| Name: | Signature: |
| :--- | :--- |
| Surname: | Number: |

KOÇ UNIVERSITY<br>College of Sciences<br>PHYS 102 General Physics 2<br>Spring Semester 2017<br>Midterm Exam 1<br>March 14, 2017 Thursday, 19:00-20:40

## Please read.

- Count to make sure that there are 5 pages in this question booklet
- Check your name, number, on front page, and student ID on each page.
- This examination is conducted with closed books and notes.
- Put all your personal belongings underneath your seat and make sure that pages of books or notebooks are not open.
- Absolutely no talking or exchanging anything (like rulers, erasers) during the exam.
- You must show all your work to get credit; you will not be given any points unless you show the details of your work (this applies even if your final answer is correct).
- Write neatly and clearly; unreadable answers will not be given any credit.
- If you need more writing space, use the backs of the question pages and put down the appropriate pointer marks.
- Make sure that you include units in your results.
- Make sure that you label the axis and have units in your plots.
- You are not allowed to use calculators during this exam.
- Turn off your mobile phones, and put away.
- You are not allowed to leave the class during the first 15 minutes, and last 15 minutes.

P102_Index:

| 1 | 2 | 3 | 4 | Total |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |


| ExamRoom: | P101_Index: |
| :--- | :--- |
| Student ID Number: | Signature: |

1-(25 Points) Two identical point charges with charge $Q$ are positioned a distance $d$ apart. Another point charge $q$ is placed in the middle of the two.
a) Find the charge $q$ (in terms of $Q$ ) if the system is in equilibrium.

b) Assume the charges reside on the $x$-axis and the charge $q$ is at the origin (see figure). Find the point on the positive $y$-axis where the electric field is zero.
c) Is the charge $q$ in stable equilibrium? Are the charges $Q$ in stable equilibrium? Give your answers by considering a small horizontal displacement of the charge and checking if you get a restoring force.


| ExamRoom: | P101_Index: |
| :--- | :--- |
| Student ID Number: | Signature: |

2-(25 Points) 2) Four infinite, non-conducting planes each with uniform surface charge density $\sigma$ are perpendicular to the $x-y$ plane, and they intersect each other to form a square of side $2 a$. An infinitely long, non-conducting, thin cylindrical shell of radius $a$ is also parallel to the planes (its central axis is the $z$ axis). The cylindrical shell has uniform surface charge density $-\sigma$. You can see the cross section of the charge configuration in the figure, all shapes continue infinitely in the $z$ direction.

a) Find the electric field vector on the $x$ axis for all values of $-\infty<x<\infty$
b) Find the electric field vector at the point $(x, y)=(3 a, 4 a)$


| ExamRoom: | P101_Index: |
| :--- | :--- |
| Student ID Number: | Signature: |

3-(25 Points) Answer the following questions. Show your calculations. Unjustified answers will not be given any score. Write your answers in the boxes; answers outside the boxes will not be given any score.
(i) Find the potential at a distance $z$ above the centre of a thin disk of Radius R with uniform charge distribution $\sigma$.

(ii) Using the electric field of a uniformly charged solid sphere of radius $R$ and total charge $Q$, which is given by $\vec{E}= \begin{cases}\frac{1}{4 \pi \varepsilon_{0}} \frac{Q}{r^{2}} \hat{r}_{s} & \text { outside }(\mathrm{r}>\mathrm{R}) ; \\ \frac{1}{4 \pi \varepsilon_{0}} \frac{Q}{R^{\mathrm{a}}} r \hat{r}_{s} & \text { inside }(\mathrm{r}<\mathrm{R}),\end{cases}$
find the potential inside and outside the sphere. $\square$
(iii) The potential of a charge distribution is given by $V(x, y, z)=A x^{2} y^{2}+B x y z$, where $A, B$, and $C$ are constants and $x, y$, and $z$ are the Cartesian coordinates. Find the electric field.

(iv) How much work does it take to assemble a charge configuration where four charges of $\mathrm{q}_{1}=\mathrm{q}, \mathrm{q}_{2}=\mathrm{q}, \mathrm{q}_{3}=\mathrm{q}$, and $\mathrm{q}_{4}=\mathrm{q}$ are located at the corners of $\square$

| ExamRoom: | P101_Index: |
| :--- | :--- |
| Student ID Number: | Signature: |

4-(25 Points) Two concentric spherical conducting shells are separated by vacuum. The inner shell has radius $r_{a}$ and a total charge $+Q$, while the outer shell has radius $r_{b}$ and a total charge -Q.
Give your answers in terms of $Q, r_{a}, r_{b}$, and $\varepsilon_{0}$.
a) Calculate the electric-field energy density at a point a distance $r$ from the center of the sphere for $r<r_{a}, r_{a}<r<r_{b}$, and $r>r_{b}$.

b) Calculate the total electric field energy associated with the charged spheres.

c) By using $U=Q^{2} / 2 C$, calculate the capacitance of the system.


