

Closed book. No calculators are to be used for this quiz.

Quiz duration: 10 minutes

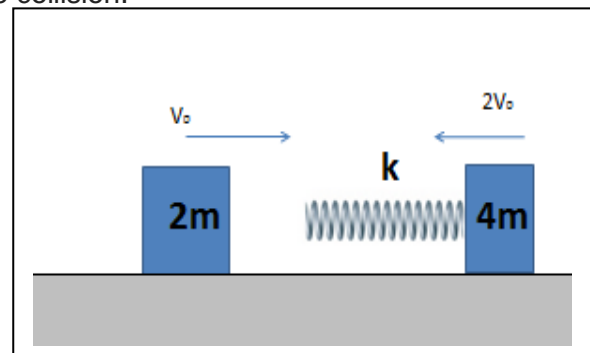
Name:

Student ID:

Signature:

A block of mass $2m$ moving to the right with a speed of V_0 on a frictionless surface collides with a light spring attached to a second block of mass $4m$ initially moving to the left with a speed of $2V_0$ as shown in Figure. The spring constant is k .

- Find the velocities of the two blocks when the spring reaches its maximum compression.
- Calculate the maximum compression of the spring.
- Find the velocities of the blocks after the collision.



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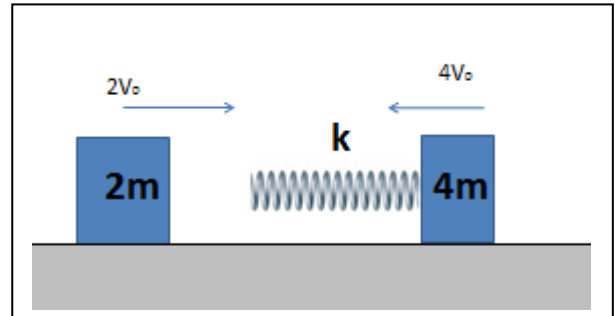
Name:

Student ID:

Signature:

A block of mass $2m$ moving to the right with a speed of $2V_0$ on a frictionless surface collides with a light spring attached to a second block of mass $4m$ initially moving to the left with a speed of $4V_0$ as shown in Figure. The spring constant is k .

- Find the velocities of the two blocks when the spring reaches its maximum compression.
- Calculate the maximum compression of the spring.
- Find the velocities of the blocks after the collision.



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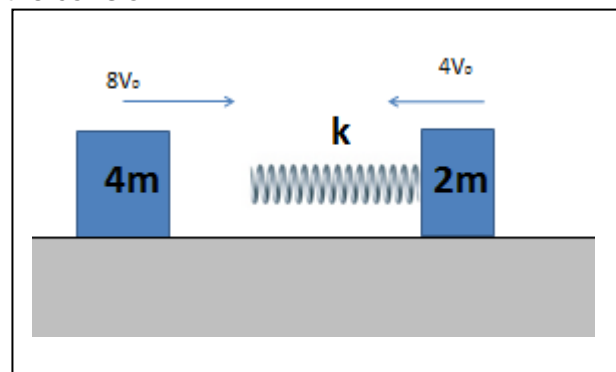
Name:

Student ID:

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A block of mass $4m$ moving to the right with a speed of $8V_0$ on a frictionless surface collides with a light spring attached to a second block of mass $2m$ initially moving to the left with a speed of $4V_0$ as shown in Figure. The spring constant is k .

- Find the velocities of the two blocks when the spring reaches its maximum compression.
- Calculate the maximum compression of the spring.
- Find the velocities of the blocks after the collision.



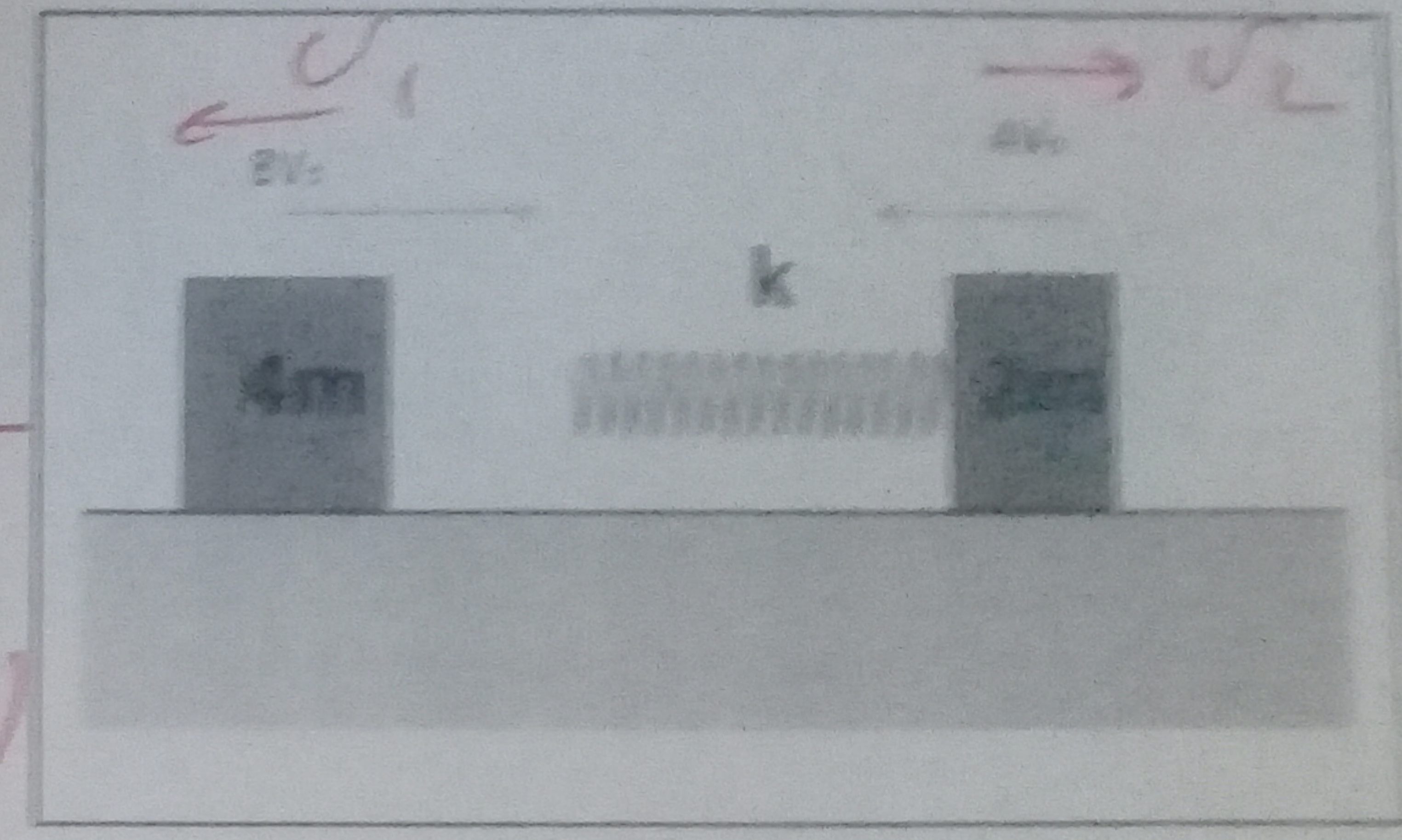
- b) Calculate the maximum compression of the spring
 c) Find the velocities of the blocks after the collision

a) they will have equal speed

momentum cons.:

$$-4m \cdot 8v_0 + 2m \cdot 4v_0 = (4m + 2m) v$$

$$v = -4v_0 \text{ (to the right)}$$



b) energy cons.:

$$\frac{1}{2} 4m (8v_0)^2 + \frac{1}{2} 2m (4v_0)^2 = \frac{1}{2} (4m + 2m) (-4v_0)^2 + \frac{1}{2} k x^2$$

$$\Rightarrow x^2 = \frac{192 m v_0^2}{k}$$

c) momentum cons. \Rightarrow

$$-24v_0 = 4v_1 - 2v_2$$

energy cons \Rightarrow

$$16k v_0^2 = 2v_1^2 + v_2^2$$

solutions

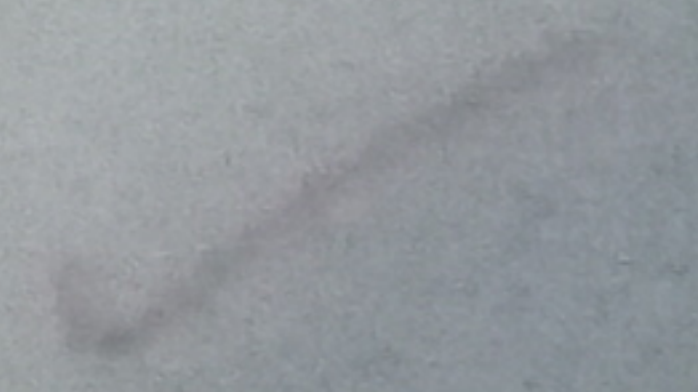
$$v_1 = -8v_0$$

$$v_2 = -4v_0$$

initial case

$$v_1 = 0$$

$$v_2 = 2v_0$$



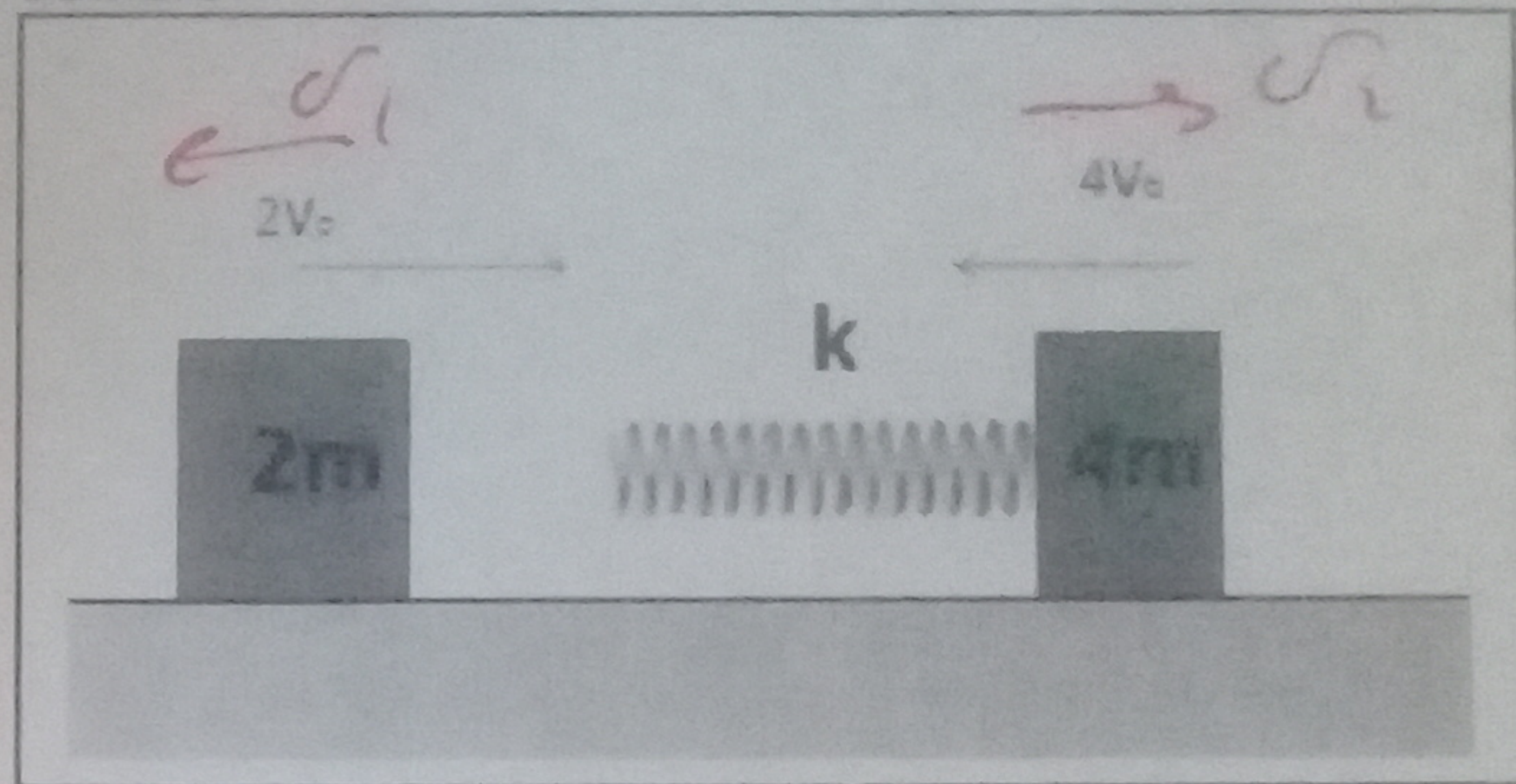
- 35 a) Find the velocities of the two blocks when the spring reaches its maximum compression.
- 35 b) Calculate the maximum compression of the spring.
- 30 c) Find the velocities of the blocks after the collision.

a) they will have equal speed.

momentum cons.:

$$-2m \cdot 2v_0 + 4m \cdot 4v_0 = (2m + 4m) v$$

$$v = 2v_0 \quad (\text{to the left})$$



b) Energy cons.:

$$\frac{1}{2} 2m (2v_0)^2 + \frac{1}{2} 4m (4v_0)^2 = \frac{1}{2} (2m + 4m) (2v_0)^2 + \frac{1}{2} kx^2$$

$$\Rightarrow x^2 = \frac{48m v_0^2}{k}$$

c) momentum cons. $\Rightarrow 2v_0 = 2v_1 - 4v_2$

energy cons. $\Rightarrow 36v_0^2 = v_1^2 + 2v_2^2$

solutions

$$\begin{aligned} v_1 &= -2v_0 \\ v_2 &= -4v_0 \end{aligned} \quad \text{initial case}$$

$$\begin{aligned} v_1 &= 6v_0 \\ v_2 &= 0 \end{aligned}$$

- 35 a) Find the velocity of the blocks at the maximum compression.
 35 b) Calculate the maximum compression of the spring.
 30 c) Find the velocities of the blocks after the collision.

a) they will have equal speed.
 momentum conservation leads to

$$-2m \cdot v_0 + 8m v_0 = (2m + 4m) v$$

$$v = +v_0 \quad (\text{to the left})$$

b) Energy conservation,

$$\frac{1}{2} \cdot 2m v_0^2 + \frac{1}{2} \cdot 4m (2v_0)^2 = \frac{1}{2} (2m + 4m) (+v_0)^2 + \frac{1}{2} k x^2$$

$$\Rightarrow x^2 = \frac{12m v_0^2}{k}$$

c) momentum cons. \Rightarrow

$$6v_0 = 2v_1 - 4v_2$$

energy

" \Rightarrow

$$9v_0^2 = v_1^2 + 2v_2^2$$

solutions

$$\begin{aligned} v_1 &= -v_0 \\ v_2 &= -2v_0 \end{aligned} \quad \text{initial case}$$

$$\begin{aligned} v_1 &= 3v_0 \\ v_2 &= 5v_0 \end{aligned} \quad \checkmark$$

