

Closed book. No calculators are to be used for this quiz.

Quiz duration: 10 minutes

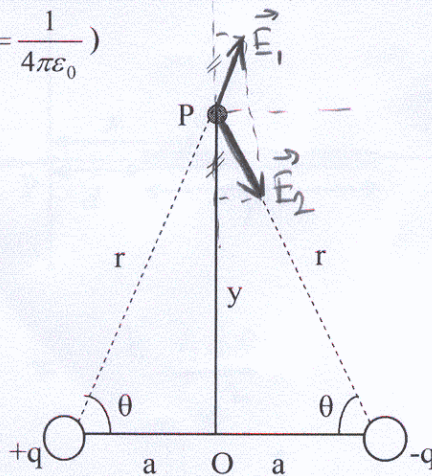
Name:

Student ID:

Signature:

An electric dipole consists of a positive charge q and a negative charge $-q$ separated by a distance $2a$ as in the figure. Find the electric field E due to these charges along the y -axis at the point P , which is a distance y from the origin. Express your answer in

terms of k , q , a , y . ($k = \frac{1}{4\pi\epsilon_0}$)



$$E_1 = E_2 = k \frac{q}{r^2} = k \frac{q}{y^2 + a^2}$$

$$E = 2E_1 \cos\theta = 2k \frac{q}{y^2 + a^2} \cdot \frac{y}{\sqrt{y^2 + a^2}} = \frac{2kqa}{(y^2 + a^2)^{3/2}}$$

$$y \gg a, \quad E = k \frac{2qa}{y^3}$$

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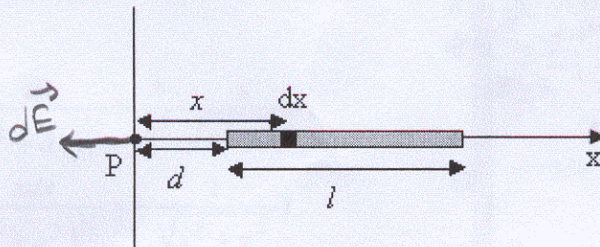
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A rod of length l has a uniform positive charge per unit length λ and a total charge Q . Calculate the electric field at a point P along the axis of the rod, a distance d from one end.

Express your answer in terms of k , Q , d , l . ($k = \frac{1}{4\pi\epsilon_0}$)



$$dE = k \frac{dq}{x^2} = k \frac{\lambda dx}{x^2}$$

$$E = k\lambda \int \frac{dx}{x^2} = k\lambda \left[-\frac{1}{x} \right]_d^{d+l}$$

$$E = k\lambda \left[\frac{1}{d} - \frac{1}{d+l} \right] = \frac{k\lambda l}{d(d+l)} = \frac{kQ}{d(d+l)}$$

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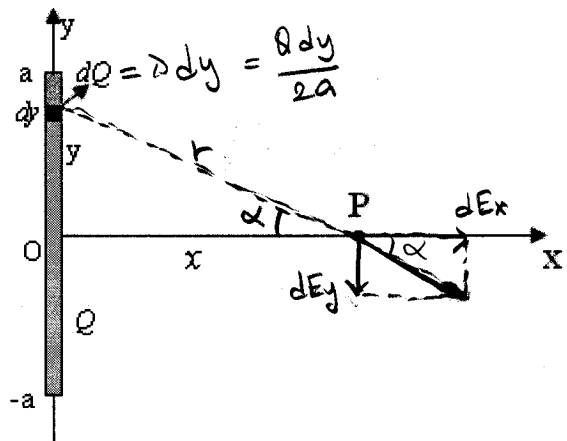
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Positive electric charge Q is distributed uniformly along a line with length $2a$, lying along the y -axis between $y=-a$ and $y=+a$. Find the magnitude and the direction of the electric field at a point P on the x -axis at a distance x from the origin. Express your

answer in terms of k, Q, x, a . ($k = \frac{1}{4\pi\epsilon_0}$)

Integrals: $\int \frac{dx}{(x^2 + a^2)^{3/2}} = \frac{1}{a^2} \frac{x}{\sqrt{x^2 + a^2}}$,
 $\int \frac{xdx}{(x^2 + a^2)^{3/2}} = -\frac{1}{\sqrt{x^2 + a^2}}$



$$dE_x = dE \cos \alpha,$$

$$dE_y = -dE \sin \alpha,$$

$$dE = k \frac{dQ}{r^2} = kQ \frac{dy}{2a(x^2 + y^2)}$$

$$\sin \alpha = \frac{y}{\sqrt{x^2 + y^2}}, \quad \cos \alpha = \frac{x}{\sqrt{x^2 + y^2}}$$

$$\Rightarrow dE_x = kQ \frac{x dy}{2a(x^2 + y^2)^{3/2}}$$

$$dE_y = -kQ \frac{y dy}{2a(x^2 + y^2)^{3/2}}$$

$$E_x = \frac{kQx}{2a} \int_{-a}^a \frac{dy}{(x^2 + y^2)^{3/2}} = kQ \frac{1}{x\sqrt{x^2 + a^2}}$$

$$E_y = -\frac{kQ}{2a} \int_{-a}^a \frac{y dy}{(x^2 + y^2)^{3/2}} = 0$$

$$\vec{E} = k \frac{Q}{x\sqrt{x^2 + a^2}} \hat{i}, \quad |\vec{E}| = \frac{kQ}{x\sqrt{x^2 + a^2}}$$

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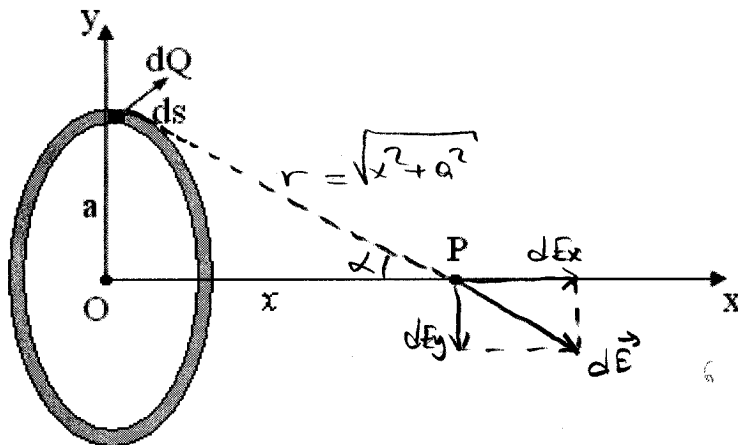
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A ring shaped conductor with radius a carries a total charge Q uniformly distributed around it. Find the magnitude and the direction of electric field at a point P that lies on the axis of the ring at a distance x from its center.

Express your answer in terms of k , Q , x , a . ($k = \frac{1}{4\pi\epsilon_0}$)



$$dE = k \frac{dQ}{r^2 + a^2}$$

By symmetry; $dE_y = 0$

$$dE_x = dE \cos \alpha, \quad \cos \alpha = \frac{x}{\sqrt{x^2 + a^2}}$$

$$dE_x = k \frac{dQ}{x^2 + a^2} \cdot \frac{x}{\sqrt{x^2 + a^2}} = k \frac{x dQ}{(x^2 + a^2)^{3/2}}$$

$$E_x = \int k \frac{x dQ}{(x^2 + a^2)^{3/2}} = k \frac{xQ}{(x^2 + a^2)^{3/2}}$$

$$\vec{E} = E_x \hat{i} = k \frac{xQ}{(x^2 + a^2)^{3/2}} \hat{i}$$

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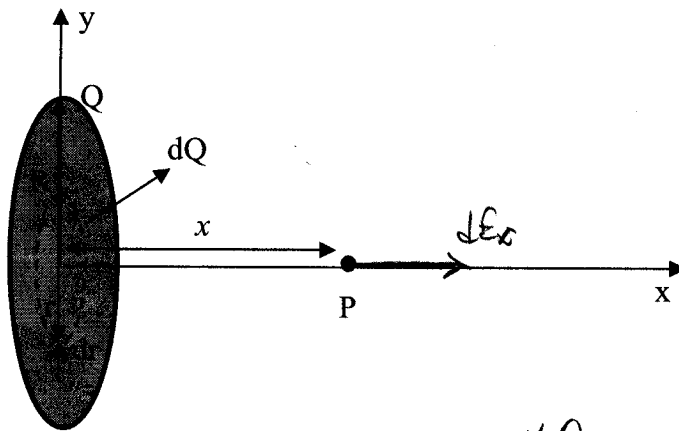
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Find the electric field caused by a disk of radius R with a uniform surface charge density σ (charge per unit area), at a point along the axis of the disk a distance x from its center. (Assume that x is positive) Express your answer in terms of σ , ϵ_0 , x , R .

Integrals: $\int \frac{dx}{(x^2 + a^2)^{3/2}} = \frac{1}{a^2} \frac{x}{\sqrt{x^2 + a^2}}$, $\int \frac{xdx}{(x^2 + a^2)^{3/2}} = -\frac{1}{\sqrt{x^2 + a^2}}$

(Hint: Electric field of a ring shaped conductor with total charge Q and radius a at a distance x from its center is $E_x = \frac{Q}{4\pi\epsilon_0} \frac{x}{(x^2 + a^2)^{3/2}}$)



for ring with radius $r \Rightarrow E_x = \frac{xQ}{4\pi\epsilon_0 (x^2 + r^2)^{3/2}} \Rightarrow$

For disk; $dA = 2\pi r dr$, $dQ = \sigma dA \Rightarrow dQ = 2\pi\sigma r dr$

$dE_x = \frac{1}{4\pi\epsilon_0} \frac{x \cdot 2\pi\sigma r dr}{(x^2 + r^2)^{3/2}}$, $dE_y = 0$, $dE_z = 0$ (By symmetry)

$\Rightarrow E_x = \int_0^R \frac{1}{4\pi\epsilon_0} \frac{(2\pi\sigma r dr) x}{(x^2 + r^2)^{3/2}}$

$E_x = \frac{\sigma x}{2\epsilon_0} \left[-\frac{1}{\sqrt{x^2 + R^2}} + \frac{1}{x} \right] = \frac{\sigma}{2\epsilon_0} \left[1 - \frac{1}{\sqrt{\frac{R^2}{x^2} + 1}} \right]$

$\vec{E} = E_x \hat{i} = \frac{\sigma}{2\epsilon_0} \left[1 - \frac{1}{\sqrt{\frac{R^2}{x^2} + 1}} \right] \hat{i}$, when $R \gg x$; $E_x = \frac{\sigma}{2\epsilon_0}$