

Closed book. No calculators are to be used for this quiz.
Quiz duration: 10 minutes

Name:

Student ID:

Signature:

A circuit is composed of a single loop with an alternating current source $V(t) = V_0 \sin(\omega t)$, a capacitor C and a resistor R . Derive the current $I(t)$ as a function of (V_0, ω, t, C, R) .

$$V(t) = V_0 \cos(\omega t - \frac{\pi}{2})$$

$$I(t) = I_0 \cos(\omega t)$$

$$I_0 = \frac{V_0}{Z} = \frac{V_0}{\sqrt{R^2 + \frac{1}{\omega^2 C^2}}}$$

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A circuit is composed of a single loop with an alternating current source $V(t) = V_0 \sin(\omega t)$, an inductor, a capacitor C and a resistor R . The resultant current is $I(t) = I_0 \sin(\omega t + \pi/4)$, and $X = \omega L = 1/4 \omega C$.

(a) What is the resistance in terms of X ?

(b) Completely determine the characteristic of this circuit element in terms of V_0 , I_0 , ω , t , X , L and C . (all of these will not be necessary).

$$V(t) = V_0 \sin(\omega t)$$

$$I = I_0 \sin(\omega t + \frac{\pi}{4}) \quad , \quad X = \omega L = \frac{1}{4\omega C}$$

$$\begin{aligned} \tan \phi &= \frac{X_L - X_C}{R} \Rightarrow R = \frac{\frac{1}{4\omega C} - \frac{1}{\omega C}}{\tan \phi} \\ &= \frac{-\frac{3}{4\omega C}}{\tan(-\frac{\pi}{4})} \Rightarrow R = \frac{3}{4\omega C} \end{aligned}$$

$$Z = R \cos \phi \Rightarrow Z = \sqrt{2} R$$

$$V_L = I_0 X_L = \frac{I_0}{4\omega C}$$

$$V_C = I_0 X_C = \frac{I_0}{\omega C}$$

$$V_R = I_0 R = \frac{3I_0}{4\omega C}$$

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A circuit is composed of a single loop with an alternating current source

$V(t) = V_0 \cos(\omega t)$, and an unknown element. If the resultant current is

$I(t) = \frac{V_0}{R} \cos(\omega t - \pi/2)$, identify the unknown element and plot the current passing through this element together with the potential difference.

$$\frac{V_0}{Z} = \frac{V_0}{R} \Rightarrow Z = R \Rightarrow X_L = X_C = 0$$

It contains just Inductor

$$V_0 = \bar{I} X_L \Rightarrow \bar{I} = \frac{V_0}{\omega L}$$

$$\bar{I} = \frac{V_0}{\omega L} \cos(\omega t - \frac{\pi}{2})$$

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A circuit is composed of a single loop with an alternating current source

$V(t) = V_0 \sin(\omega t)$, an inductor L and a resistor R . Derive the power $P(t)$ obtained from the alternating current source as a function of (V_0, ω, t, L, R) .

$$V = V_0 \sin(\omega t), \quad I = I_0 \sin(\omega t - \phi)$$

$$\tan \phi = \frac{\omega L}{R}, \quad \phi = \tan^{-1} \frac{\omega L}{R}$$

$$P(t) = i(t) V(t) = I_0 V_0 \sin(\omega t) \sin\left(\omega t - \tan^{-1} \frac{\omega L}{R}\right)$$

$$I_0 = \frac{V_0}{Z} = \frac{V_0}{\sqrt{R^2 + \omega^2 L^2}}$$

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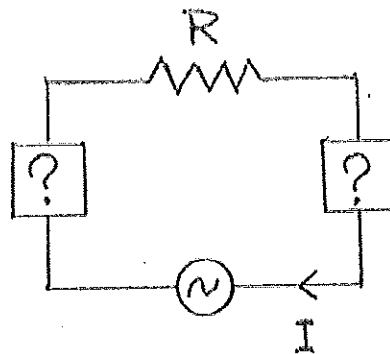
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A circuit is composed of a single loop with an alternating current source

$V(t) = V_0 \sin(\omega t)$, two unknown circuit elements and a resistor R .

The current is $I(t) = I_0 \sin(\omega t - \pi/3)$.



(a) What are the circuit elements in the boxes with the question marks?

(b) Determine I_0 in terms of (V_0, R, ω, t) (all of these may not be necessary).

Inductor + capacitor

$$V(t) = V_0 \sin(\omega t), \quad I(t) = I_0 \sin(\omega t - \frac{\pi}{3})$$

$$\tan\left(\frac{\pi}{3}\right) = \frac{X_L - X_C}{R} \Rightarrow X_L - X_C = \sqrt{3} R$$

$$V_0 = I_0 Z \Rightarrow I_0 = \frac{V_0}{\sqrt{R^2 + (X_L - X_C)^2}} = \frac{V_0}{2R}$$