

Selda Küçükçifçi  
Math 200: Multivariable Calculus and Matrix Algebra  
EXAM II

May 9, 2005

NAME: \_\_\_\_\_

1	/24
2	/18
3	/22
4	/16
5	/20
Total:	/100

WRITE ALL ANSWERS CLEARLY, AND SHOW ALL WORK TO GET CREDIT  
NO QUESTIONS, NO CALCULATOR, 90 MINUTES

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1. a) (6 points) Find the point in which the line through the origin perpendicular to the plane  $2x - y - z = 4$  meets the plane  $3x - 5y + 2z = 6$ .

b) (6 points) How can you tell when two planes  $A_1x + B_1y + C_1z = D$  and  $A_2x + B_2y + C_2z = D_2$  are parallel? Perpendicular? Give reasons for your answers.

c) (6 points) Is the line  $x = 1 + 3t, y = 2 - t, z = 2 + 3t$  parallel to the plane  $x - z = 5$ ? Give reasons for your answer.

d) (6 points) Describe the set of points in space that lie 2 units from the point  $(0, 0, 1)$  and at the same time 2 units from the point  $(0, 0, -1)$ .

2. a) (6 points) Replace the polar equation  $r = \sin \theta$  by a cartesian equation and sketch its graph.

b) (6 points) Graph  $r = 1 - \sin \theta$ .

c) (6 points) Find the points of intersection of  $r = \sin \theta$  and  $r = 1 - \sin \theta$ . Give the coordinates of the points of intersection both in cartesian and polar forms.

3. a) (8 points) Find the domain and the range of the function  $f(x, y) = \frac{1}{\sqrt{x^2 - y^2}}$ . Decide if the domain is bounded or unbounded. Explain your answer.

b) (8 points) Describe the level curves of this function.

c) (6 points) Find  $f_x(x, y)$  and  $f_{xy}(x, y)$ .

4. (8 points) a) What condition must the constants  $a, b$ , and  $c$  satisfy to guarantee that the  $\lim_{(x,y) \rightarrow (0,0)} \frac{xy}{ax^2 + bxy + cy^2}$  exists? Explain your answer.

b) (8 points) Suppose the equation  $x^2y + e^{x+2y} + \cos(xy^3) - 6 = 0$  defines  $y$  as a differentiable function of  $x$ . Find the value  $dy/dx$  at the point  $P(\ln 5, 0)$ .

5. a) (7 points) Find the tangent plane to the surface with equation  $z = x^4 - 4xy^3 + 6y^2 - 2$  at the point  $P(0, 1, 4)$ .

b) (7 points) Find the coordinates of all points on the surface in part (a) where the surface has a horizontal tangent plane.

c) (6 points) Find parametric equation for the line tangent to the intersection of the surface in part (a) and the plane with equation  $x + y - 1 = 0$  at the intersection point  $P(0, 1, 4)$ .