

(1.a) (10 pts) Find the following derivative.

$$\frac{d}{dx} \left(\int_x^{x^2-1} \sin^3(7t-1) dt \right)$$

(1.b) (10 pts) Given that the derivative of $e^x(x^2 - 2x - 1)$ is equal to $e^x(x^2 - 3)$ evaluate the following integral.

$$\int_0^1 e^x(x^2 - 3) dx$$

(2) Evaluate the following integrals.

(2.a) (10 pts)

$$\int x \cos x dx$$

(2.b) (10 pts)

$$\int \frac{4x^2}{(x+1)^2(x^2+1)} dx$$

Question 3: (15 Points)

- (a) Write an integral expression for the volume of the solid generated by revolving the region bounded by $y = -x + 2$, and the lines $y = 0$, $x = 0$, and $x = 2$, about the x-axis.
- (b) Write an integral expression for the volume of the solid generated by revolving the region bounded by $y = -x + 2$, and the lines $y = 0$, $x = 0$, and $x = 2$, about $y = 3$.
- (c) Write an integral expression for the volume of the solid generated by revolving the region bounded by $y = -x + 2$, and the lines $y = 0$, $x = 1$, and $x = 2$, about the y-axis.

Question 4: (10 Points)

Find the area of the region between the curve $y = 2 - \sqrt{x}$ and the x-axis for $0 \leq x \leq 4$.

Question 5: (10 Points)

Find the derivatives of the inverse functions $f^{-1}(x)$ of the following functions $f(x)$:

- (a) $f(x) = 2^x$
- (b) $f(x) = \log_3(x)$
- (c) $f(x) = 2 \sin(x)$

Question 6: (10 Points)

Find the integrals of the following functions:

- (a) $f(x) = x^\pi$
- (b) $f(x) = \pi^x$
- (c) $f(x) = 6 \tan(3x)$

Question 7: (40 Points)

Evaluate the following integrals

(a) $\int \cos^3(x) \sin(x) dx$

(b) $\int \frac{dx}{x^2 - 2x + 2}$

(c) $\int \frac{2x^3}{x^2 - 1} dx$

(d) $\int \frac{\log_2(x^2)}{x} dx$

Here are some derivatives :

1) $\frac{d}{dx} a^x = \ln(a) a^x$

2) $\frac{d}{dx} \log_a(x) = \frac{1}{x \ln(a)}$

3) $\frac{d}{dx} \tan(x) = \sec^2(x)$

4) $\frac{d}{dx} \cot(x) = -\csc^2(x)$

5) $\frac{d}{dx} \sec(x) = \sec(x) \tan(x)$

6) $\frac{d}{dx} \csc(x) = -\csc(x) \cot(x)$

7) $\frac{d}{dx} \sin^{-1}(x) = \frac{1}{\sqrt{1-x^2}}$

8) $\frac{d}{dx} \cos^{-1}(x) = \frac{-1}{\sqrt{1-x^2}}$

9) $\frac{d}{dx} \tan^{-1}(x) = \frac{1}{1+x^2}$

10) $\frac{d}{dx} \cot^{-1}(x) = \frac{-1}{1+x^2}$

11) $\frac{d}{dx} \sec^{-1}(x) = \frac{1}{|x| \sqrt{1-x^2}}$

12) $\frac{d}{dx} \csc^{-1}(x) = \frac{-1}{|x| \sqrt{1-x^2}}$