

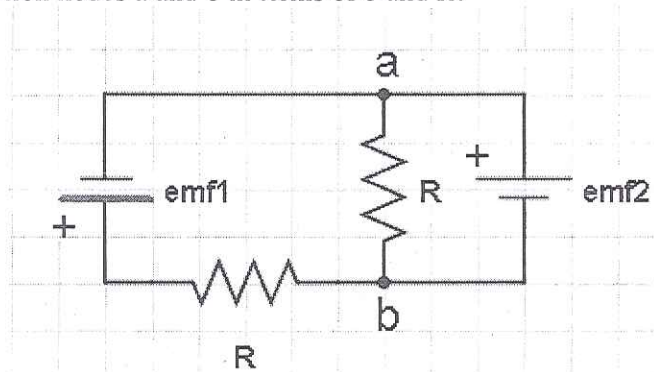
Closed book. No calculators are to be used for this quiz.
Quiz duration: 10 minutes

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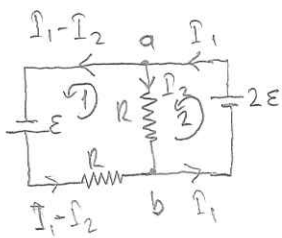
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In the circuit shown, $\text{emf1} = \varepsilon$, $\text{emf2} = 2\varepsilon$. Batteries are ideal. Find the power used between the junction nodes a and b in terms of ε and R .



First, we need to find V_{ab} and currents of the circuit.



Loop 1 in c.c.w direction:

$$\varepsilon - (I_1 - I_2)R + I_2 R = 0$$

$$\varepsilon - I_1 R + 2I_2 R = 0 \quad (1)$$

Loop 2 in c.c.w direction:

$$2\varepsilon - I_2 R = 0$$

$$I_2 = \frac{2\varepsilon}{R} \quad (2)$$

Replacing for I_2 in equation (1):

$$\varepsilon - I_1 R + 2 \frac{2\varepsilon}{R} R = 0$$

$$I_1 = \frac{5\varepsilon}{R}$$

$$I_1 - I_2 = \frac{3\varepsilon}{R}$$

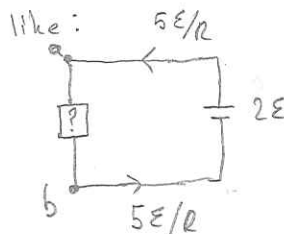
$$V_{ab} = I_2 R = 2\varepsilon$$

We could find V_{ab} going from other paths as well:

$$V_a + \varepsilon - (I_1 - I_2)R = V_b$$

$$\begin{aligned} V_a - V_b = V_{ab} &= (I_1 - I_2)R - \varepsilon \\ &= 2\varepsilon \end{aligned}$$

Now we know what our circuit looks



$$V_{ab} = 2\varepsilon \frac{5\varepsilon}{R} = \frac{10\varepsilon^2}{R}$$

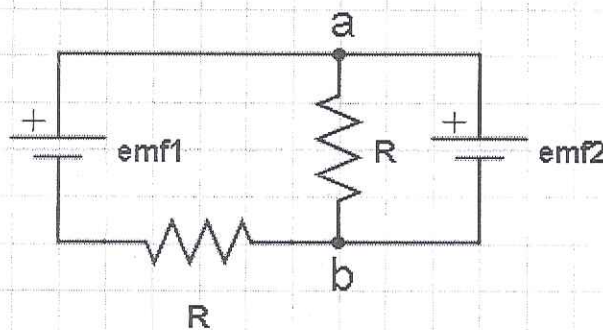
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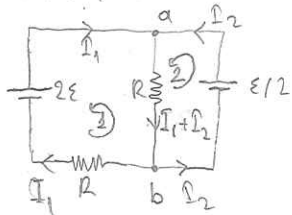
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In the circuit shown, $\text{emf1} = 2\varepsilon$, $\text{emf2} = \varepsilon/2$. Batteries are ideal. Find the power used between the junction nodes a and b in terms of ε and R .



First, we need to find V_{ab} and currents of the circuit.



Loop 1 in c.c.w direction:

$$-2\epsilon + I_1 R + (I_1 + I_2)R = 0$$

$$-2I_1 R + I_2 R = 2\epsilon \quad (1)$$

Loop 2 in c.c.w direction:

$$\frac{\epsilon}{2} - (I_1 + I_2)R = 0$$

$$I_1 R + I_2 R = \frac{\epsilon}{2} \quad (2)$$

Subtracting eq. (2) from eq. (1) we get:

$$I_1 R = \frac{3\epsilon}{2} \rightarrow I_1 = \frac{3\epsilon}{2R}$$

From eq. (2):

$$\frac{3\epsilon}{2R} R + I_2 R = \frac{\epsilon}{2}$$

$$I_2 = -\frac{\epsilon}{R}$$

$$I_1 + I_2 = \frac{\epsilon}{2R}$$

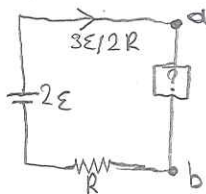
$$V_{ab} = (I_1 + I_2)R = \frac{\epsilon}{2}$$

We could find V_{ab} going from other paths as well. Example:

$$V_b - I_1 R + 2\epsilon = V_a$$

$$V_a - V_b = 2\epsilon - \frac{3\epsilon}{2R} R = \frac{\epsilon}{2}$$

Our circuit looks like:



$$P_{ab} = V_{ab} I_1 = \frac{\epsilon}{2} \frac{3\epsilon}{2R} = \frac{3\epsilon^2}{4R}$$

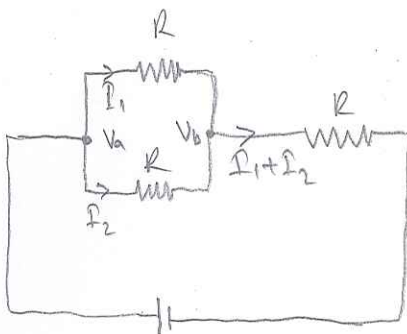
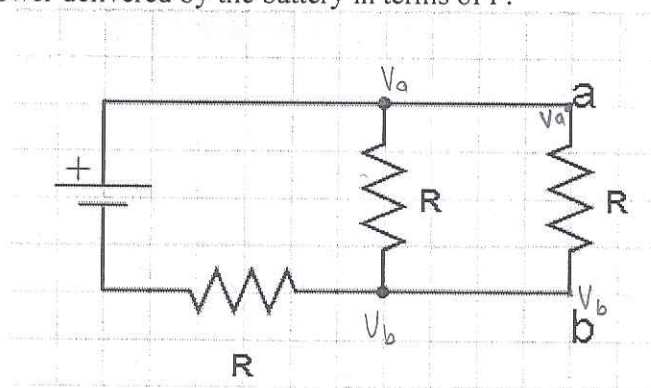
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In the circuit shown, the power dissipated (used) between the nodes a and b is P. Determine the power delivered by the battery in terms of P.



$I_1 = I_2$ since resistors are parallel
 and their resistance is equal.

$$P_{ab} = I_1^2 R = P$$

$$P_{\text{battery}} = I_1^2 R + I_2^2 R + (I_1 + I_2)^2 R$$

$$= 6I_1^2 R = 6P$$