

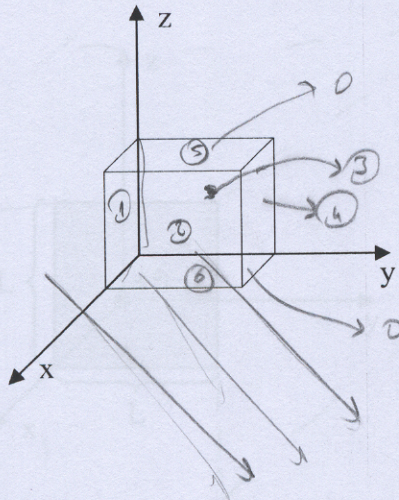
Closed book. No calculators are to be used for this quiz.
Quiz duration: 10 minutes

Name:

Student ID:

Signature:

A cube has sides of length L . It is placed with one corner at the origin as shown below. The electric field is uniform and given by $\vec{E} = -B\hat{i} + C\hat{j}$, where B , and C are positive constants. Find the total outward electric flux through the surface of the cube as a function of L , B , and C .



$$\Phi = \vec{E} \cdot \vec{A}$$

$$\vec{E} = -B\hat{i} + C\hat{j}$$

$$\vec{A} = A\hat{n}$$

$$① \vec{A}_1 = -L^2\hat{j}$$

$$\Phi_1 = \vec{E} \cdot \vec{A}_1 = (-B\hat{i} + C\hat{j}) \cdot (-L^2\hat{j}) = -CL^2$$

$$② \vec{A}_2 = L^2\hat{i}$$

$$\Phi_2 = (-B\hat{i} + C\hat{j}) \cdot (L^2\hat{i}) = -BL^2$$

$$③ \vec{A}_3 = -L^2\hat{i}$$

$$\Phi_3 = BL^2$$

$$④ \vec{A}_4 = L^2\hat{j} \Rightarrow \Phi_4 = CL^2$$

$$⑤ \vec{A}_5 = L^2\hat{k}, \vec{A}_6 = -L^2\hat{k} \Rightarrow \Phi_5 = \Phi_6 = 0$$

$$\Phi_{\text{Total}} = -CL^2 - BL^2 + BL^2 + CL^2 = 0$$

total electric flux through all sides is zero.

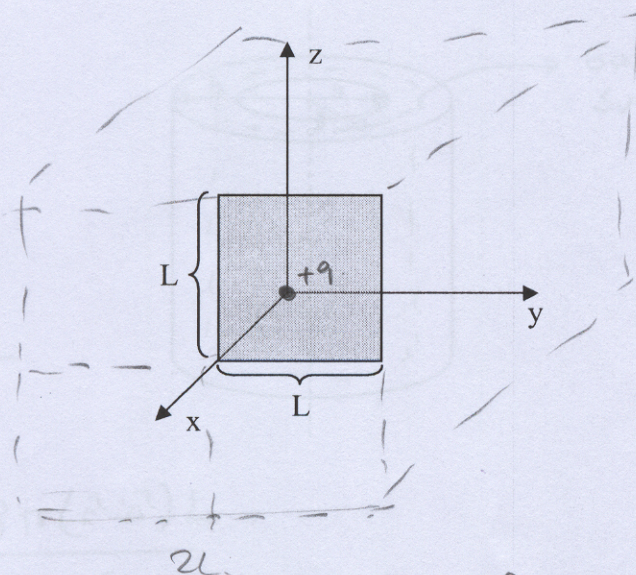
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A flat, square surface with sides of length L (shown below) is described by the equations $x = L$, $0 \leq y \leq L$, and $0 \leq z \leq L$. Find the electric flux through the square due to a positive point charge q located at the origin as a function of q and ϵ_0 . (Hint: Think of the square as part of a cube centered on the origin)



$$A_{\text{cube}} = 6(2L)^2 = 24L^2, \quad A_{\text{square}} = L^2 \Rightarrow A_{\text{square}} = \frac{A_{\text{cube}}}{24}$$

$$\text{for cube; } \Phi_E = \oint \vec{E} \cdot d\vec{A} = E \cdot A_{\text{cube}} = \frac{q_{\text{enc}}}{\epsilon_0} = \frac{q}{\epsilon_0}$$

$$\text{for square; } \Phi_E = E \cdot A_{\text{square}} = \frac{q}{\epsilon_0} \cdot \frac{1}{24} = \frac{q}{24\epsilon_0}$$

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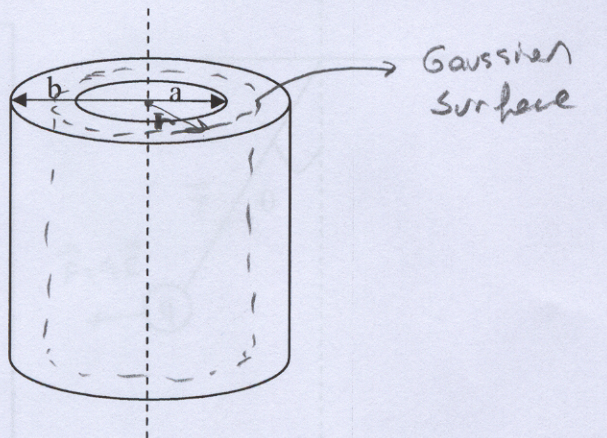
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A very long hollow cylinder with inner radius a and outer radius b has positive charge uniformly distributed throughout it, with charge per unit volume ρ . Derive the expression for the electric field inside the volume at a distance r from the axis of the cylinder ($a < r < b$).



$$\oint \vec{E} \cdot d\vec{A} = \frac{q_{enc}}{\epsilon_0}$$

$$q_{enc} = \rho \pi (r^2 - a^2) L$$

$$E \cdot 2\pi r L = \frac{\rho \pi (r^2 - a^2) L}{\epsilon_0}$$

$$E = \frac{\rho}{2\epsilon_0 r} (r^2 - a^2), \quad \vec{E} = \frac{\rho}{2\epsilon_0 r} (r^2 - a^2) \hat{r}$$

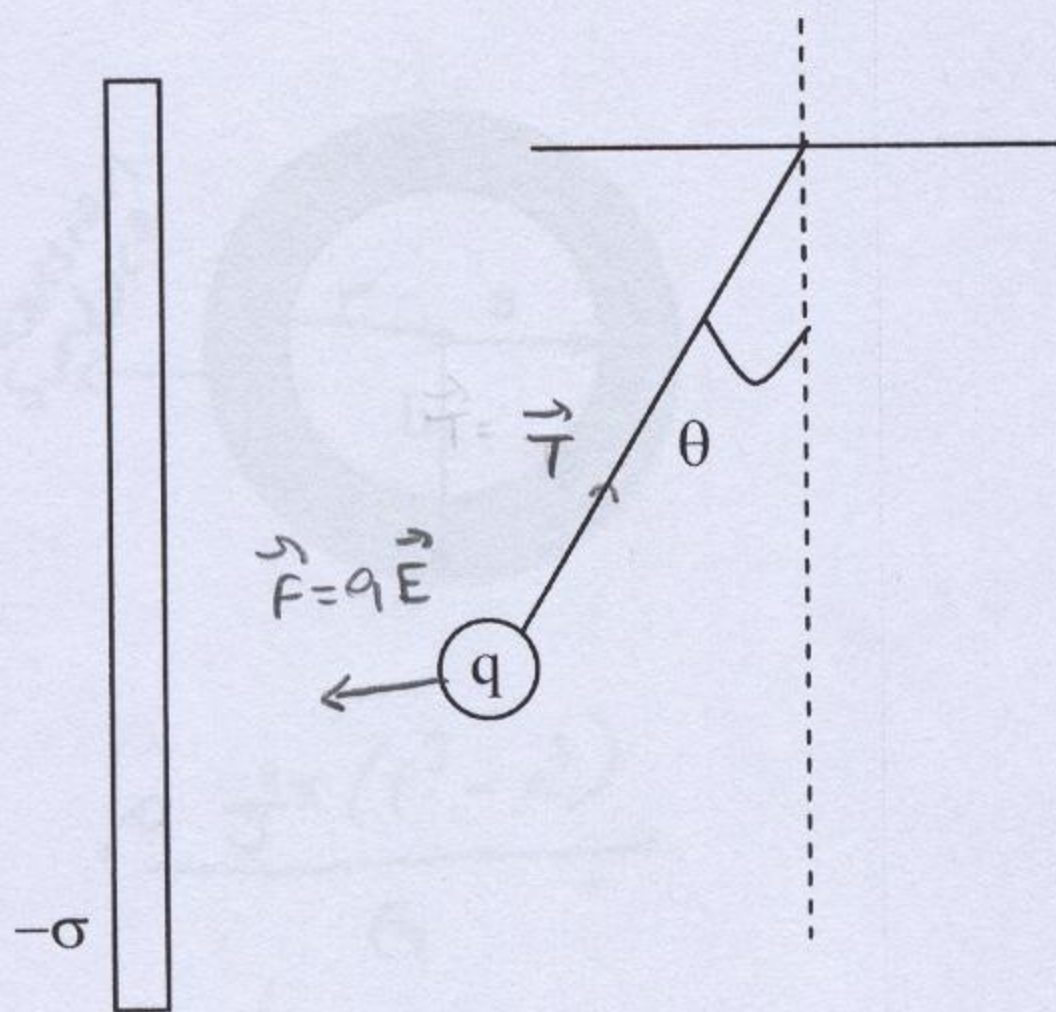
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A small sphere with a mass m and carrying a charge q hangs from a thread near a very large, charged conducting sheet as shown below. The charge density on the sheet is $-\sigma$. Find the angle of the thread as a function of m , g , q , σ , and ϵ_0 .



Forces act on the sphere are balanced;

$$\left. \begin{aligned} qE &= T \cdot \sin \theta \\ mg &= T \cdot \cos \theta \end{aligned} \right\} \tan \theta = \frac{qE}{mg} \Rightarrow \theta = \arctan \left(\frac{qE}{mg} \right)$$

Electric field for a sheet of charge;

$$E = \frac{\sigma}{2\epsilon_0} \Rightarrow \theta = \arctan \left(\frac{q\sigma}{2mg\epsilon_0} \right)$$

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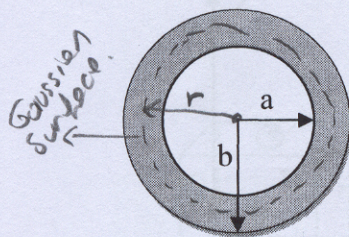
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An insulating spherical shell with inner radius a and outer radius b has positive charge uniformly distributed throughout it, with charge per unit volume ρ . Derive the expression for the electric field inside the volume at a distance r from the center of the sphere ($a < r < b$).

$$\oint \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0}$$

$$q_{enc} = \rho \frac{4}{3} \pi (r^3 - a^3)$$



$$\Rightarrow E 4\pi r^2 = \frac{\rho \frac{4}{3} \pi (r^3 - a^3)}{\epsilon_0}$$

$$E = \frac{\rho}{3\epsilon_0 r^2} (r^3 - a^3), \quad \vec{E} = \frac{\rho}{3\epsilon_0 r^2} (r^3 - a^3) \hat{r}$$