





Closed book. No calculators are to be used for this quiz.  
Quiz duration: 10 minutes

Name:

Student ID:

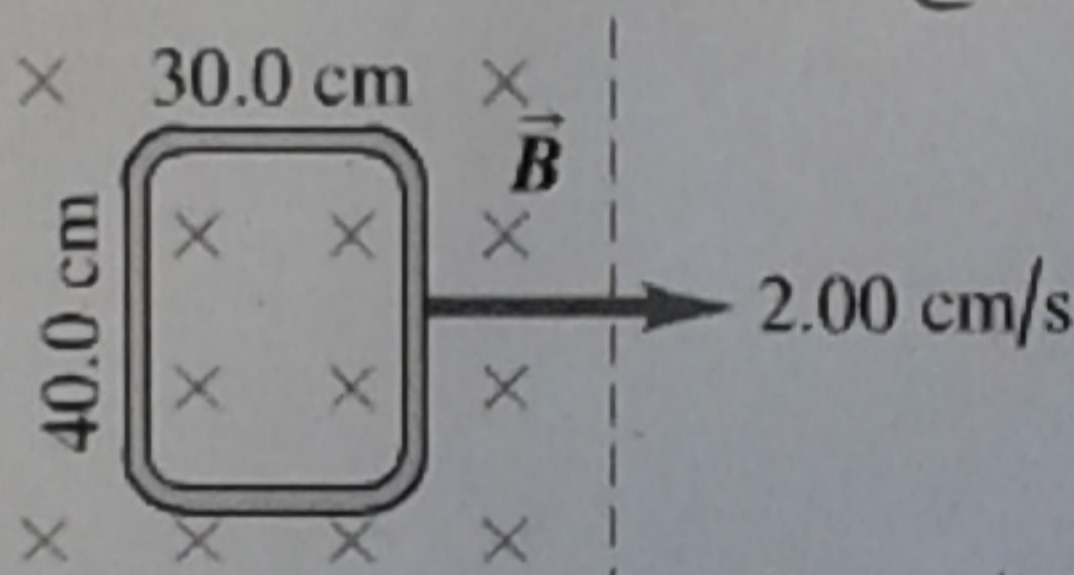
Signature:

A rectangle measuring 30.0 cm by 40.0 cm is located inside a region of a spatially uniform magnetic field of 1.25 T, with the field perpendicular to the plane of the coil as shown in the figure. The coil is pulled out at a steady rate of 2.00 cm/s traveling perpendicular to the field lines. The region of the field ends abruptly as shown. Find the emf induced in this coil when it is;

- a) All inside the field;
- b) Partly inside the field;
- c) All outside the field.

Induced emf :

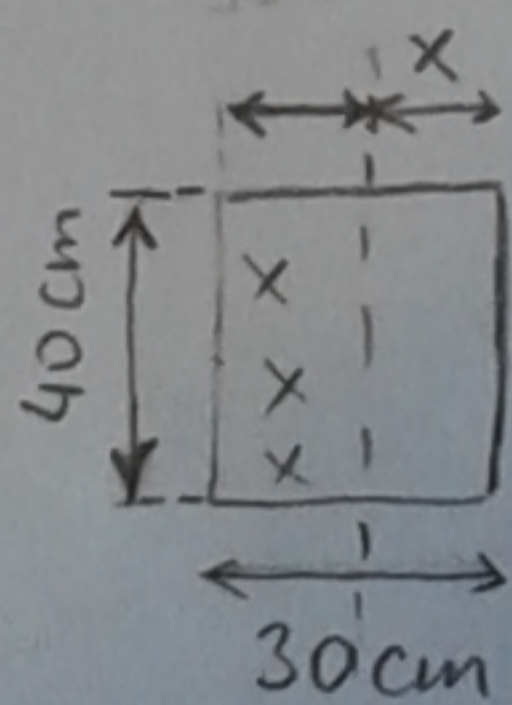
$$\mathcal{E} = - \frac{d\Phi_B}{dt}$$



a) 
$$\mathcal{E} = - \frac{d}{dt} (\vec{B} \cdot A \hat{n}) = - \frac{d}{dt} (BA) = 0$$

where  $B = \text{const.} = 1.25 \text{ T}$  and  $A = 0.3 \text{ m} \cdot 0.4 \text{ m} = 0.12 \text{ m}^2 = \text{const.}$

b) Let



$$A = 0.4 \cdot (0.3 - x)$$

$$B = \text{const} = 1.25 \text{ T}$$

$$\mathcal{E} = - \frac{d}{dt} (BA) = -B \cdot \frac{dA}{dt} = -B \frac{d}{dt} (0.4 \cdot (0.3 - x)) =$$

$$= 0.4 B \cdot \frac{dx}{dt} = 0.4 B v = 0.4 \cdot 1.25 \cdot 0.02 = 0.01 \text{ Tm}^2/\text{s}$$

c) The same as in b) for  $x = 0.3 \text{ m} \Rightarrow \mathcal{E} = 0.01 \text{ Tm}^2/\text{s}$  //

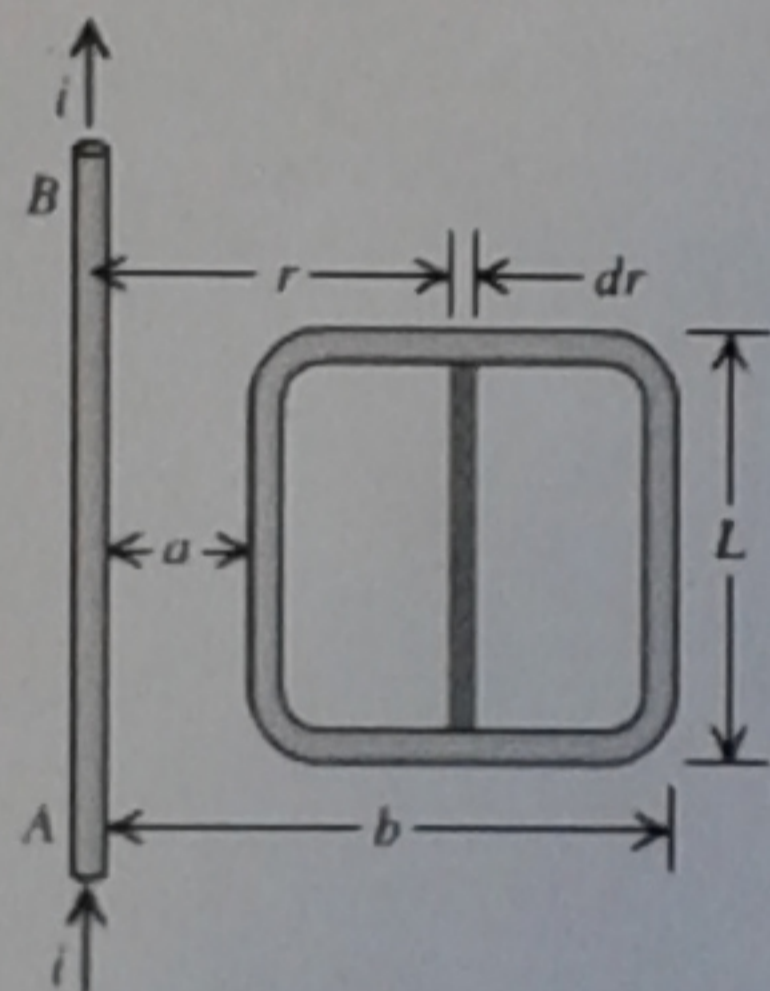


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The current in the long, straight wire AB shown in the figure below is upward and is increasing steadily at a rate  $di/dt$ .

- a) At an instant when the current is  $i$ , what are the magnitude <sup>and</sup> direction of the field  $\vec{B}$  at a distance  $r$  to the right of the wire?
- b) What is the flux  $d\Phi_B$  through the narrow, shaded strip?
- c) What is the total flux through the loop?
- d) What is the induced emf in the loop?



a) From Ampère's law:  $\oint_C \vec{B} \cdot d\vec{\ell} = \mu_0 I_{enc}$

where  $I_{enc} = i(t) = \frac{di}{dt} t$  and  $\frac{di}{dt} = \text{const.}$

$\Rightarrow B \cdot (2\pi r) = \mu_0 i \Rightarrow B = \frac{\mu_0 i}{2\pi r}$

The direction of  $\vec{B}$  into into the plane  $\otimes$  at "r".

b)  $d\Phi_B = \vec{B} \cdot d\vec{S} = B \cdot (L dr) = \frac{\mu_0 i L}{2\pi r} dr$  ( $\vec{B} \parallel \vec{S}$ )

c)  $\Phi_B = \int \vec{B} \cdot d\vec{S} = \frac{\mu_0 i L}{2\pi} \int_a^b \frac{dr}{r} = \frac{\mu_0 i L}{2\pi} \ln(b/a)$

d)  $\mathcal{E} = -\frac{d\Phi_B}{dt} = -\frac{\mu_0 L}{2\pi} \frac{di}{dt} \ln(b/a)$