

Closed book. No calculators are to be used for this quiz.

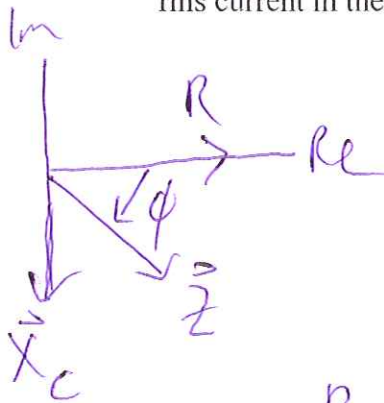
Quiz duration: 10 minutes

Name:

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Signature:

A circuit consists of a resistor and a capacitor in series with an ac source that supplies an rms voltage 240 V. At the frequency of the source the reactance of the capacitor is 50.0 Ω . The rms current in the circuit is 3.0 A. What is the average power supplied by the source?



$$Z = [R^2 + X_c^2]^{1/2}$$

$$P_{av} = V_{rms} I_{rms} \cos \phi$$

$$P_{av} = 0.78 \times (240V)(3A)$$

$$P_{av} = 562.05 \text{ Watt}$$

$$Z = \frac{V_{rms}}{I_{rms}} = \frac{240V}{3A} = 80 \Omega$$

$$R = [Z^2 - X_c^2]^{1/2}$$

$$R = 62.45 \Omega$$

$$\cos \phi = \frac{62.45}{80} = 0.78$$

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An L-R-C series circuit has $R=300\ \Omega$. At the frequency of the source, the inductor has reactance $X_L = 900\ \Omega$ and the capacitor has reactance $X_C = 500\ \Omega$. The amplitude of the voltage across the inductor is $450\ \text{V} = V_L$.

- What is the amplitude of the voltage across the resistor?
- What is the amplitude of the voltage across the capacitor?
- What is the amplitude of the voltage across the source?
- What is the rate at which the source is delivering electrical energy to the circuit?

$$a) I = \frac{V_L}{X_L} = \frac{450\text{V}}{900\ \Omega} = \boxed{0.5\text{A}}; \quad V_R = IR = (0.5\text{A}) \times (300\ \Omega) = \boxed{V_R = 150\text{V}}$$

$$b) V_C = I X_C = (0.5\text{A}) \times (500\ \Omega) = \boxed{250\text{V} = V_C}$$

$$c) Z = \left[R^2 + (X_L - X_C)^2 \right]^{1/2} = \left\{ 300^2 + [900 - 500]^2 \right\}^{1/2} \Omega = \boxed{500\ \Omega = Z}$$

$$V = IZ = (0.5\text{A}) (500\ \Omega) = \underline{250\text{V}}$$

$$d) P_{\text{ave}} = I_{\text{rms}}^2 R = \frac{1}{2} (0.5\text{A})^2 (300\ \Omega) = \underline{37.5\text{Watt}}$$

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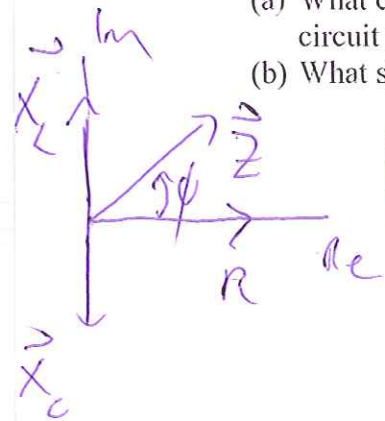
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A series circuit has an impedance of 60.0Ω and a power factor of 0.7 at 50.0 Hz . The source voltage lags the current. (For $\cos \phi = 0.7 \rightarrow \phi = 45^\circ \rightarrow \tan 45^\circ = 1$)

- (a) What circuit element, an inductor or a capacitor, should be placed in series with the circuit to raise its power factor?
 (b) What size element will raise the power factor to unity?



$$\text{Power Factor} = \frac{R}{Z} = \cos \phi$$

$$X_L > X_C \text{ at } t=0$$

a) Voltage lags $\Rightarrow \phi > 0$ so in order to increase power factor, we should reduce Z .

- to reduce Z $\phi > 0$, we should add X_C to balance $X_L (> X_C)$.

$$\text{b) if } X_L = X_C \Rightarrow Z = R \Rightarrow \cos \phi = 1$$

we need to add X_C in such a way that $\phi = 0$.

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An L-R-C series circuit has $C=5.0 \mu\text{F}$, $L=500 \text{ mH}$, and source voltage amplitude $V=60.0 \text{ V}$. The source is operated at the resonance frequency of the circuit. If the voltage across the capacitor has amplitude 80.0 V , what is the value of R for the resistor in the circuit?

$$X_L(\omega_R) \equiv X_C(\omega_R) \rightarrow \omega_R = [L \cdot C]^{-1/2} = [(500 \times 10^{-3} \text{ H}) \cdot (5 \times 10^{-6} \text{ F})]^{-1/2}$$

$$\omega_R = 632.46 \text{ rad/s} \rightarrow X_L(\omega_R) = \omega_R L = (632.46 \text{ rad/s}) \cdot (500 \times 10^{-3} \text{ H})$$
$$X_L(\omega_R) = 316.23 \Omega$$

$$I(\omega_R) = \frac{V_C(\omega_R)}{X_C(\omega_R)} = \frac{80 \text{ V}}{316.23 \Omega} = 0.253 \text{ A}$$

$$Z(\omega_R) = R \rightarrow R = \frac{V}{I(\omega_R)} = \frac{60 \text{ V}}{0.253 \text{ A}} = 237.17 \Omega$$

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In the L-R-C series circuit, $L = 160 \text{ mH}$ and $C = 4 \mu\text{F}$. The voltage amplitude of the source is 120 V .

- What is the resonance angular frequency of the circuit?
- When the source operates at the resonance angular frequency, the current amplitude in the circuit is 1.0 A . What is the resistance R of the resistor?
- At the resonance angular frequency, what are the peak voltages across the inductor, the capacitor, and the resistor?

$$a) \text{ if } \omega = \omega_R \Rightarrow (X_L(\omega_R) - X_C(\omega_R)) = \frac{\omega_R L}{\omega_R C} - \frac{1}{\omega_R C} = 0 \Rightarrow \omega_R = \frac{1}{\sqrt{LC}}$$

$$\rightarrow \omega_R = [(160 \times 10^{-3} \text{ H}) \cdot (4 \times 10^{-6} \text{ F})]^{-1/2} = (1.25 \times 10^3) \text{ rad/s}$$

$$b) Z(\omega = \omega_R) = R \rightarrow Z = \frac{V}{I} \rightarrow R = \frac{V(\omega_R)}{I(\omega_R)} = \frac{120 \text{ V}}{1 \text{ A}} = 120 \Omega$$

$$c) V_L(\omega_R) = I(\omega_R) X_L(\omega_R) = I(\omega_R) \cdot [\omega_R L] = [1 \text{ A} \times (1.25 \times 10^3 \text{ rad/s}) \times (160 \times 10^{-3} \text{ H})]$$

$$\boxed{V_L(\omega_R) = 200 \text{ V}} ; X_L(\omega_R) = X_C(\omega_R) \text{ \& } V_C = I X_C \Rightarrow \boxed{V_C = 200 \text{ V}}$$

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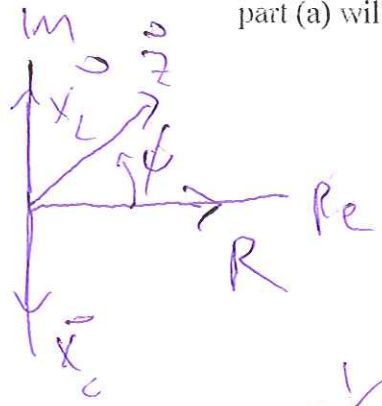
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$\omega = 2\pi f$

An L-R-C series circuit consists of 4Ω resistor, a $11 \mu\text{F}$ capacitor, a 3 mH inductor, and an ac voltage source of voltage amplitude 6 V operating at 1000 Hz . (Take $\pi=3$)

- (a) Find the current amplitude and the voltage amplitudes across the inductor, the resistor, and the capacitor. Why can the voltage amplitudes add up more than 6 V ?
- (b) If the frequency is now doubled, but nothing else is changed, which of the quantities in part (a) will change? Find the new values for those that do change.



$$Z = [R^2 + (X_L - X_C)^2]^{1/2}$$

$$= [16 + 81]^{1/2} \Omega$$

$$Z = 9.85 \Omega$$

$Z \approx 10 \Omega$

a) $X_L = \omega L = (10^3 \text{ 1/s}) \cdot (3 \times 10^{-3} \text{ H}) \cdot (2 \cdot 3 \text{ rad})$

$$X_L = 6 \Omega$$

$$X_C = [\omega C]^{-1} = [(6 \times 10^3 \text{ rad/s}) \cdot (11 \times 10^{-6} \text{ C})]^{-1}$$

$$X_C \approx 15 \Omega$$

$$I = \frac{V}{Z} = \frac{6 \text{ V}}{10 \Omega} = 0.6 \text{ A} = I$$

$$V_L = I X_L = 3.6 \text{ V}; \quad V_C = I X_C = 9 \text{ V};$$

$$V_R = I R = 2.4 \text{ V}$$

b) $\omega' = 2\omega$

$$X_L' = 2X_L = 12 \Omega$$

$$X_C' = \frac{1}{2}X_C = 7.5 \Omega$$

$$Z' = 6 \Omega \rightarrow I' = \frac{6 \text{ V}}{6 \Omega} = 1 \text{ A}$$

$$V_L' = I' X_L' = 12 \text{ V} \leftarrow \text{increased}$$

$$V_C' = I' X_C' = 7.5 \text{ V} \leftarrow \text{decreased}$$

$$V_R' = I' R = 4 \text{ V} \leftarrow \text{increased}$$