

Closed book. No calculators are to be used for this quiz.

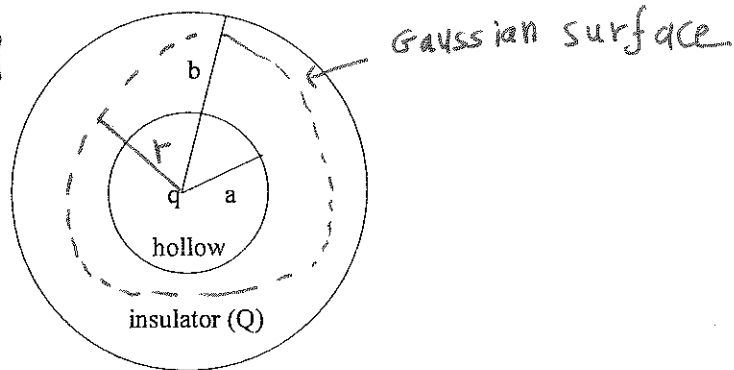
Quiz duration: 10 minutes

Name:

Student ID:

Signature:

Consider the insulating solid sphere with a hollow cavity shown in the figure. The total charge  $Q$  is uniformly distributed over the insulating material, and there is a point charge  $q$  at the center of the cavity. First identify the volume/surface/line charge density within the insulator and use the Gauss law to calculate the electric field for  $a < r < b$ .



The volume of the insulating spherical shell is

$$V = \frac{4}{3} \pi (b^3 - a^3)$$

The charge density  $\rho$  is

$$\rho = \frac{Q}{V} = \frac{Q}{\frac{4}{3} \pi (b^3 - a^3)}$$

by applying Gauss's law, we calculate the electric field in the region  $a < r < b$

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q_{enc}}{\epsilon_0}$$

$$E \cdot 4\pi r^2 = \frac{q + Q_{ins.}}{\epsilon_0}$$

charge in the insulator

$$E = \frac{q + Q_{ins.}}{4\pi r^2 \epsilon_0}$$

$$Q_{ins.} = \int V = \rho \cdot \frac{4\pi (r^3 - a^3)}{3} = \frac{Q}{\frac{4}{3} \pi (b^3 - a^3)} \cdot \frac{4\pi (r^3 - a^3)}{3} = \frac{Q (r^3 - a^3)}{(b^3 - a^3)}$$

$$\vec{E} = \frac{1}{4\pi \epsilon_0 r^2} \left( q + \frac{Q (r^3 - a^3)}{(b^3 - a^3)} \right) \hat{r}$$

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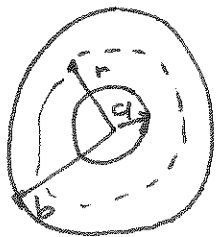
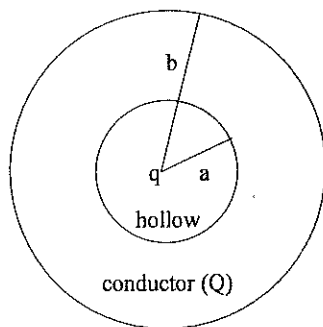
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Consider the conducting solid sphere with a hollow cavity shown in the figure. The total charge on the conductor is  $Q$ , and there is a point charge  $q$  at the center of the cavity. First identify the volume/surface/line charge density within the conductor and use the Gauss law to calculate the electric field for  $r > b$ .

surface density at the inner surface of the conductor. (charges are on the surfaces of the conductor)



$E = 0 \Rightarrow$  inside conductor

$$\oint \vec{E} \cdot d\vec{a} = 0 = \frac{Q_{enc}}{\epsilon_0} \Rightarrow Q_{enc} = 0$$

from conservation of charges

$$Q_{enc} = q + Q_{in} = 0 \Rightarrow \boxed{Q_{in} = -q}$$

charge surface density

$$\boxed{\sigma_{in} = \frac{Q_{in}}{A_{in}} = \frac{-q}{4\pi a^2}}$$

\* outer surface:  $Q = Q_{in} + Q_{out}$  (from charge conservation)

$$Q = -q + Q_{out} \Rightarrow \boxed{Q_{out} = Q + q}$$

The surface charge density

$$\sigma_{\text{out}} = \frac{Q_{\text{out}}}{A_{\text{out}}} = \frac{Q + q}{4\pi b^2}$$

when  $r > b$ : using Gauss's law, we find



$$\oint \vec{E} \cdot d\vec{a} = \frac{Q_{\text{enc}}}{\epsilon_0}$$

$$E \cdot 4\pi r^2 = \frac{q + Q}{\epsilon_0}$$

$$\vec{E} = \frac{q + Q}{4\pi r^2 \epsilon_0} \hat{r}$$

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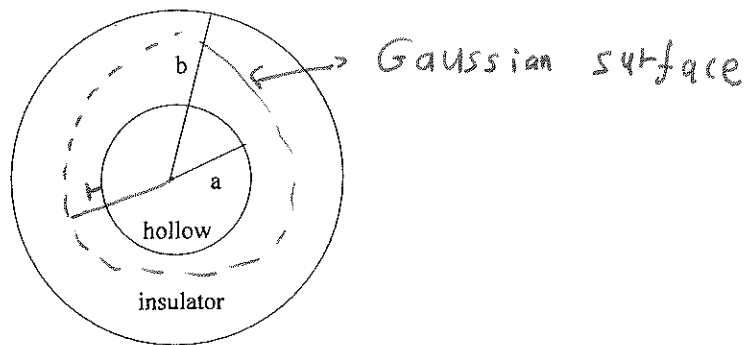
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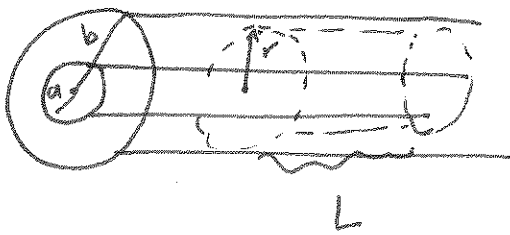
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Consider the infinitely long solid cylinder with a hollow cavity shown in the figure. The cylinder is made of an insulating material and it is uniformly charged with a volume charge density  $\rho$ . Use the Gauss law to calculate the electric field for  $a < r < b$ .

$a < r < b$



(top view of the cylinder)



using Gauss's law we find the electric field

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q_{enc}}{\epsilon_0} = \frac{\rho V}{\epsilon_0}$$

$$E \cdot 2\pi rL = \frac{\rho}{\epsilon_0} \pi (r^2 - a^2)L$$

$$\vec{E} = \frac{\rho (r^2 - a^2)}{2\epsilon_0 r} \hat{r}$$

Section 4

Quiz 2

18 February 2016

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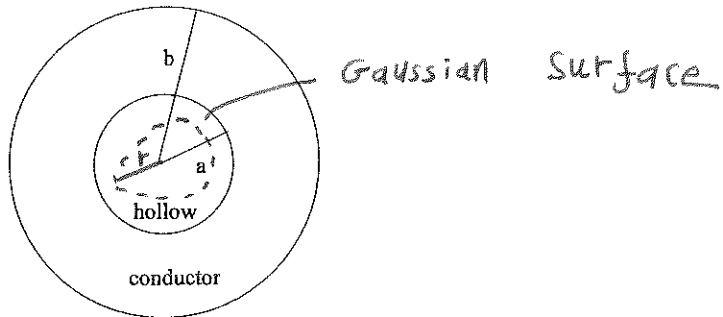
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Consider the infinitely long solid cylinder with a hollow cavity shown in the figure. The cylinder is made of a conducting material and its charge per unit length  $C$  is a constant. Use the Gauss law to calculate the electric field **everywhere** in space.

When  $r < a$ :

$$\oint \vec{E} \cdot d\vec{q} = \frac{Q_{enc}}{\epsilon_0} = 0$$

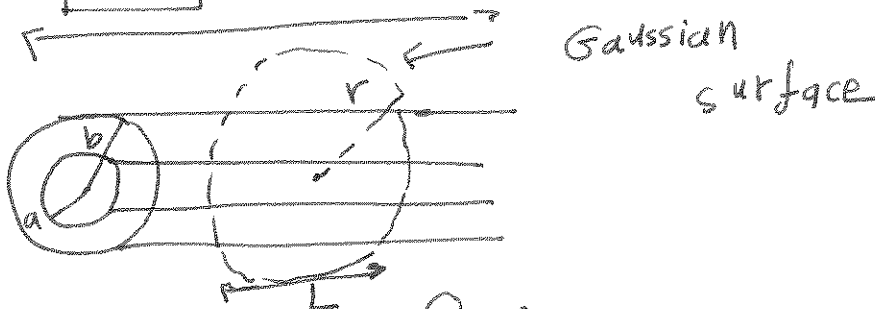
$$\Rightarrow \boxed{E=0}$$



(top view of the cylinder)

$a < r < b$ :  $\boxed{E=0}$  inside conductor  $\vec{E}$  is always zero

$r > b$ :



$$\oint \vec{E} \cdot d\vec{a} = \frac{Q_{enc}}{\epsilon_0}$$

$$E \cdot 2\pi r L = \frac{cL}{\epsilon_0}$$

$$\boxed{\vec{E} = \frac{c}{2\pi r \epsilon_0} \hat{r}}$$