = \frac{10 M_E G}{11 R_E}$$

$$E_{\text{total, orbit}} = K_{\text{orbit}} + U_{\text{orbit}} = \frac{1}{2} m_s v_0^2 - \frac{G M_E m_s}{\left(\frac{11R_E}{10}\right)}$$

$$E_{\text{total, orbit}} = -\frac{1}{2} \frac{G M_E m_s}{\frac{11R_E}{10}}$$

$$E_{\text{before launch}} = -\frac{G M_E m_s}{R_E}$$

$$W = E_{\text{total, orbit}} - E_{\text{before launch}} = \frac{G M_E m_s}{R_E} \left( -\frac{10}{22} + 1 \right)$$

$$W = \frac{6}{11} \frac{G M_E m_s}{R_E}$$