# KOÇ UNIVERSITY <br> MATH 102 - CALCULUS <br> Final Exam <br> January 22, 2009 

Duration of Exam: 90 minutes

INSTRUCTIONS: No calculators may be used on the test. No books, no notes, and no talking allowed. You must always explain your answers and show your work to receive full credit. Use the back of these pages if necessary. Print (use CAPITAL LETTERS) and sign your name, and indicate your section below.

Surname, Name:

Signature: $\qquad$

Section (Check One):

> Section 1: T. Etgü (11:00)
> Section 2: T. Etgü (15:30)
> Section 3: S. Ünver $(9: 30)$

| PROBLEM | POINTS | SCORE |
| :---: | :---: | :---: |
| 1 | 20 |  |
| 2 | 20 |  |
| 3 | 20 |  |
| 4 | 20 |  |
| 5 | 20 |  |
| TOTAL | $\mathbf{1 0 0}$ |  |

Problem 1. Compute the following:
(i) $\lim _{x \rightarrow 9} \frac{3-\sqrt{x}}{9-x}$
(ii) $\lim _{x \rightarrow \infty}\left(x-\sqrt{x^{2}-3 x}\right)$
(iii) $\frac{d}{d x}(x \sqrt{x-\sqrt{x}})$
(iv) $\frac{d}{d x}\left(\cos \left(1+x^{2}\right)\right)$

Problem 2. Find the volume of the solid obtained by rotating the region between the curve $y=\sqrt{3 \cos x}$ and the lines $y=0, x=0, x=\pi / 2$ about the x -axis. $\quad(20 \mathrm{pts}$.)

Problem 3. Compute the following:
(i) $\arctan \left(\tan \left(\frac{5 \pi}{4}\right)\right)$
(ii) $e^{3 \ln x}$
(iii) $\frac{d}{d x}\left(\ln \left(3+2 x^{3}\right)\right)$
(iv) $\frac{d}{d x}\left(e^{\sin x}\right)$
(v) $\int_{1}^{4} \frac{d x}{x}$

Problem 4. Compute the following integral using integration by parts:

$$
\int x^{2} e^{4 x} d x
$$

Problem 5. Compute the following integral using partial fractions: (20 pts.)

$$
\int \frac{x^{2}+2 x-1}{(x-1)\left(x^{2}+1\right)} d x
$$

