| KOÇ UNIVERSITY  |                    |  |
|-----------------|--------------------|--|
| FALL 2017       | MATH102            |  |
| MIDTERM 2       | December 9, $2017$ |  |
| Duration of the | exam: 75 minutes   |  |

Instructions: Calculators are not allowed. No books, no notes, no talking allowed. Explain your answers to get full credit. You can use the back of these pages.

Name, Surname:

Signature: \_\_\_\_\_

Section:

 $\Box$  1 (Mo & We 14.30-15.45)  $\Box$  2 (Mo & We 16.00-17.15)

| Problem | Points | Score |
|---------|--------|-------|
|         |        |       |
| 1       | 30     |       |
| 2       | 25     |       |
| 3       | 25     |       |
| 4       | 25     |       |
| Total   | 105    |       |

a) Use implicit differentiation to find an equation of the tangent line to the curve

$$x^2 + 2xy + 4y^2 = 12$$

at the point (2,1)

(10 points).

b) Find the limit

$$\lim_{x \to \infty} \left( 1 + \frac{a}{x} \right)^{bx}$$

where a, b > 0 are fixed numbers. (*Hint:L'Hospital*)

(10 points)

c) Find the absolute maximum and absolute minimum values of

$$f(x) = \ln(x^2 + x + 1)$$

on the interval [-1, 1].

(10 points)

| Sketch the curve $y = \frac{2x^2 + x - 1}{x^2}$ using the gu | idelines A-H. (25 points) |
|--|---------------------------|
| A Domain   | B Intercepts              |
| C Symmetry   | D Asymptotes              |
| E Intervals of Increase or Decrease                          | F Local Max./Min.         |
| G Concavity and Points of Inflection                         | H Sketch                  |



a) A piece of wire 10 m long is cut into two pieces. One piece is bent into a square and the other into a circle. How should the wire be cut so that the total area enclosed is (a) a maximum (b) a minimum? (Formulas for Circle with radius r: circumference  $2\pi r$ , area  $\pi r^2$ ) (20 points)



b) Evaluate the integral

(5 points)

$$\int_0^1 (3 + x\sqrt{x}) \ dx$$

a) Evaluate the integral

(5 points)

$$\int_{1}^{3} \frac{x^3 - 2x^2 - x}{x^2} \, dx$$

b) Evaluate the indefinite integral

(10 points)

$$\int \frac{\cos(\ln(x))}{x} \, dx$$

c) Evaluate the indefinite integral

(10 points)

$$\int \frac{2^x}{2^x + 3} \, dx$$