

Closed book. No calculators are to be used for this quiz.
Quiz duration: 15 minutes

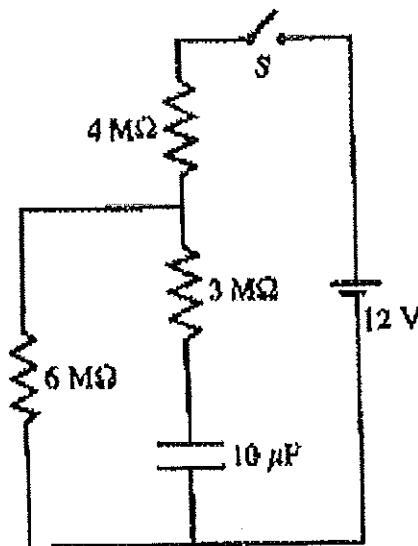
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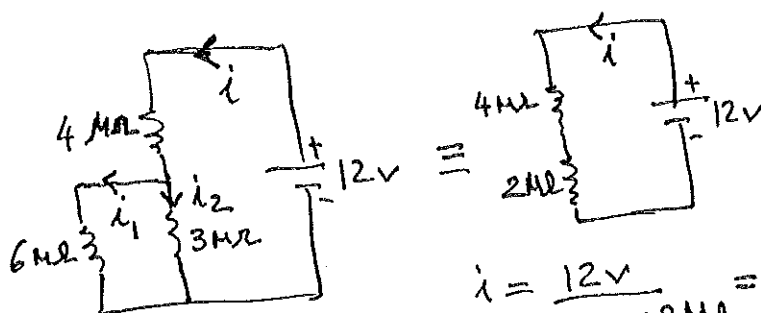
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The switch S in the given circuit is initially left open for a long time and then closed. Find the current through each resistor at the instant the switch S is closed.

($1\text{M}\Omega = 10^6\Omega$), ($1\mu\text{F} = 10^{-6}\text{F}$).



The capacitor is uncharged before the switch S is closed. So, it acts as a short circuit at the instant the switch S is closed. Circuit becomes



$$i = \frac{12\text{V}}{4\text{M}\Omega + 2\text{M}\Omega} = 2\mu\text{A}$$

$$i_1(6\text{M}\Omega) = i_2(3\text{M}\Omega)$$

$$2i_1 = i_2$$

$$i = i_1 + i_2 = 3i_1, \quad i_1 = \frac{i}{3}, \quad i_1 = \frac{2}{3}\mu\text{A}$$

$$i_2 = \frac{4}{3}\mu\text{A}$$

$$i_{4\text{M}\Omega} = 2\mu\text{A}$$

$$i_{6\text{M}\Omega} = \frac{2}{3}\mu\text{A}$$

$$i_{3\text{M}\Omega} = \frac{4}{3}\mu\text{A}$$

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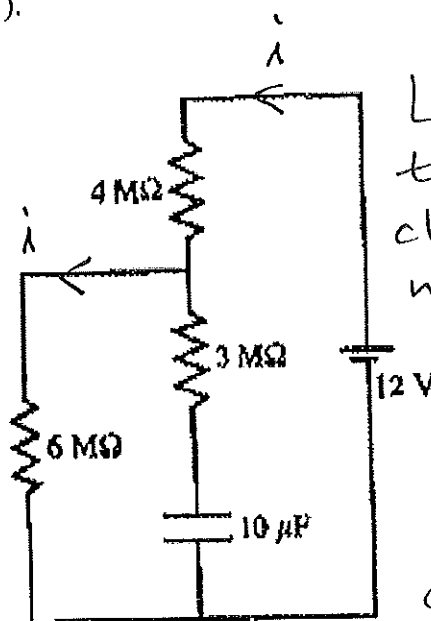
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In the circuit below, find the maximum charge on the capacitor.

($1\text{M}\Omega = 10^6\Omega$), ($1\mu\text{F} = 10^{-6}\text{F}$).



Long after S is closed the capacitor is fully charged and has the maximum charge.

No current flows through the $3\text{M}\Omega$ resistor and the capacitor.

Capacitor acts as an open circuit.

$$i = \frac{12\text{V}}{4\text{M}\Omega + 6\text{M}\Omega} = 1.2\ \mu\text{A}$$

$$V_C = i(6\text{M}\Omega) = (1.2\ \mu\text{A})(6\text{M}\Omega) = 7.2\ \text{V}$$

$$q = C V_C = (10\ \mu\text{F})(7.2\ \text{V}) = 72\ \mu\text{C}$$

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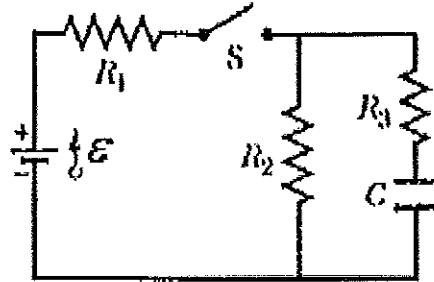
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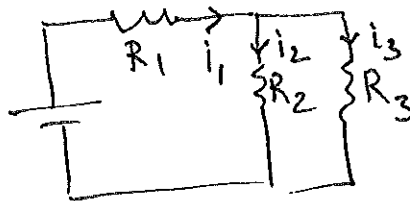
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In the circuit below, $\varepsilon = 1.2\text{kV}$, $C = 6.5\mu\text{F}$, $R_1 = R_2 = R_3 = 0.2\text{M}\Omega$. With C completely uncharged, switch S is suddenly closed (at $t=0$). Determine the currents I_1, I_2 and I_3 passing on the resistors R_1, R_2 and R_3 .

($1\text{M}\Omega = 10^6\Omega$), ($1\mu\text{F} = 10^{-6}\text{F}$).



At $t=0$



$$i_1 = i_2 + i_3$$

Loop rule applied to the left-hand loop;

$$\varepsilon - i_1 R_1 - i_2 R_2 = 0$$

to the right-hand loop;

$$i_2 R_2 - i_3 R_3 = 0$$

Resistances are all the same

$$R_1 = R_2 = R_3 = R$$

$$i_1 = \frac{2\varepsilon}{3R} = \frac{2}{3} \frac{1.2 \times 10^3 \text{V}}{0.2 \times 10^6 \Omega} = 4 \times 10^{-3} \text{A}$$

$$i_2 = i_3 = \frac{\varepsilon}{3R} = \frac{1}{3} \frac{1.2 \times 10^3 \text{V}}{0.2 \times 10^6 \Omega} = 2 \times 10^{-3} \text{A}$$

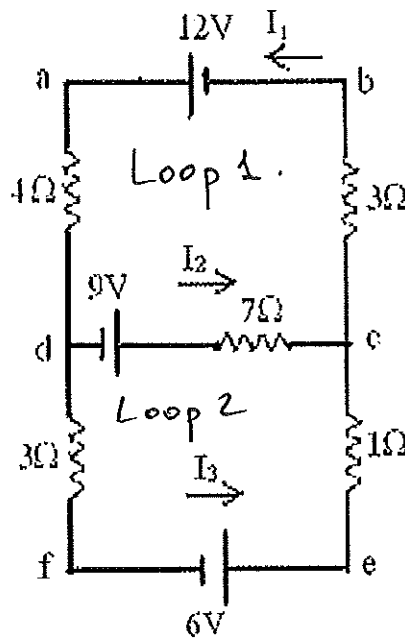
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In the circuit below, determine the current in each resistor.



$$I_1 = I_2 + I_3$$

Loop 1 :

$$9 - 7I_2 - 3I_1 + 12 - 4I_1 = 0$$

Loop 2 :

$$6 - 3I_3 - 1I_3 + 7I_2 - 9 = 0$$

$$21 - 7I_2 - 7I_1 = 0$$

$$-3 - 4I_3 + 7I_2 = 0$$

insert $I_2 = I_1 - I_3$

$$21 - 7(I_1 - I_3) - 7I_1 = 0$$

$$-3 - 4I_3 + 7(I_1 - I_3) = 0$$

$$21 - 14I_1 + 7I_3 = 0$$

$$-3 + 7I_1 - 11I_3 = 0$$

$$I_1 = 2 \text{ A}$$

$$I_2 = 1 \text{ A}$$

$$I_3 = 1 \text{ A}$$

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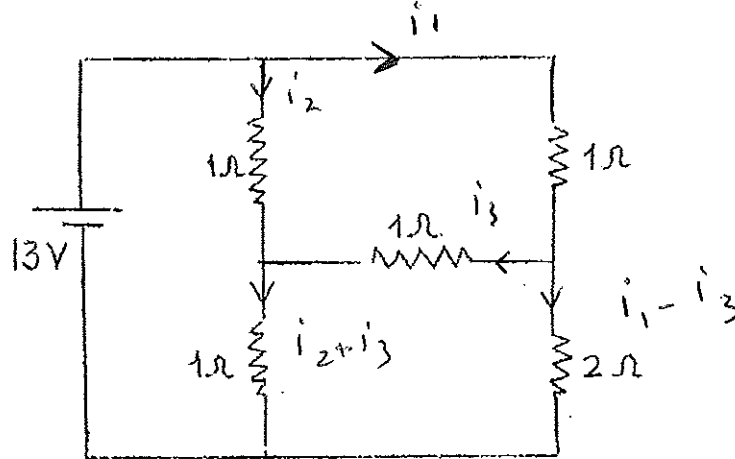
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In the circuit below, determine the current in each resistor.



$$-1i_1 - 1i_3 + 1i_2 = 0$$

$$\left. \begin{aligned} 1i_1 + 2(i_1 - i_3) &= 13 \\ 1i_2 + 1i_3 + 1i_2 &= 13 \end{aligned} \right\} \begin{aligned} i_1 - 2i_2 + 2i_1 - 2i_3 - i_3 &= 0 \\ \Rightarrow 3i_1 - 2i_2 - 3i_3 &= 0 \end{aligned}$$

$$3(i_2 - i_3) - 2i_2 - 3i_3 = 0$$

$$i_2 = 6i_3$$

$$i_3 = 1 \text{ A}$$

$$i_2 = 6 \text{ A}$$

$$i_1 = 5 \text{ A}$$

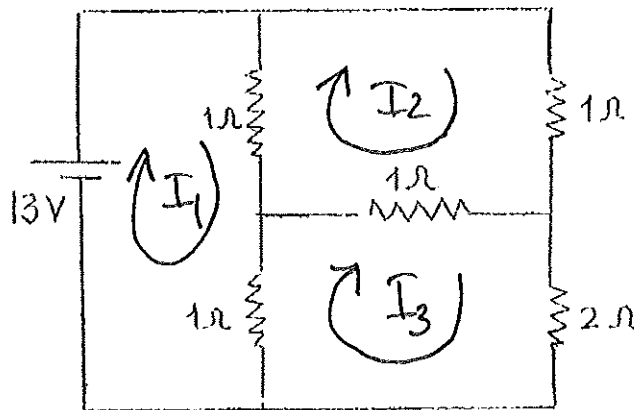
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In the circuit below, determine the current in each resistor.



Loop 1 :

$$13 - 1I_1 + 1I_2 - 1I_1 + 1I_3 = 0$$

Loop 2:

$$-1I_2 + 1I_1 - 1I_2 - 1I_2 + 1I_3 = 0$$

Loop 3 :

$$-1I_3 + 1I_1 - 1I_3 + 1I_2 - 2I_3 = 0$$

$$13 - 2I_1 + I_2 + I_3 = 0$$

$$I_1 - 3I_2 + I_3 = 0$$

$$I_1 + I_2 - 4I_3 = 0$$

$$\Delta = \begin{vmatrix} -2 & 1 & 1 \\ 1 & -3 & 1 \\ 1 & 1 & -4 \end{vmatrix} = -13$$

$$\Delta = -13$$

$$I_1 = \frac{1}{\Delta} \begin{vmatrix} -13 & 1 & 1 \\ 0 & -3 & 1 \\ 0 & 1 & -4 \end{vmatrix} = 11 \text{ A}$$

$$I_2 = \frac{1}{\Delta} \begin{vmatrix} -2 & -13 & 1 \\ 1 & 0 & 1 \\ 1 & 0 & -4 \end{vmatrix} = 5 \text{ A}$$

$$I_3 = \frac{1}{\Delta} \begin{vmatrix} -2 & 1 & -13 \\ 1 & -3 & 0 \\ 1 & 1 & 0 \end{vmatrix} = 4 \text{ A}$$

$$I_{1\Omega} = 11 - 5 = 6 \text{ A} \checkmark$$

$$I_{1\Omega} = I_1 - I_3 = 11 - 4 = 7 \text{ A} \checkmark$$

$$I_{1\Omega} = I_2 = 5 \text{ A} \checkmark$$

$$I_{1\Omega} = I_2 - I_3 = 5 - 4 = 1 \text{ A} \checkmark$$

$$I_{2\Omega} = 4 \text{ A} \checkmark$$