

Section 1

Quiz 1

17 February 2011

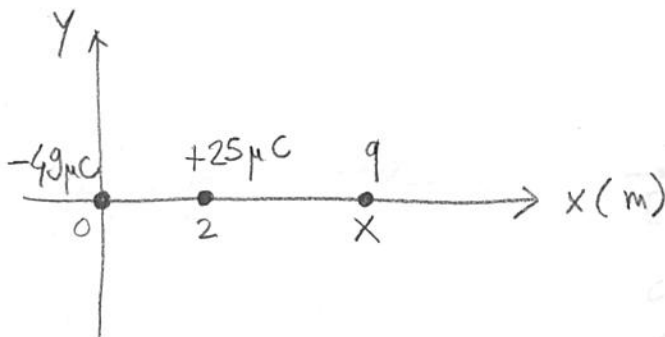
Closed book. No calculators are to be used for this quiz.
Quiz duration: 10 minutes

Name:

Student ID:

Signature:

Three charged particles are positioned on the x-axis. A positive charge ($25 \mu\text{C}$) is placed at $x=2\text{ m}$ and a negative charge ($-49 \mu\text{C}$) is positioned at the origin ($x=0$). Where on the positive x-axis must a third charge be placed so that the resultant force on it is zero?



$$k \frac{|(-49 \mu\text{C}) \cdot q|}{x^2} = k \frac{|(+25 \mu\text{C}) \cdot q|}{(x-2)^2}$$

$$\rightarrow x = 7 \text{ m}$$

Closed book. No calculators are to be used for this quiz.

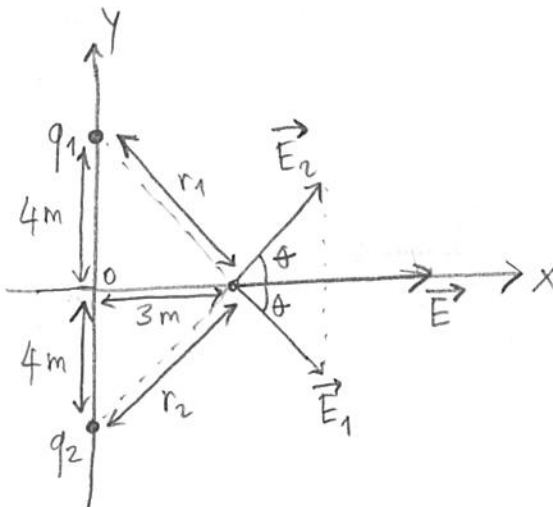
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Two identical $25 \times 10^{-8} \text{ C}$ charges are placed on the y-axis at $y = \pm 4 \text{ m}$. What is the electric field vector on the x-axis at $x = 3 \text{ m}$?



$$q_1 = q_2 = 25 \times 10^{-8} \text{ C}$$

$$\vec{E} = \vec{E}_1 + \vec{E}_2$$

$$\cos \theta = 0.6$$

$$\sin \theta = 0.8$$

$$E_1 = k \cdot \frac{q_1}{r_1^2} = k \cdot \frac{25 \times 10^{-8}}{25} = 10^{-8} \cdot k \text{ N/C}$$

$$E_2 = k \cdot \frac{q_2}{r_2^2} = k \cdot \frac{25 \times 10^{-8}}{25} = 10^{-8} \cdot k \text{ N/C}$$

$$E_{1x} = E_{2x} = E_1 \cdot \cos \theta = (10^{-8} \cdot k)(0.6) = 6 \times 10^{-9} \cdot k \text{ N/C}$$

$$\rightarrow E_x = E_{1x} + E_{2x} = 2E_{1x} = 1.2 \times 10^{-8} \cdot k \text{ N/C}$$

$$E_y = E_{1y} + E_{2y} = E_1 \cdot \sin \theta - E_2 \cdot \sin \theta = 0$$

$$\rightarrow E = E_x = 1.2 \times 10^{-8} \cdot k \text{ (in the } +x \text{ direction)}$$

$$= 108 \text{ N/C}$$

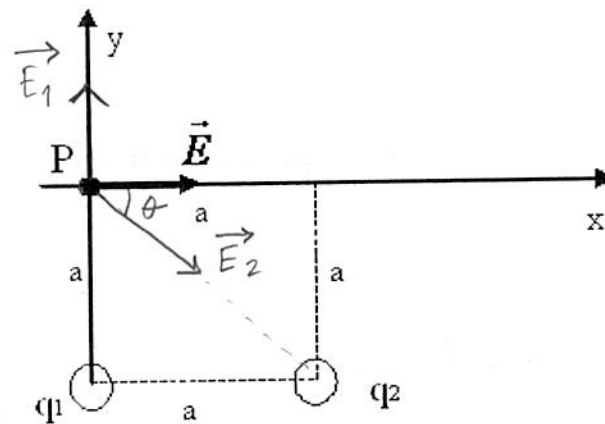
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Two point charges q_1 and q_2 are located at the corners of a square as in the figure. If the direction of the resultant electric field at point P is to the right, find the ratio (q_1/q_2) of the charges.



$$E_1 = k \frac{|q_1|}{a^2}, \quad E_2 = k \frac{|q_2|}{2a^2} \rightarrow |E_{2y}| = E_2 \cdot \sin \theta = \frac{k |q_2|}{2a^2} \cdot \frac{1}{\sqrt{2}}$$

$$E_y = 0 \rightarrow E_1 = |E_{2y}|$$

$$k \frac{|q_1|}{a^2} = k \frac{|q_2|}{2\sqrt{2}a^2}$$

$$\rightarrow \left| \frac{q_1}{q_2} \right| = \frac{1}{2\sqrt{2}}$$

• q_1 and q_2 are of opposite sign $\rightarrow \frac{q_1}{q_2} = -\frac{1}{2\sqrt{2}}$

Closed book. No calculators are to be used for this quiz.

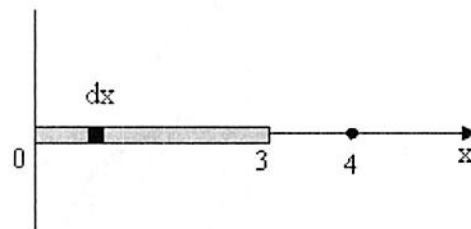
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A charge (uniform linear density = 8×10^{-9}) is distributed along the x-axis from $x=0$ to $x=3$ m. Determine the magnitude of the electric field at a point on the x-axis with $x=4$ m.



$$(\text{charge over } dx) = dq = (8 \times 10^{-9}) dx$$

$$(\text{electric field at } x=4\text{m due to } dq) = dE = k \frac{dq}{(4-x)^2} = k \frac{(8 \times 10^{-9}) dx}{(4-x)^2}$$

where x is the coordinate of dq

$$(\text{Total field at } x=4\text{m}) = E = \int dE = \int_0^3 k \frac{(8 \times 10^{-9}) dx}{(4-x)^2}$$

$$= k(8 \times 10^{-9}) \left[\frac{1}{4-x} \right]_0^3$$

$$= k(8 \times 10^{-9}) \left[1 - \frac{1}{4} \right]$$

$$= (6 \times 10^{-9}) k \text{ N/C}$$

$$= 54 \text{ N/C}$$

Closed book. No calculators are to be used for this quiz.

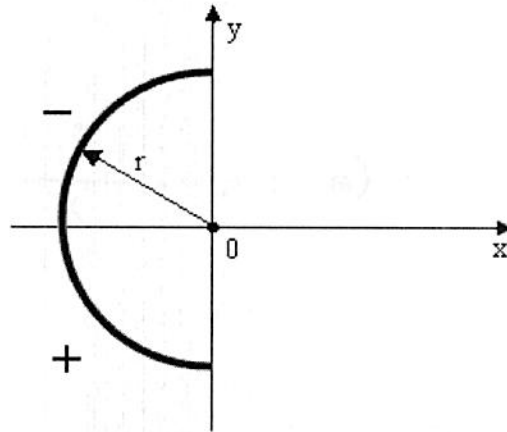
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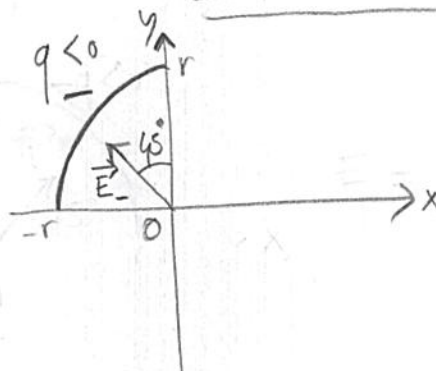
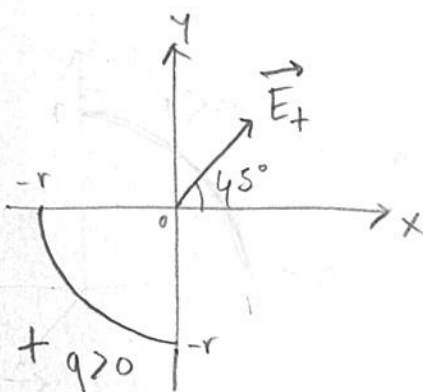
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A thin glass rod of length 15 cm is bent into a semicircle of radius $r=5$ cm. A charge $q=-7.5 \mu\text{C}$ is uniformly distributed along the upper half and a charge $q=+7.5 \mu\text{C}$ is uniformly distributed along the lower half as shown in the figure. Find the electric field vector at point 0.

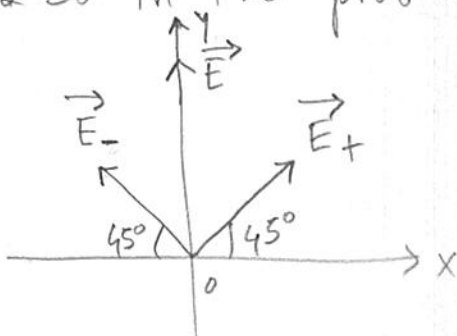


Electric field at the origin due to charge q distributed uniformly over a $\frac{1}{4}$ -circle:



$$(E_+)_{\cancel{y}} = (E_-)_{\cancel{y}} = \left(\frac{2}{\pi}\right) \frac{kq}{r^2}$$

So in the problem:



$$(E)_{\cancel{y}} = (E_+)_{\cancel{y}} = \left(\frac{2}{\pi}\right) k \frac{(7.5 \times 10^{-6})}{(0.05)^2} = \left(\frac{k}{\pi}\right) (6 \times 10^{-3}) \text{ N/C}$$

$$\vec{E} = \vec{E}_- + \vec{E}_+$$

$$\rightarrow E_x = 0, E_y = (E_-)_y + (E_+)_y = \left(\frac{12}{\pi} \times 10^{-3}\right) k \text{ N/C}$$

$$= \frac{12}{\pi} (3 \times 10^9) = 3.6 \times 10^7 \text{ N/C}$$