

---

KOÇ UNIVERSITY

MATH 200 - Multivariable Calculus and Matrix Algebra

Final Exam      June 1, 2009

**Duration of Exam: 120 minutes**

---

**INSTRUCTIONS:** Calculators are not allowed. No books, no notes, no questions and no talking allowed. You must always **explain your answers** and **show your work** to receive **full credit**. Use the back of these pages if necessary. **Print (use CAPITAL LETTERS)** and sign your name, and indicate your section below.

Surname, Name: \_\_\_\_\_

Signature: \_\_\_\_\_

Section (Check One):

Section 1: S. Küçükçifçi (Mon-Wed 11:00)      \_\_\_\_\_

Section 2: S. Küçükçifçi (Mon-Wed 15:30)      \_\_\_\_\_

PROBLEM	POINTS	SCORE
1	16	
2	16	
3	16	
4	18	
5	18	
6	16	
<b>TOTAL</b>	<b>100</b>	

1. (16 points) Let  $M$  be the matrix  $\begin{bmatrix} 3 & 2 & 1 \\ 0 & -1 & 3 \\ 0 & 5 & -4 \end{bmatrix}$ .

(a) Evaluate the determinant of  $M$  by elementary row operations.

(b) Evaluate the determinant by cofactor expansions (that is by using the formula).

2. (16 points) Compute  $A^{10}$  using the diagonalization of the matrix  $A$ , where

$$A = \begin{bmatrix} 1 & 0 \\ -1 & 2 \end{bmatrix}.$$

3. (16 points) (a) Find  $dy/dx$  if  $x^3 + y^3 = 6xy$ .

(b) Find the directions in which the directional derivative of  $f(x, y) = ye^{-xy}$  at the point  $(0, 2)$  has the value 1.

**4.** (18 points) Find all the local maxima, local minima, and saddle points of the function  $f(x, y) = x^2 + y^2 + x^2y + 4$ .

**5.** (18 points) Use Lagrange multipliers to find the maximum and minimum values of the function  $f(x, y, z) = 2x + 6y + 10z$  subject to the constraint  $x^2 + y^2 + z^2 = 35$ .

**6.** (16 points) (a) Evaluate  $\int_R \int (x + 2) dA$ , where  $R$  is the finite region bounded by the parabolas  $y = 2x^2$  and  $y = 1 + x^2$ .

(b) Reverse the order of the integration of the integral  $\int_0^1 \int_x^1 e^{x/y} dy dx$ . (Do not evaluate the integral.)