

Closed book. No calculators are to be used for this quiz.

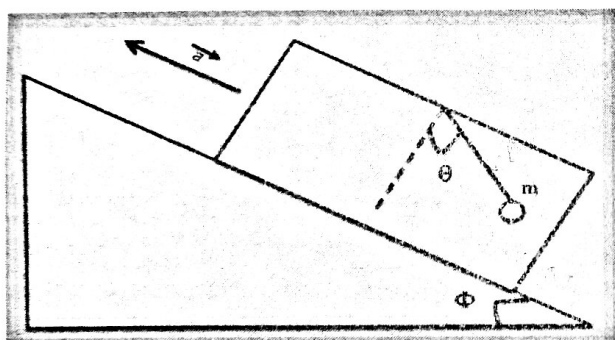
Quiz duration: 10 minutes

Name: Onur ARISEV

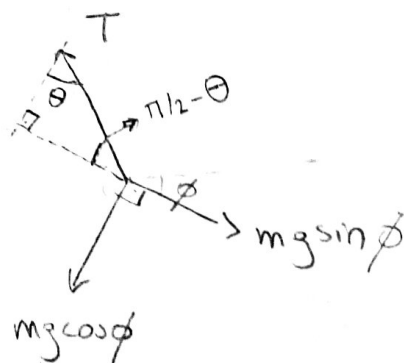
Student ID:

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A particle of mass m is suspended from the ceiling of a hollow block by a massless cord as shown in the figure. The block is pulled up a wedge that makes an angle Φ with the horizontal at a constant acceleration a . If the cord makes a constant angle θ the perpendicular to the ceiling, what is a in terms of Φ , θ and gravitational acceleration g .



Two forces act on the particle
The weight of the particle and the tension on the rope.



y-dir \rightarrow

$$T \sin\left(\frac{\pi}{2} - \theta\right) = mg \cos \Phi = T \cos(\theta)$$

x-dir \rightarrow

$$T \sin \theta - mg \sin \Phi = ma \quad (2)$$

(1) \rightarrow

$$T = \frac{mg \cos \Phi}{\cos \theta} \quad (3)$$

(3) \rightarrow (2)

$$\frac{mg \cos \Phi \sin \theta}{\cos \theta} - mg \sin \Phi = ma \Rightarrow a = g(\tan \theta \cos \Phi - \sin \Phi)$$

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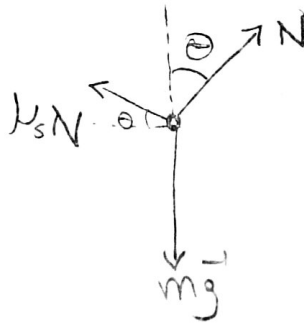
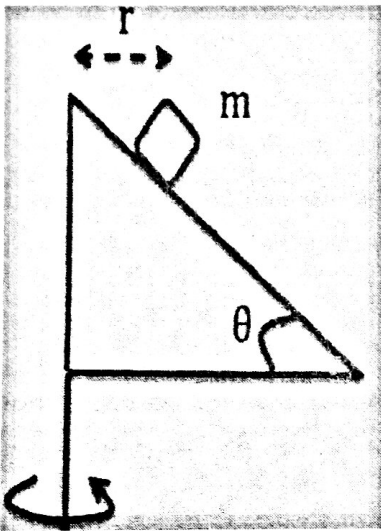
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A particle of mass m rotates, at a constant speed on a circle of radius r , on a wedge with static friction coefficient μ_s , firmly attached to a vertical rod rotating at a constant angular frequency ω . Find the condition on ω for which the particle remains at constant height.



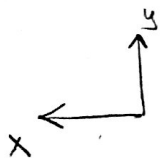
$$m\omega^2 r = \mu_s N \cos\theta - N \sin\theta$$

$$m\omega^2 r = N(\mu_s \cos\theta - \sin\theta) \quad (1)$$

$$N \cos\theta + \mu_s N \sin\theta = mg$$

$$N(\cos\theta + \mu_s \sin\theta) = mg \quad (2)$$

Centripetal acceleration in x-direction



Solve (2) for N and plug into (1)

$$m\omega^2 r = \frac{mg}{\cos\theta + \mu_s \sin\theta} (\mu_s \cos\theta - \sin\theta)$$

$$\omega = \sqrt{\frac{g}{r} \left(\frac{\mu_s \cos\theta - \sin\theta}{\mu_s \sin\theta + \cos\theta} \right)}$$

This is the maximum frequency possible so

$$\omega \leq \sqrt{\frac{g}{r} \left(\frac{\mu_s \cos\theta - \sin\theta}{\mu_s \sin\theta + \cos\theta} \right)}$$

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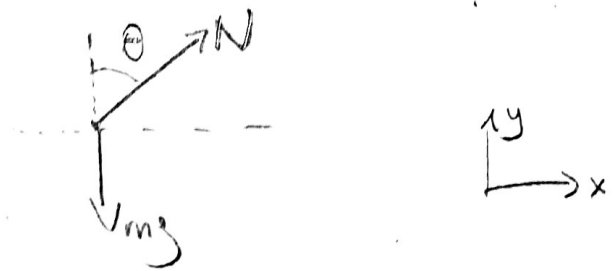
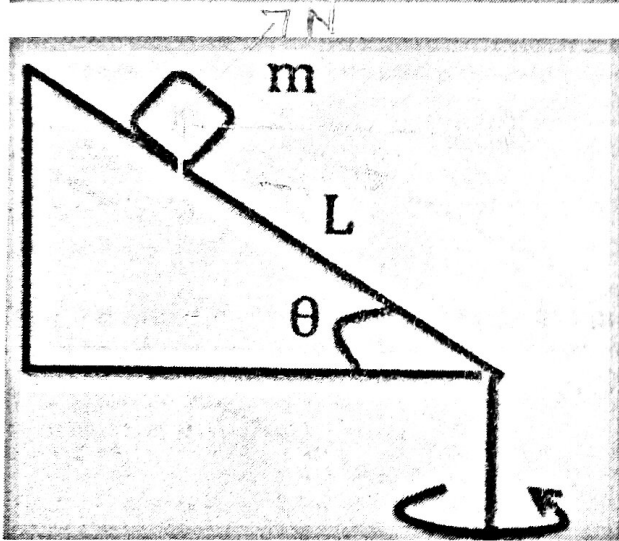
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A particle of mass m remains at a constant height on a frictionless wedge, firmly attached to a vertical rod rotating at a certain constant rate. Find the velocity of the particle in terms of the parameters θ , L shown in the figure and the gravitational acceleration g .



$$x\text{-dir} \rightarrow m\omega^2(L\cos\theta) = N\sin\theta \quad (1)$$

$$y\text{-dir} \rightarrow N\cos\theta = mg \Rightarrow N = \frac{mg}{\cos\theta} \quad (2)$$

$$m\omega^2(L\cos\theta) = mg\tan\theta$$

$$\frac{\omega^2}{L\cos\theta} = g\tan\theta$$

$$\omega^2 = gL\sin\theta$$

$$\omega = \sqrt{gL\sin\theta}$$