

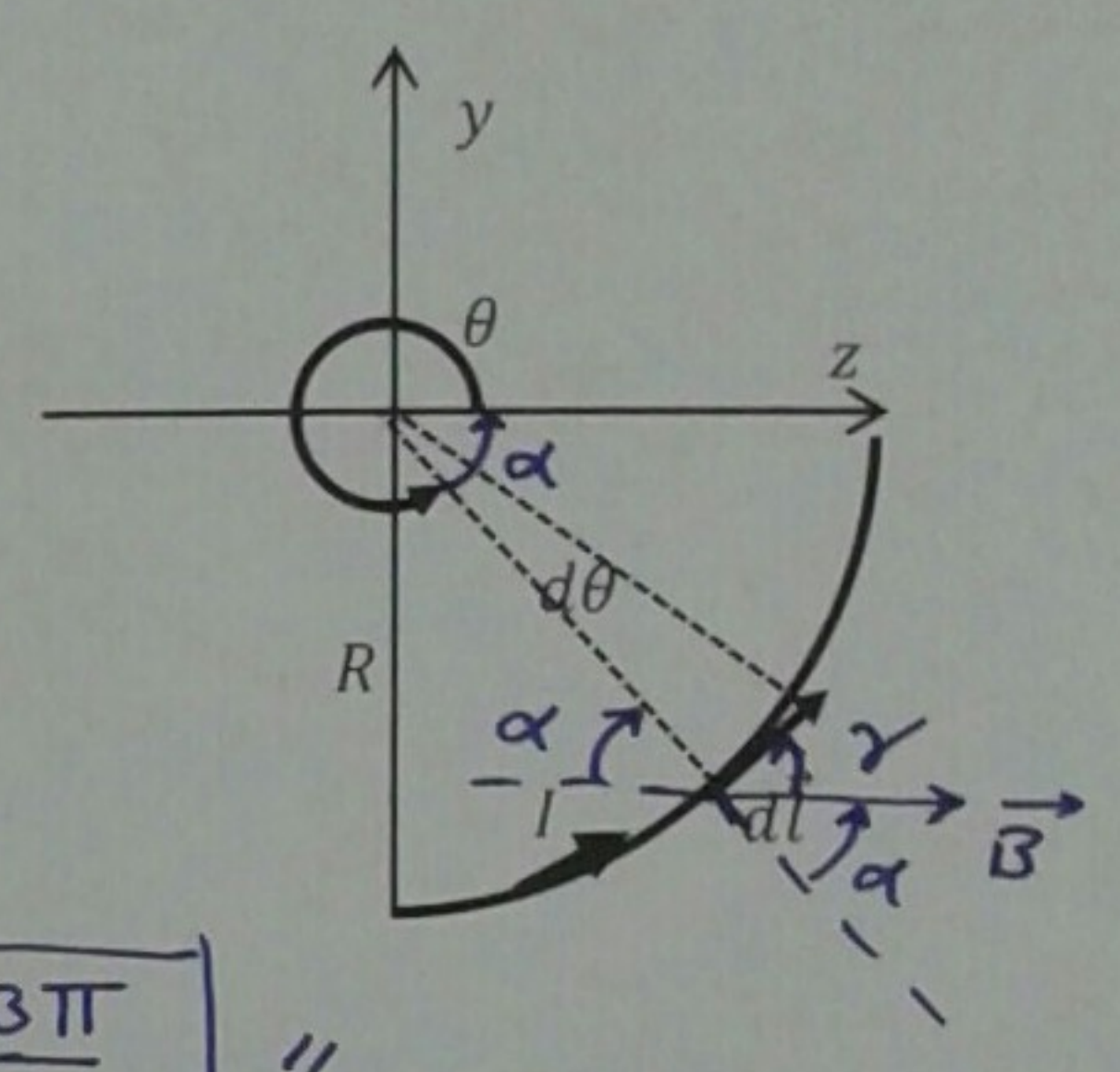
Closed book. No calculators are to be used for this quiz.
Quiz duration: 10 minutes

Name:

Student ID:

Signature:

The quarter circular arc segment of a wire with current I in counterclockwise direction is placed in a uniform magnetic field $\vec{B} = B\hat{z}$. The radius of arc is R . Using $d\vec{F} = I d\vec{l} \times \vec{B}$ and the polar coordinates, calculate the total force on the wire segment. Hint: First find the direction of \vec{F} by the right hand rule. In finding the magnitude by the integral, express the angle between $d\vec{l}$ and \vec{B} in terms of θ .



$$\alpha = 2\pi - \theta$$

$$\gamma = \frac{\pi}{2} - \alpha = \frac{\pi}{2} - (2\pi - \theta) =$$

$$= \theta - \frac{3\pi}{2} \Rightarrow \boxed{\gamma = \theta - \frac{3\pi}{2}} //$$

Since $d\vec{F} = I d\vec{l} \times \vec{B}$

By the right hand rule the direction of \vec{F} is perpendicular to the plane (into the plane) $\Rightarrow \otimes \vec{F}$

Also, $dF = I dl B \sin \gamma = I dl B \sin(\theta - \frac{3\pi}{2}) =$
 $= -I dl B \sin(\frac{3\pi}{2} - \theta) = IB dl \cos \theta //$

$\Rightarrow F = \int IB dl \cos \theta = IB R \int_{3\pi/2}^{2\pi} \cos \theta d\theta = IB R \sin \theta \Big|_{3\pi/2}^{2\pi} =$
 $= IB R //$

$\Rightarrow \boxed{F = IB R} //$

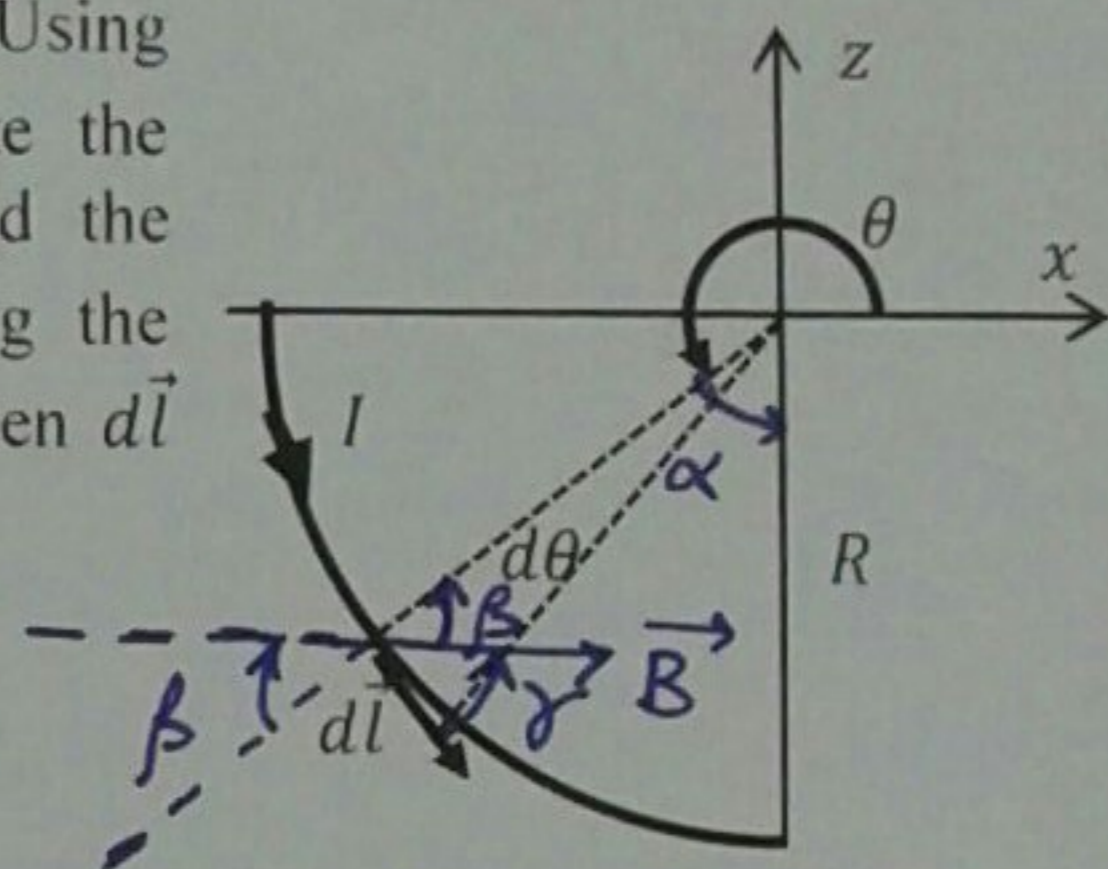
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The quarter circular arc segment of a wire with current I in counterclockwise direction is placed in a uniform magnetic field $\vec{B} = B\hat{x}$. The radius of arc is R . Using $d\vec{F} = I d\vec{l} \times \vec{B}$ and the polar coordinates, calculate the total force on the wire segment. Hint: First find the direction of \vec{F} by the right hand rule. In finding the magnitude by the integral, express the angle between $d\vec{l}$ and \vec{B} in terms of θ .



$$\alpha = \frac{3\pi}{2} - \theta, \quad \beta = \frac{\pi}{2} - \alpha$$

$$\gamma = \frac{\pi}{2} - \beta = \frac{\pi}{2} - \left(\frac{\pi}{2} - \alpha\right) = \alpha = \frac{3\pi}{2} - \theta \Rightarrow \boxed{\gamma = \frac{3\pi}{2} - \theta}$$

By the right hand rule the direction of \vec{F} is perpendicular to the plane (out of the plane) $\Rightarrow \odot \vec{F}$

$$\text{Also, } dF = I dl B \sin \gamma = I dl B \sin \left(\frac{3\pi}{2} - \theta\right) = -IB dl \cos \theta$$

$$\Rightarrow F = \int -IB dl \cos \theta = -IBR \int_{\pi}^{2\pi} \cos \theta d\theta = -IBR \sin \theta \Big|_{\pi}^{2\pi} =$$

$$= IBR \Rightarrow \boxed{F = IBR}$$

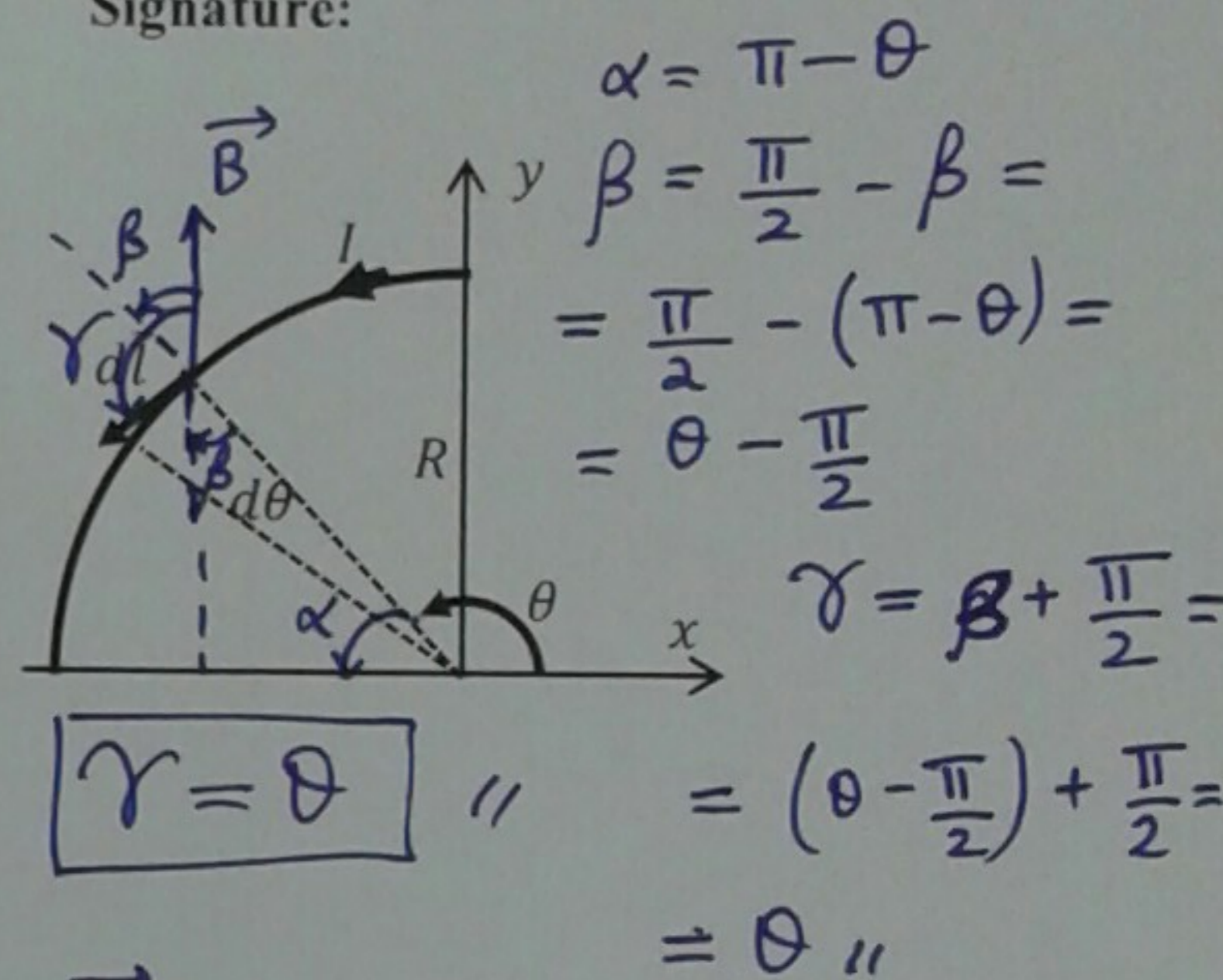
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Name:

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The quarter circular arc segment of a wire with current I in counterclockwise direction is placed in a uniform magnetic field $\vec{B} = B\hat{y}$. The radius of arc is R . Using $d\vec{F} = Id\vec{l} \times \vec{B}$ and the polar coordinates, calculate the total force on the wire segment. Hint: First find the direction of \vec{F} by the right hand rule. In finding the magnitude by the integral, express the angle between $d\vec{l}$ and \vec{B} in terms of θ .



Since $d\vec{F} = Id\vec{l} \times \vec{B}$

By the right hand rule the direction of \vec{F} is perpendicular to the plane (into the plane) $\Rightarrow \otimes \vec{F}$

Also, $dF = IdlB \sin \gamma = IdlB \sin \theta$

$\Rightarrow F = \int IB \sin \theta dl = IBR \int_{\pi/2}^{\pi} \sin \theta d\theta = IRR (-\cos \theta) \Big|_{\pi/2}^{\pi} = IBR$
 where $dl = R d\theta$

$\Rightarrow \boxed{F = IBR} \quad \text{''}$