Name:	Signature:
Surname:	Number:

## **KOÇ UNIVERSITY**

## College of Sciences PHYS 102 General Physics 2 Spring Semester 2017 Midterm Exam 1 March 14, 2017 Thursday, 19:00-20:40

## Please read.

- Count to make sure that there are 5 pages in this question booklet
- Check your name, number, on front page, and student ID on each page.
- This examination is conducted with closed books and notes.

• Put all your personal belongings underneath your seat and make sure that pages of books or notebooks are not open.

• Absolutely no talking or exchanging anything (like rulers, erasers) during the exam.

• You must show all your work to get credit; you will not be given any points unless you show the details of your work (this applies even if your final answer is correct).

- Write neatly and clearly; unreadable answers will not be given any credit.
- If you need more writing space, use the backs of the question pages and put down the appropriate pointer marks.
- Make sure that you include units in your results.
- Make sure that you label the axis and have units in your plots.
- You are not allowed to use calculators during this exam.
- Turn off your mobile phones, and put away.
- You are not allowed to leave the class during the first 15 minutes, and last 15 minutes.

P102\_Index:

1	2	3	4	Total

ExamRoom:	P101_Index:
Student ID Number:	Signature:

**1-(25 Points)** Two identical point charges with charge Q are positioned a distance d apart. Another point charge q is placed in the middle of the two.







V

q

(d/2,0)

0

> X

(-d/2,0)

Q

c) Is the charge *q* in stable equilibrium? Are the charges *Q* in stable equilibrium? Give your answers by considering a small horizontal displacement of the charge and checking if you get a restoring force.

ExamRoom:	P101_Index:
Student ID Number:	Signature:

**2-(25 Points)** 2) Four *infinite*, non-conducting planes each with *uniform* surface charge density  $\sigma$  are perpendicular to the *x-y* plane, and they intersect each other to form a square of side 2*a*. An *infinitely long*, non-conducting, thin cylindrical shell of radius *a* is also parallel to the planes (its central axis is the *z* axis). The cylindrical shell has *uniform* surface charge density –  $\sigma$ . You can see the cross section of the charge configuration in the figure, all shapes continue infinitely in the *z* direction.



a) Find the electric field *vector* on the *x* axis for all values of  $-\infty < x < \infty$ 



b) Find the electric field *vector* at the point (x, y) = (3a, 4a)



ExamRoom:	P101_Index:
Student ID Number:	Signature:

**3-(25 Points)** <u>Answer the following questions. Show your calculations. Unjustified answers will</u> <u>not be given any score. Write your answers in the boxes; answers outside the boxes will not be</u> given any score.

(i) Find the potential at a distance z above the centre of a thin disk of Radius R with uniform charge distribution  $\sigma$ .

(ii) Using the electric field of a uniformly charged solid sphere of radius R and total charge Q, which is given by

$$\vec{E} = \begin{cases} \frac{1}{4\pi\varepsilon_0} \frac{Q}{r^2} \hat{r}, & \text{outside (r>R);} \\ \frac{1}{4\pi\varepsilon_0} \frac{Q}{R^3} r \hat{r}, & \text{inside (r$$

find the potential inside and outside the sphere.



(iii) The potential of a charge distribution is given by  $V(x, y, z) = Ax^2y^2 + Bxyz$ , where A, B, and C are constants and x, y, and z are the Cartesian coordinates. Find the electric field.



(iv) How much work does it take to assemble a charge configuration where four charges of  $q_1=q$ ,  $q_2=q$ ,  $q_3=q$ , and  $q_4=q$  are located at the corners of



ExamRoom:	P101_Index:
Student ID Number:	Signature:

**4-(25 Points)** Two concentric spherical conducting shells are separated by vacuum. The inner shell has radius  $r_a$  and a total charge +Q, while the outer shell has radius  $r_b$  and a total charge -Q.

*Give your answers in terms of Q,*  $r_a$ ,  $r_b$ , and  $\varepsilon_0$ .

a) Calculate the electric-field energy density at a point a distance *r* from the center of the sphere for  $r < r_a$ ,  $r_a < r < r_b$ , and  $r > r_b$ .



b) Calculate the total electric field energy associated with the charged spheres.



c) By using  $U = Q^2/2C$ , calculate the capacitance of the system.

