

Closed book. No calculators are to be used for this quiz.

Quiz duration: 10 minutes

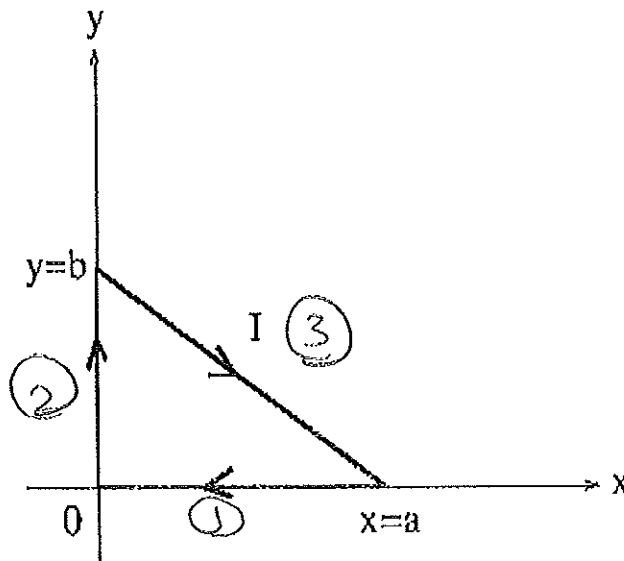
Name:

Student ID:

Signature:

If the current carrying loop shown in the figure is under a varying magnetic field given by

$\vec{B} = B_0 xy \hat{j}$, calculate the total magnetic force on the loop.



$$d\vec{F} = I d\vec{l} \times \vec{B}$$

$$\textcircled{1} \Rightarrow \vec{F} = \int_{x=0, y=0}^0 I dx \hat{i} \times B_0 xy \hat{j} = 0$$

$$\textcircled{2} \Rightarrow \vec{F} = \int_{x=0, y=0}^b I dy \hat{j} \times B_0 xy \hat{j} = 0$$

$$\textcircled{3} \Rightarrow x = t, \quad y = \frac{b}{a}(a-t)$$

$$\int_{t=0}^0 I dt \left(\hat{i} - \frac{b}{a} \hat{j} \right) \times B_0 \frac{tb}{a} (a-t) \hat{j}$$

$$= \int_{t=0}^0 I dt B_0 \frac{tb}{a} (a-t) \hat{k} = \frac{B_0 b a^2}{6} \hat{k}$$

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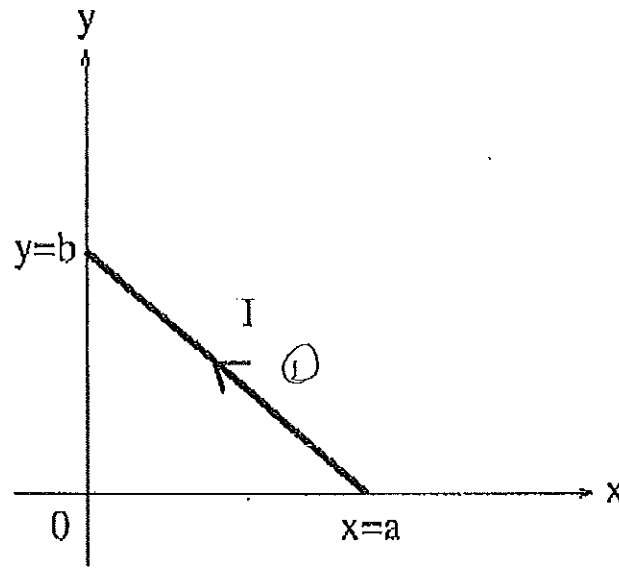
Name:

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If the current carrying loop shown in the figure is under a varying magnetic field given by

$\vec{B} = B_0(x\hat{i} + y\hat{j})$, calculate the total magnetic force.



$$d\vec{F} = I d\vec{l} \times \vec{B}$$

① $x + \frac{a}{b}y = a \Rightarrow \begin{matrix} x = t \\ y = (a-t)\frac{b}{a} \end{matrix} \Rightarrow d\vec{l} = dx\hat{i} + dy\hat{j} = dt(\hat{i} - \frac{b}{a}\hat{j})$

$$\int_a^0 I dt (\hat{i} - \frac{b}{a}\hat{j}) \times B_0 (t\hat{i} + (a-t)\frac{b}{a}\hat{j}) = \int_a^0 I B_0 (a-t)\frac{b}{a} + t\frac{b}{a} \hat{k} dt$$

$$= I B_0 (bt - \frac{t^2 b}{2a} + t^2 \frac{b}{2a}) \Big|_a^0 \hat{k}$$

$$= -I B_0 b a \hat{k}$$

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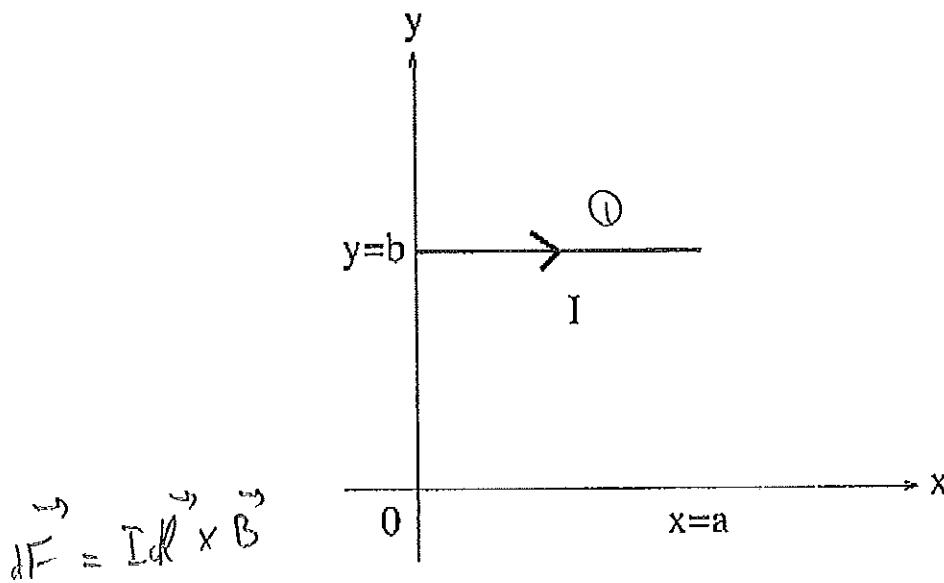
Name:

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If the current carrying wire shown in the figure is under a varying magnetic field given by

$\vec{B} = B_0 xy \hat{k}$, calculate the total magnetic force.



$$\textcircled{1} \vec{F} = \int_{x=0, y=b}^a I dx \hat{i} \times B_0 xy \hat{k} = -B_0 b I \frac{a^2}{2} \hat{j}$$

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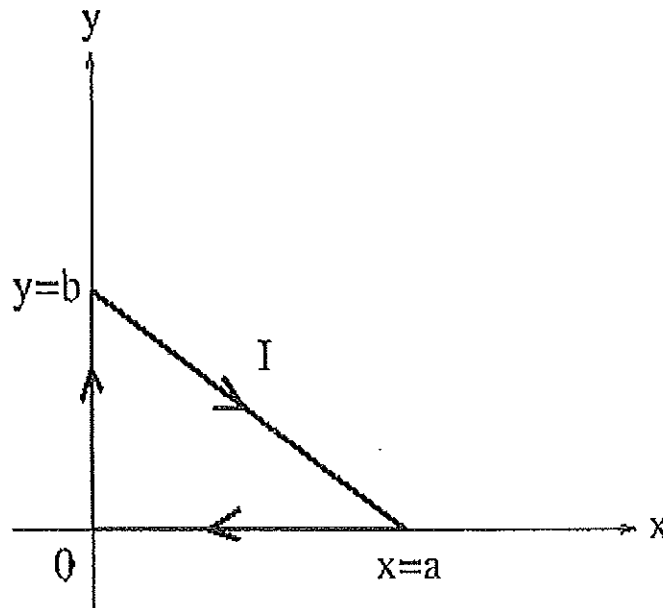
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If the current carrying loop shown in the figure is under a uniform magnetic field

$\vec{B} = B_0(2\hat{i} - \hat{k})$, calculate the total torque caused by the magnetic force.



The total \vec{F} is equal zero because the magnetic field is homogeneous.

$$\vec{\tau} = \vec{r} \times \vec{B} = \frac{ba}{2} (-\hat{k}) \times B_0 (2\hat{i} - \hat{k})$$

$$= \underline{\underline{-baB_0 \hat{j}}}$$

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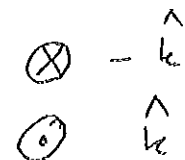
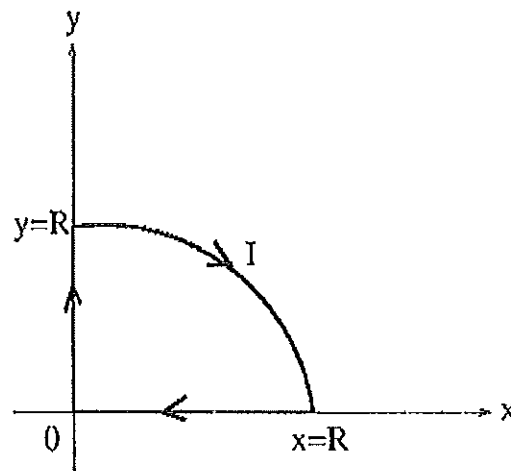
Name:

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If the current carrying loop shown in the figure is under a uniform magnetic field

$\vec{B} = B_0(\hat{i} + \hat{j} + \hat{k})$, calculate the total torque caused by the magnetic force.



Total Force is equal to zero

$$\vec{\tau} = \vec{\mu} \times \vec{B}, \quad \vec{\mu} = \frac{\pi R^2}{4} (-\hat{k})$$

$$\begin{aligned} \vec{\tau} &= \vec{\mu} \times \vec{B} = \frac{\pi R^2}{4} B_0 (-\hat{j} + \hat{i}) \\ &= \frac{\pi R^2}{4} B_0 (\hat{i} - \hat{j}) \end{aligned}$$

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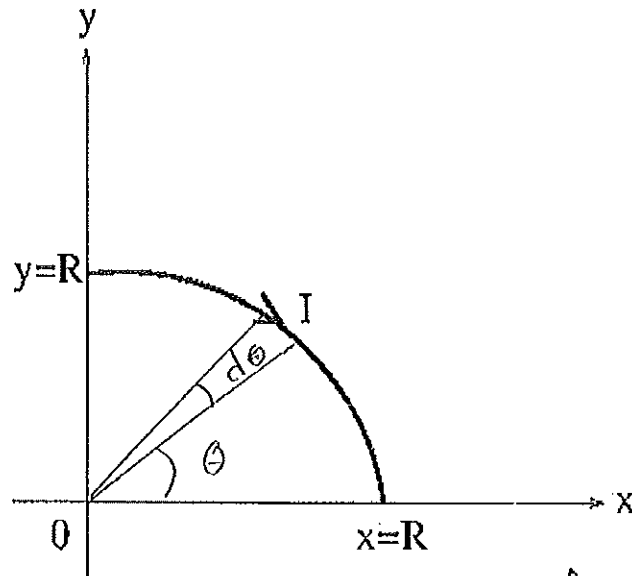
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If the current carrying wire shown in the figure is under a varying magnetic field given by

$\vec{B} = B_0 x \hat{j}$, calculate the total magnetic force.



$$d\vec{F} = I d\vec{l} \times \vec{B} = I (dx \hat{i} + dy \hat{j}) \times B_0 x \hat{j}$$

$$d\vec{l} = R d\theta (-\sin\theta \hat{i} + \cos\theta \hat{j})$$

$$x = R \cos\theta, \quad y = R \sin\theta$$

$$\vec{F} = \int_{\pi/2}^0 I R^2 B_0 (-\sin\theta \hat{i} + \cos\theta \hat{j}) x \cos\theta \hat{j} d\theta$$

$$= \int_{\pi/2}^0 I R^2 B_0 (-\sin\theta \cos\theta \hat{k}) d\theta = \frac{I R^2 B_0}{2} \cos^2\theta \Big|_{\pi/2}^0$$

$$= \frac{I R^2 B_0}{2} \hat{k}$$