

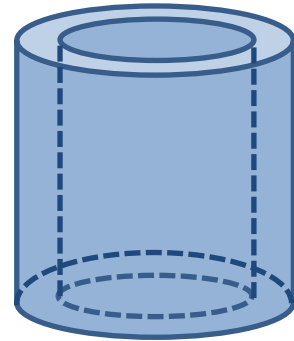
**Closed book. No calculators are to be used for this quiz.**  
**Quiz duration: 10 minutes**

**Name:**

**Student ID:**

**Signature:**

A hollow cylindrical conductor with center axis along the  $z$  axis has inner radius  $R_1$  and outer radius  $R_2$ . The current density in the conductor (i.e between  $R_1$  and  $R_2$ ) is given by  $\vec{J} = J_0 \hat{z}$  where  $J_0$  is a constant. Outside the conductor, the current is zero. Using Ampere's law, calculate the magnetic field  $B(r)$  for  $r < R_1$ ,  $R_1 < r < R_2$ , and  $R_2 < r$ . (Ampere's law:  $\oint \vec{B} \cdot d\vec{l} = \mu_0 I$ )



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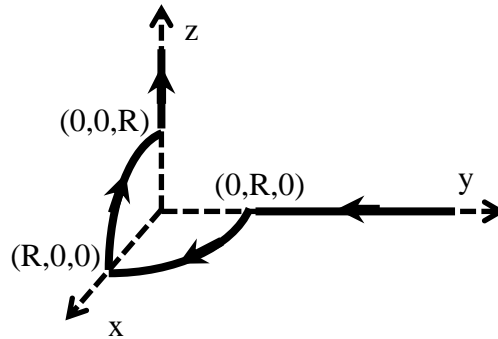
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An infinitely long wire along the  $y$ -axis is bent to form two quarter circles of radius  $R$  centered at the origin and then extends in the  $z$  direction as shown in the figure. Current  $I$  flows in the wire in the direction shown by the arrows. Determine the net magnetic field (magnitude & direction) generated at the origin using Biot and Savart law:  $d\vec{B} = \frac{\mu_0}{4\pi} \frac{I d\vec{l} \times \hat{r}}{r^2}$ . Also use symmetry arguments)



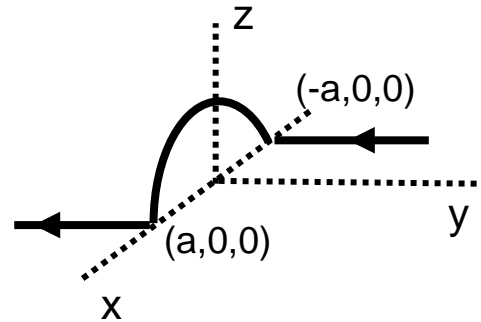
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An infinitely long wire parallel to y axis is bent to form a semicircle of radius  $a$  in the x-z plane and centered at the origin. The intersection points of the wire with the x-axis are shown in the figure. A current  $I$  flows through the wire in the shown direction. Determine the net magnetic field (magnitude and direction) at the origin using Biot and Savart law:  $d\vec{B} = \frac{\mu_0 I d\vec{l} \times \hat{r}}{4\pi r^2}$ . (Hint: For the straight wire parts use your reasoning.)



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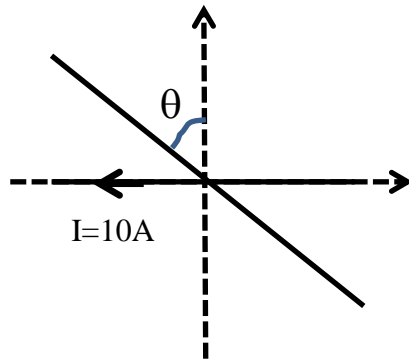
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Two infinite wires are located on the x-y plane. One of the wires is oriented along the x-axis and carries a current 10 A in the -x direction. The other wire is oriented at an angle  $\theta$  with the y-axis and carries a current of 5A. If the magnetic field along the y-axis is zero, what must be the direction of the current of the second wire and the angle  $\theta$ ? (The magnitude of the magnetic field of an infinite wire at a distance  $r$  is  $B = \frac{\mu_0 I}{2\pi r}$ )



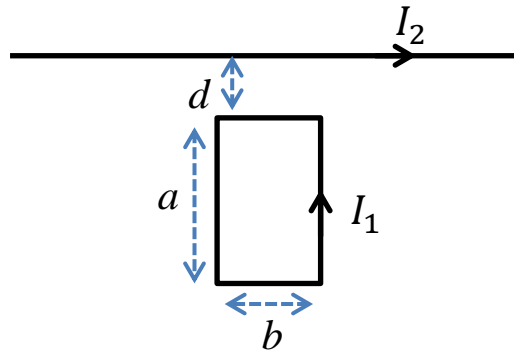
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A rectangular loop wire (long edge length  $a$ , short edge length  $b$ ) is placed with the short edges parallel to an infinitely long straight wire located on the  $x$ -axis as shown in the figure. The close edge of the rectangle is at a distance  $d$  from the wire. The loop carries a current  $I_1$  in the counterclockwise direction and the straight wire carries a current  $I_2$  in the  $+x$  direction. Determine the net force (magnitude and direction) acting on the loop. (Hint: the magnetic force on a straight wire of length  $\vec{L}$  with current  $I$  in constant magnetic field  $\vec{B}$  is  $\vec{F} = I\vec{L} \times \vec{B}$ . Also, use symmetry arguments in your solution).



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A very long solid cylindrical conductor of radius  $R$  has a current density  $J = ar^2$  for  $0 < r < R$  flowing along the axis of the conductor ( $a$  is a constant). Outside the conductor, the current density is zero ( $J = 0$  for  $r > R$ ). Using Ampere's law, determine the magnitude of the magnetic field inside and outside the conductor as a function of radial distance  $r$  from the center of the conductor. (Ampere's law:  $\oint \vec{B} \cdot d\vec{l} = \mu_0 I$ )

