

Closed book. No calculators are to be used for this quiz.

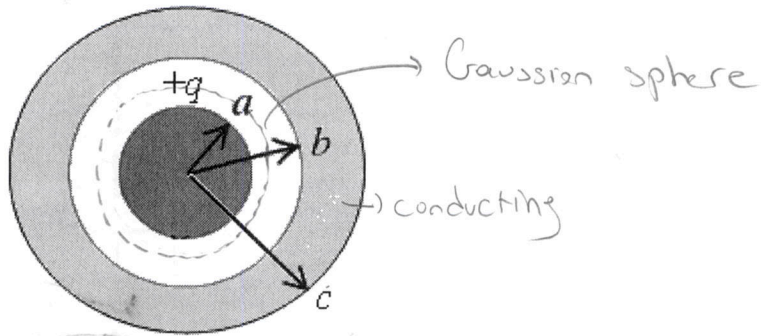
Quiz duration: 10 minutes

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A solid conducting sphere carrying charge q has radius a . It is inside a concentric hollow conducting sphere with inner radius b and outer radius c . The hollow sphere has no net charge.

(a) Derive expressions for the electric field magnitude in terms of the distance r from the center for the regions $r < a$, $a < r < b$, $b < r < c$, and $r > c$.

(b) Graph the magnitude of the electric field as a function of r from $r = 0$ to $r = 2c$.

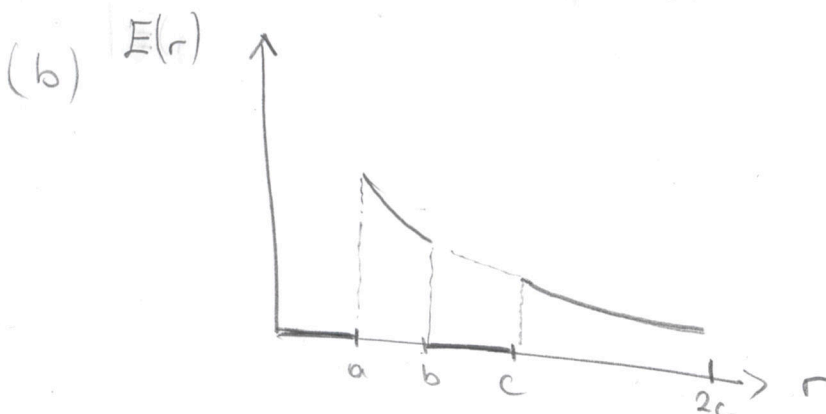


(a) $\oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{enclosed}}}{\epsilon_0}$ and $\vec{E} = \vec{0}$ in conductor

Therefore

$$E(r) = \begin{cases} 0 & r < a & \text{(conductor)} \\ \frac{q}{4\pi\epsilon_0 r^2} & a < r < b & \left(4\pi r^2 E = \frac{q}{\epsilon_0} \right) \\ 0 & b < r < c & \text{spherically symmetric (conductor)} \\ \frac{q}{4\pi\epsilon_0 r^2} & r > c & \end{cases}$$

$Q_{\text{enc}} = +q$ as when $a < r < b$



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A very long conducting tube (hollow cylinder) has inner radius a and outer radius b . It carries charge per unit length $+\alpha$, where α is the positive constant with units of C/m. A line of charge lies along the axis of the tube. The line of charge has charge per unit length $+\alpha$.

(a) Calculate the electric field in terms of α and the distance r from the axis of the tube for $r < a$, $a < r < b$ and $r > b$.

(b) Graph the electric field magnitude as a function of r in all the regions?

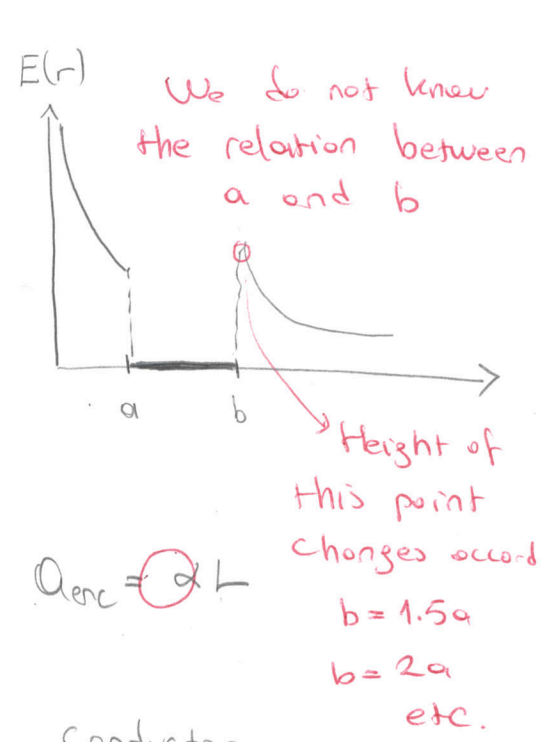
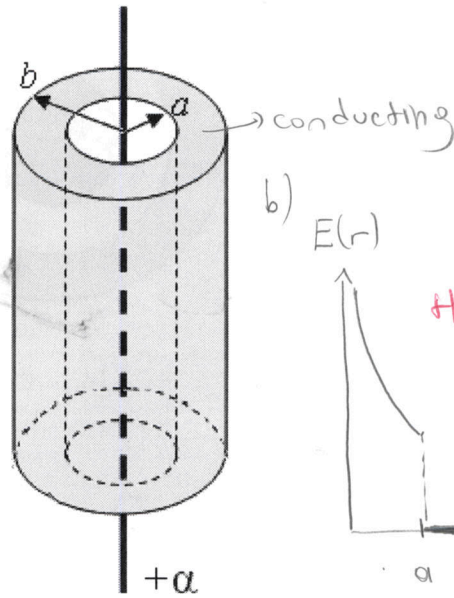
Gauss' Law for $r < a$

cylindrically symmetric

Gaussian cylinder

$$\oint \vec{E} \cdot d\vec{A} = E 2\pi r L = \frac{Q_{enc}}{\epsilon_0} = \frac{\alpha L}{\epsilon_0} \quad (1)$$

$$E = \frac{\alpha}{2\pi r \epsilon_0}$$



(a) Gauss' Law $\oint \vec{E} \cdot d\vec{A} = \frac{Q_{enc}}{\epsilon_0}$

$$E(r) = \begin{cases} \frac{\alpha}{2\pi r \epsilon_0} & r < a \\ 0 & a < r < b \\ \frac{\alpha}{\pi r \epsilon_0} & r > b \end{cases}$$

$Q_{enc} = \alpha L$

conductor

$Q_{enc} = 2\alpha L$

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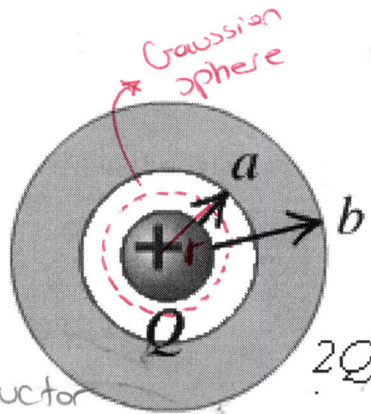
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A conducting spherical shell with inner radius a and outer radius b contains a total charge $2Q$. A positive point charge Q is located at the center of the spherical shell.

- (a) Derive the expression for the electric field magnitude as a function of the distance r from the center for the regions $r < a$, $a < r < b$, and $r > b$.
 (b) Graph the electric field magnitude as a function of r .

Gauss' Law

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{enc}}{\epsilon_0}$$



For the Gaussian sphere

$$\oint \vec{E} \cdot d\vec{A} = E \cdot 4\pi r^2 = \frac{Q}{\epsilon_0}$$

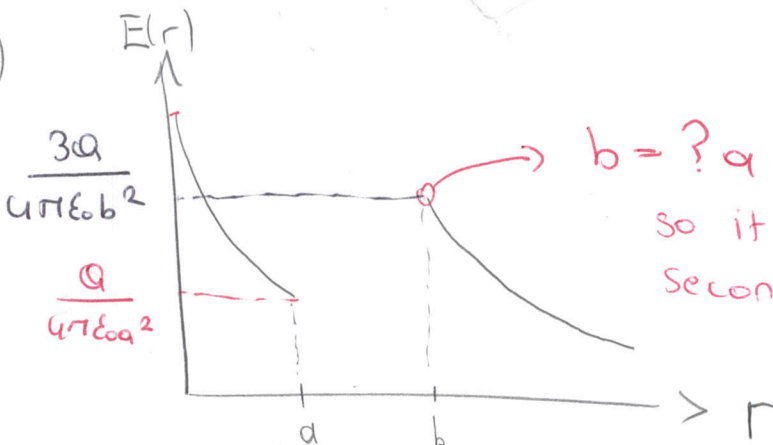
↓
spherically symmetric

$E=0$ inside a conductor

a)

$$E(r) = \begin{cases} \frac{Q}{4\pi\epsilon_0 r^2} & 0 < r < a & Q_{enc} = +Q \\ 0 & a < r < b & \text{(conductor)} \\ \frac{3Q}{4\pi\epsilon_0 r^2} & r > b & Q_{enc} = +3Q \end{cases}$$

b)



so it is also possible that the second curve is below the first one