

Section 1

Quiz 7

28 March 2013

Closed book. No calculators are to be used for this quiz.

Quiz duration: 10 minutes

Name:

Student ID:

Signature:

An open plastic soda bottle with an opening diameter of 3 cm is placed on a table. A uniform 2.25 T magnetic field directed upward and oriented 37° from vertical encompasses the bottle.

What is the total magnetic flux through the plastic of the soda bottle?

($\cos 37^\circ = 0.8$, $\sin 37^\circ = 0.6$. Take $\pi = 3$)

Solution: The total flux through the bottle is zero because it is a closed surface. The total flux is the flux through the plastic and plus the flux through the open cap, so the sum of these must be zero. $\Phi_{\text{plastic}} + \Phi_{\text{cap}} = 0$

$$\Phi_{\text{plastic}} = -\Phi_{\text{cap}} = -BA \cos \phi = -B(\pi r^2) \cos \phi$$

by substituting the numbers gives $\Phi_{\text{plastic}} = -(2.25)\pi(0.015 \text{ m})^2 \cos 37^\circ$

$$\Rightarrow \Phi_{\text{plastic}} = 1.215 \times 10^{-3} \text{ Wb}$$

It would be difficult to calculate the flux through the plastic directly, because of the complex shape of the bottle, but with a little thought we can find this flux through a simple calculation.

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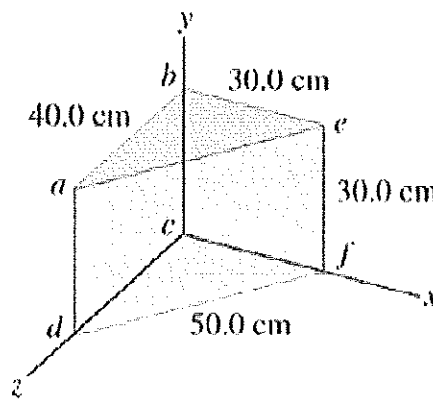
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The magnetic field \vec{B} in a certain region is 0.200 T , and its direction is that of the $+z$ axis as shown in the figure.

- What is the magnetic flux across the surface abcd in the figure?
- What is the magnetic flux across befc?
- What is the magnetic flux across the surface aefd?
- What is the net flux through all five surfaces that enclose the shaded volume?



Solution: When \vec{B} is uniform across the surface, $\Phi_B = \vec{B} \cdot \vec{A}$

$\Phi_B = \vec{B} \cdot \vec{A} = BA \cos \phi$. \vec{A} is normal to the surface and is directed outward from the enclosed surface. For surface abcd, $\vec{A} = -A \hat{i}$.

For surface befc, $\vec{A} = -A \hat{k}$. For surface aefd, $\cos \phi = \frac{3}{5}$ and the flux is positive.

$$\text{part a) } \Phi_B(\text{abcd}) = \vec{B} \cdot \vec{A} = 0$$

$$\text{part b) } \Phi_B = \vec{B} \cdot \vec{A} = -(0.2\text{ T})(0.300\text{ m})^2 = -0.018\text{ Wb}$$

$$\text{part c) } \Phi_B(\text{aefd}) = \vec{B} \cdot \vec{A} = BA \cos \phi = \frac{3}{5} (0.2\text{ T})(0.500)(0.300) = +0.018\text{ Wb}$$

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A flat square surface with side length 6.10 cm is in the xy -plane at $z=0$. Calculate the magnitude of the flux through this surface produced by a magnetic field

$$\vec{B} = (0.400T)\hat{i} + (0.100T)\hat{j} - (0.200T)\hat{k}.$$

Solution: Knowing the area of a surface and the magnetic field it is in, we want to calculate the flux through it.

$$d\vec{A} = dA\hat{k}, \text{ so } d\Phi_B = \vec{B} \cdot d\vec{A} = B_z dA$$

$$\Phi_B = B_z A = (-0.200T)(0.0610 \text{ m})^2 = -7.44 \times 10^{-4} \text{ T}\cdot\text{m}^2.$$

$$|\Phi_B| = 7.44 \times 10^{-4} \text{ Wb}$$

Since the field is uniform over the surface, it is not necessary to integrate to find the flux.

Section 4

Quiz 7

28 March 2013

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Quiz duration: 10 minutes

Name:

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A group of particles is traveling in magnetic field of unknown magnetic and direction. You observe that a proton moving at 1.00 km/s in the $+x$ -direction experience a force of $2.00 \times 10^{-16} \text{ N}$ in the $+y$ -direction, and an electron moving at 4.50 km/s in the $-z$ -direction experiences a force of $8.00 \times 10^{-16} \text{ N}$ in the $+y$ -direction.

(a) What are the magnitude and direction of the magnetic field?

(b) What are the magnitude and direction of the magnetic force on an electron on an electron moving in the $-y$ -direction at 3.00 km/s ? ($e = 1.60 \times 10^{-19} \text{ C}$)

Solution: apply $\vec{F} = q\vec{v} \times \vec{B}$ to the force on the proton and to the force on the electron, solve for the components of \vec{B} and use them to find its magnitude and direction.

\vec{F} is perpendicular to both \vec{v} and \vec{B} . since the force on the proton is in the $+y$ -direction,

$B_y = 0$ and $\vec{B} = B_x \hat{i} + B_z \hat{k}$. for the proton, $\vec{v}_p = (1 \text{ km/s}) \hat{i} = v_p \hat{i}$ and $\vec{F}_p = (2 \times 10^{-16} \text{ N}) \hat{j} = F_p \hat{j}$.

for the electron, $\vec{v}_e = (4.50 \text{ km/s}) \hat{k} = -v_e \hat{k}$ and $\vec{F}_e = (8 \times 10^{-16} \text{ N}) \hat{j} = F_e \hat{j}$. The magnetic

force is $\vec{F} = q\vec{v} \times \vec{B}$

part a) for the proton, $\vec{F}_p = q\vec{v}_p \times \vec{B}$ gives $F_p \hat{j} = ev_p \hat{i} \times (B_x \hat{i} + B_z \hat{k}) = -ev_p B_z \hat{j}$. solving for

B_z gives $B_z = -\frac{F_p}{ev_p} = -\frac{2 \times 10^{-16} \text{ N}}{(1.60 \times 10^{-19} \text{ C})(1000 \text{ m/s})} = -1.25 \text{ T}$. For electron, $\vec{F}_e = -e\vec{v}_e \times \vec{B}$,

which gives $F_e \hat{j} = (-e)(-v_e \hat{k}) \times (B_x \hat{i} + B_z \hat{k}) = ev_e B_x \hat{j}$. solving for B_x gives $B_x = \frac{F_e}{ev_e}$

$B_x = \frac{F_e}{ev_e} = \frac{8 \times 10^{-16}}{(1.60 \times 10^{-19} \text{ C})(4500 \text{ m/s})} = 1.111 \text{ T}$. Therefore $\vec{B} = 1.111 \text{ T} \hat{i} - 1.25 \text{ T} \hat{k}$. so the

magnitude of the field is $B = \sqrt{B_x^2 + B_z^2} = \sqrt{(1.111 \text{ T})^2 + (-1.25 \text{ T})^2} = 1.63 \text{ T}$

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A particle with charge $7.00\mu\text{C}$ is moving with velocity $\vec{v} = -(3.00 \times 10^3 \text{ m/s}) \hat{j}$. The

magnetic force on the particle is measured to be $\vec{F} = +(7.00 \times 10^{-3} \text{ N}) \hat{i} - (5.00 \times 10^{-3} \text{ N}) \hat{k}$.

(a) Calculate all the components of the magnetic field you can from this information.

(b) Are there components of the magnetic field that are not determined by the measurement of the force? Explain.

(c) Calculate the scalar product $\vec{B} \cdot \vec{F}$. What is the angle between \vec{B} and \vec{F} ?

Solution: First apply $\vec{F} = q\vec{v} \times \vec{B}$

set up: $\vec{v} = v_y \hat{j}$, with $v_y = -3.00 \times 10^3 \text{ m/s}$ and $F_x = 7.00 \times 10^{-3} \text{ N}$, $F_y = 0$

and $F_z = -5.00 \times 10^{-3} \text{ N}$

$$\text{part a) } F_x = q(v_y B_z - v_z B_y) = qv_y B_z \implies B_z = \frac{F_x}{qv_y}$$

$$\text{so } B_z = \frac{(7 \times 10^{-3} \text{ N})}{[(7 \times 10^{-6} \text{ C})(-3 \times 10^3 \text{ m/s})]} = -0.333 \text{ T}$$

$F_y = q(v_z B_x - v_x B_z) = 0$, which is consistent with \vec{F} as given in the problem. There is no force component along the direction of the velocity.

$$F_z = q(v_x B_y - v_y B_x) = -qv_y B_x = -\frac{F_z}{qv_y} \implies B_x = -\frac{F_z}{qv_y} = -\frac{(-5 \times 10^{-3} \text{ N})}{[(7 \times 10^{-6} \text{ C})(-3 \times 10^3 \text{ m/s})]}$$

$$\implies B_x = -0.238 \text{ T}$$

College of Arts and Sciences

Section 6

Quiz 7

28 March 2013

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Quiz duration: 10 minutes

Name:

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A particle with charge -5.00 nC is moving in a uniform magnetic field $\vec{B} = -(1.50 \text{ T})\hat{k}$. The magnetic force on the particle is measured to be $\vec{F} = -(3.00 \times 10^{-7} \text{ N})\hat{i} + (7.00 \times 10^{-7} \text{ N})\hat{j}$.

(a) Calculate all the components of the velocity of the particle that you can from this information.

(b) Are there components of the velocity that are not determined by the measurement of the force? Explain.

(c) Calculate the scalar product $\vec{v} \cdot \vec{F}$. What is the angle between \vec{v} and \vec{F} ?

$$\text{solution: } \vec{F} = q\vec{v} \times \vec{B} = qB_z [v_x(\hat{i} \times \hat{k}) + v_y(\hat{j} \times \hat{k}) + v_z(\hat{k} \times \hat{k})] = qB_z [v_x(-\hat{j}) + v_y(\hat{i})]$$

part a) set the expression for \vec{F} equal to the given value of \vec{F} to obtain:

$$v_x = \frac{F_y}{-qB_z} = \frac{(7 \times 10^{-7} \text{ N})}{-(-5 \times 10^{-9} \text{ C})(-1.50 \text{ T})} = -93.3 \frac{\text{m}}{\text{s}}$$

$$v_y = \frac{F_x}{qB_z} = \frac{-(3 \times 10^{-7} \text{ N})}{(-5 \times 10^{-9} \text{ C})(-1.5 \text{ T})} = -40 \frac{\text{m}}{\text{s}}$$

part b) v_z does not contribute to the force, so is not determined by a measurement of \vec{F} .

$$\text{part c) } \vec{v} \cdot \vec{F} = v_x F_x + v_y F_y + v_z F_z = \frac{F_y}{-qB_z} F_x + \frac{F_x}{+qB_z} F_y = 0 \Rightarrow \theta = 90^\circ$$

So easily we can know the force is perpendicular to both \vec{v} and \vec{B}